



# Solar Fire Investigation Analysis

## Concentrated Solar Reflective Irradiance from Low-E Glass

Presented by  
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**[Above Photos: 94 Charles Street, Whitman, MA –DOL: 1/13/2015]**

Better Buildings by Design Winter Conference – Burlington, Vermont



# Solar Fire

108 West Quincy Street, Somerville, MA (1/6/2018)



104/108 West Quincy Street, Somerville, MA  
(Maximum temperature observed: 480°F)



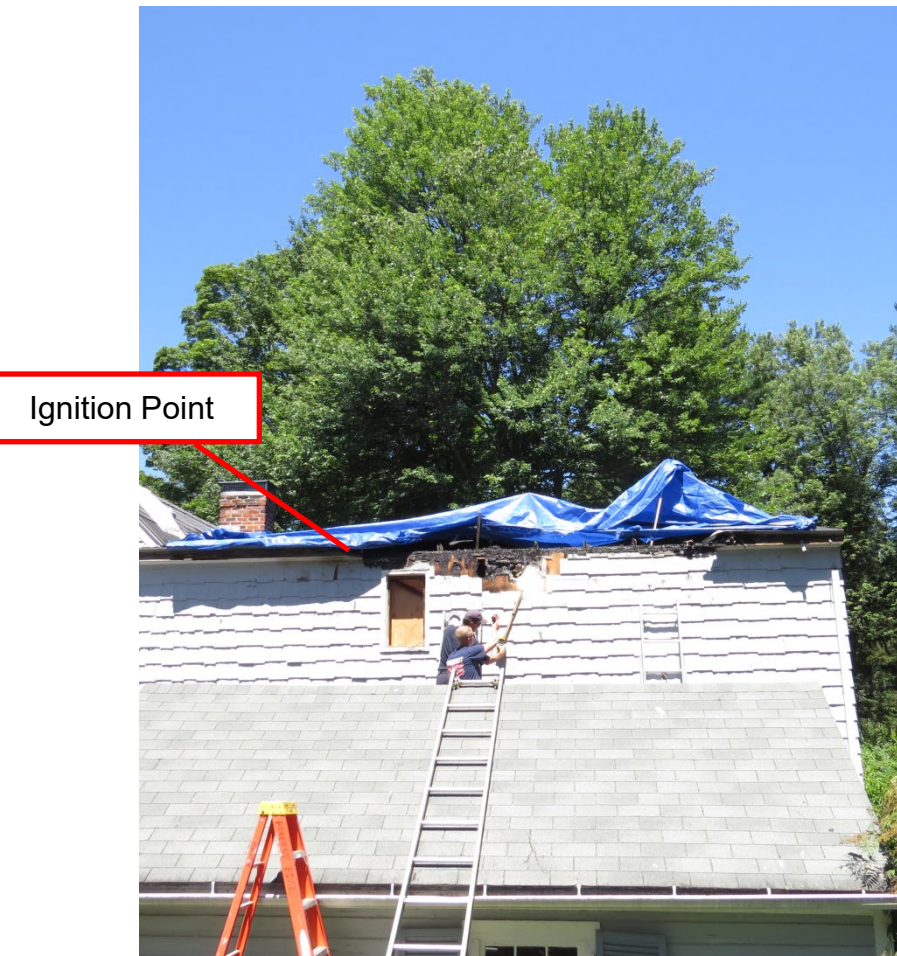


# 110 & 116 Blue Hills Road, Amherst, MA DOL: 7/8/2018



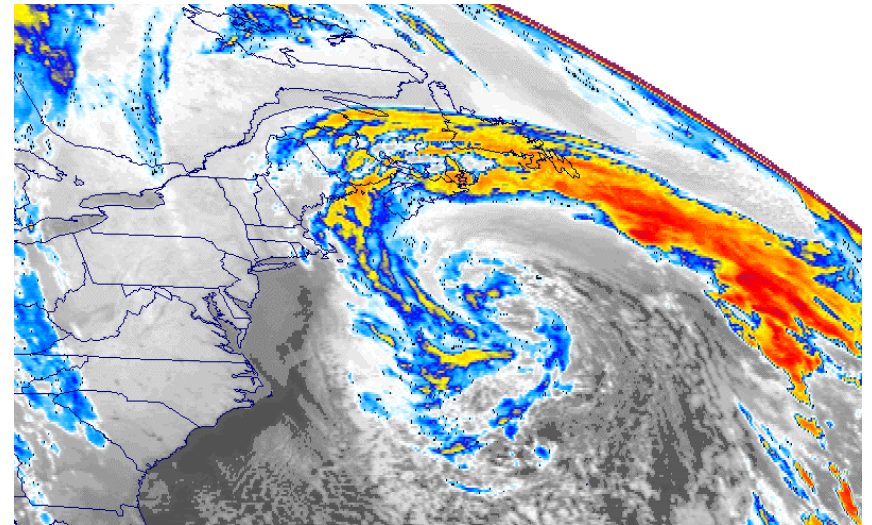


110 & 116 Blue Hills Road, Amherst, MA  
DOL: 7/8/2018



>Q] Why is this happening?

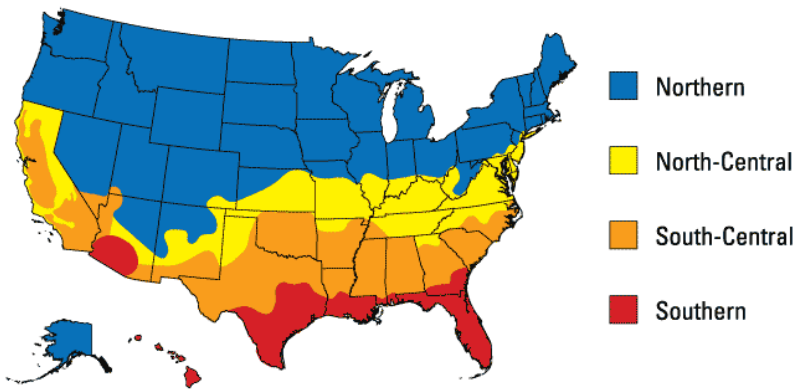
A] A Perfect Storm on a Sunny Day





# Energy Star, International Energy Code

[https://www.energystar.gov/products/building\\_products/residential\\_windows\\_doors\\_and\\_skylights/key\\_product\\_criteria](https://www.energystar.gov/products/building_products/residential_windows_doors_and_skylights/key_product_criteria)



WINDOWS			
CLIMATE ZONE	U-FACTOR <sup>1</sup>	SHGC <sup>2</sup>	
Northern	≤ 0.27	Any	Prescriptive
	≥ 0.28	≥ 0.32	Equivalent Energy Performance
	≥ 0.29	≥ 0.37	
	≥ 0.30	≥ 0.42	
North Central	≤ 0.30	≤ 0.40	
South Central	≤ 0.30	≤ 0.25	
Southern	≤ 0.40	≤ 0.25	

SKYLIGHTS		
CLIMATE ZONE	U-FACTOR <sup>1</sup>	SHGC <sup>2</sup>
Northern	≤ 0.50	Any
North Central	≤ 0.53	≤ 0.35
South Central	≤ 0.53	≤ 0.28
Southern	≤ 0.60	≤ 0.28

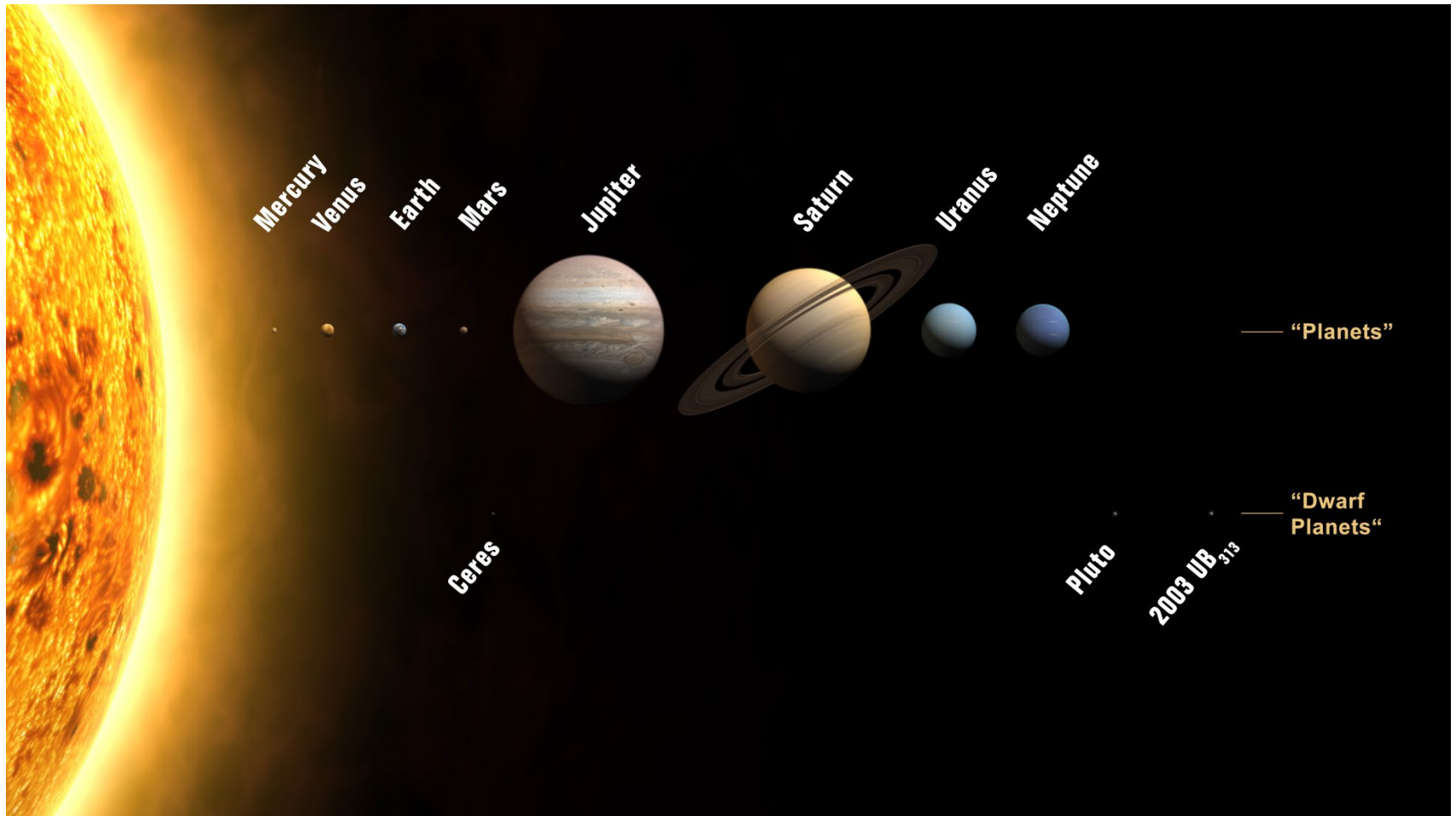
Air Leakage ≤ 0.3 cfm/ft<sup>2</sup>

<sup>1</sup> Btu/h ft<sup>2</sup>·°F  
<sup>2</sup> Solar Heat Gain Coefficient

# Our Solar System



# Our Solar System



# Solar Constant

$$P = \epsilon \sigma A T^4$$

$$\epsilon = 1.0 \text{ (Emissivity)}$$

Stefen Boltzmann Constant:

$$\sigma = 5.670367(13) \times 10^{-8} \text{ W/(m}^2\text{K}^4\text{)}$$

In US customary units:

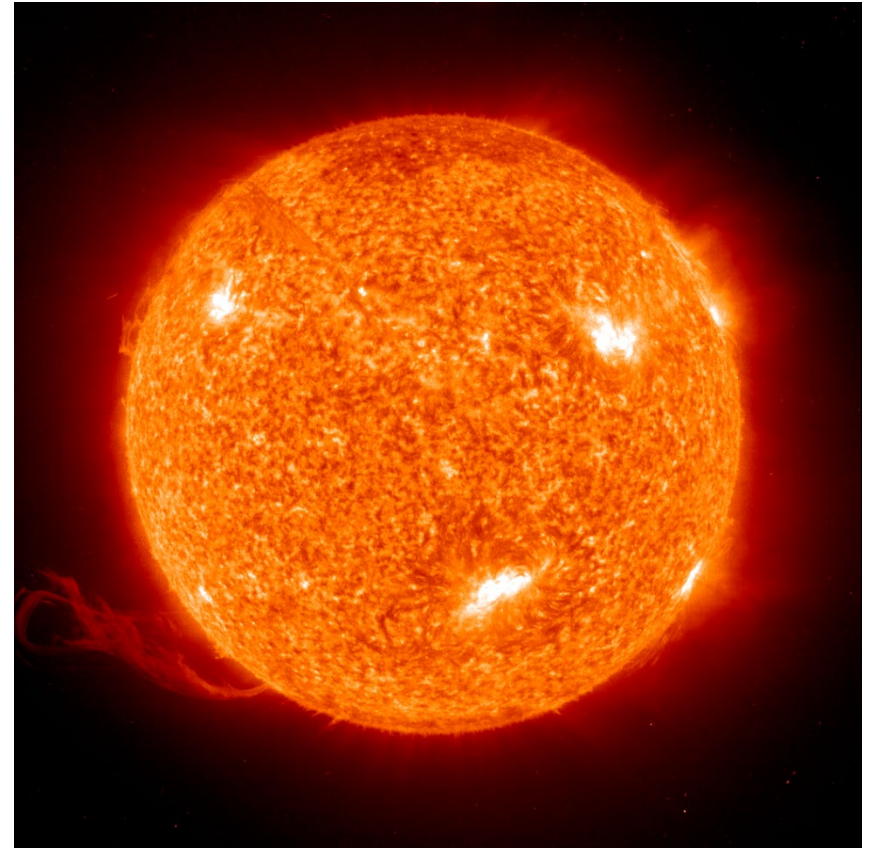
$$\sigma \approx 1.714 \times 10^{-9} \text{ BTU/( hr ft}^2 \text{ }^\circ\text{R}^4\text{)}$$

$$A = \text{Surface area of Sun} = 4 \pi R_{\text{sun}}^2 \quad R_{\text{sun}} = 695,700,000 \text{ m}$$

$$\text{Effective Temperature of Photosphere} = 5772 \text{ }^\circ\text{K}$$

$$P = 1.0 \cdot [5.67036713 \times 10^{-8} \text{ W/(m}^2\text{K}^4\text{)}] \cdot 4 \pi \cdot [6.957 \times 10^8 \text{ m}]^2 \cdot (5772 \text{ }^\circ\text{K})^4$$

$$\mathbf{> P = 3.9512 \times 10^{26} \text{ watts}}$$

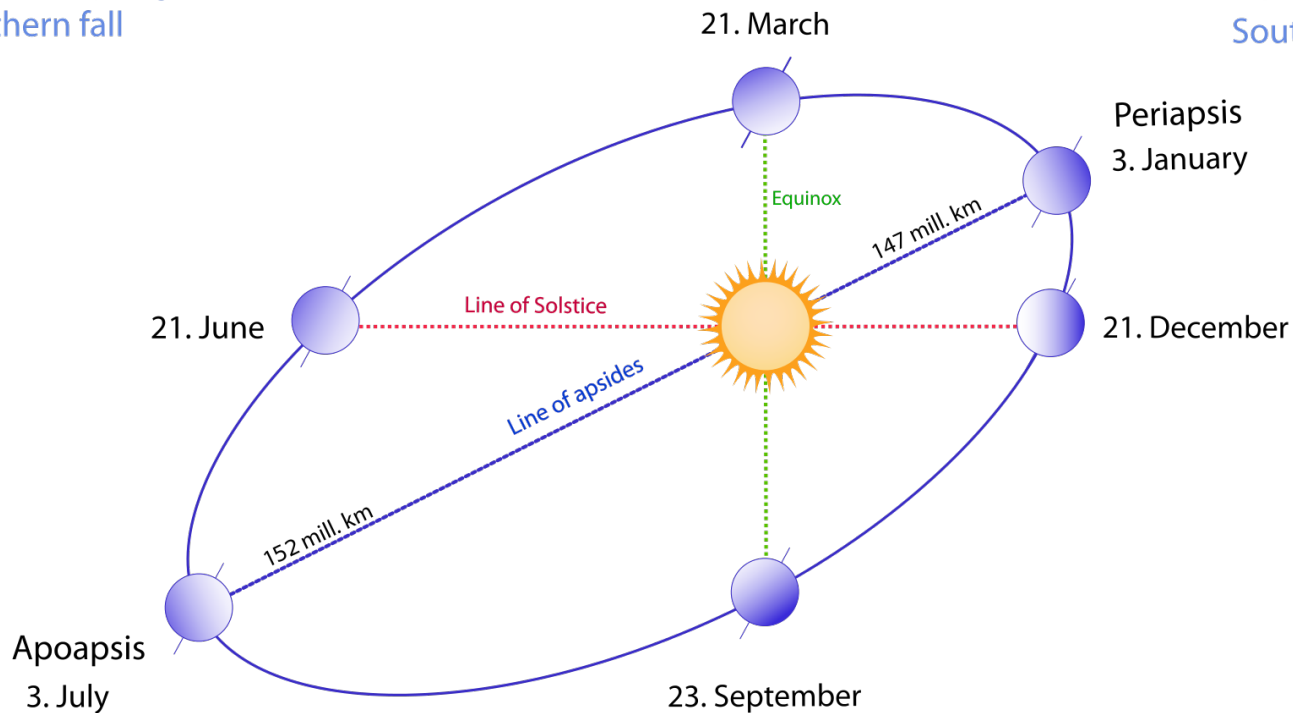




Perihelion: 147,100,000 km (91,420,479 mi)  
Aphelion: 152,100,000 km (94,525,254 mi)

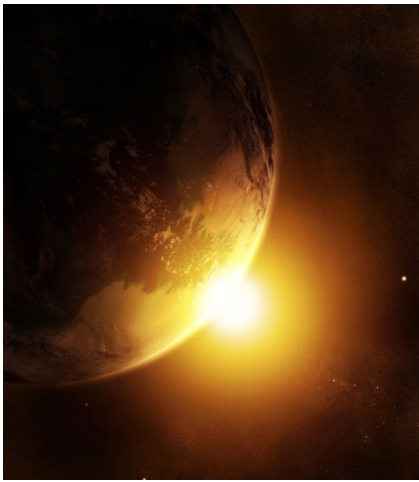
Northern spring/  
Southern fall

Northern winter/  
Southern summer

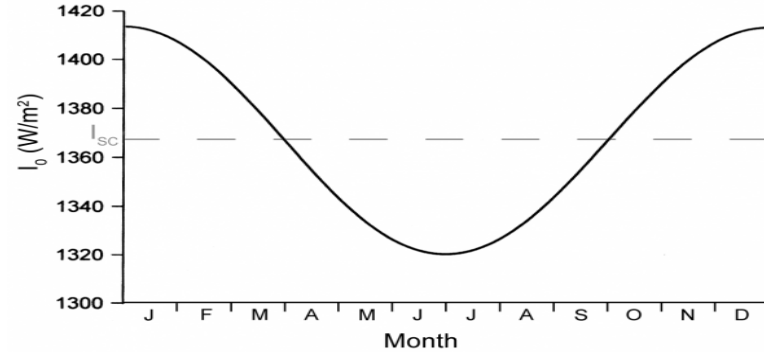
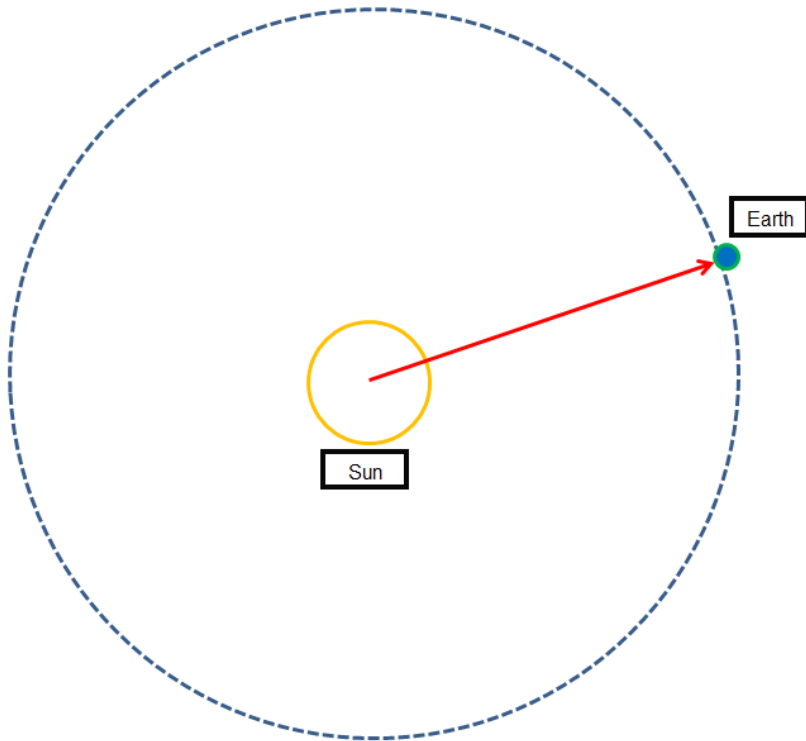


Northern summer/  
Southern winter

Northern fall/  
Southern spring



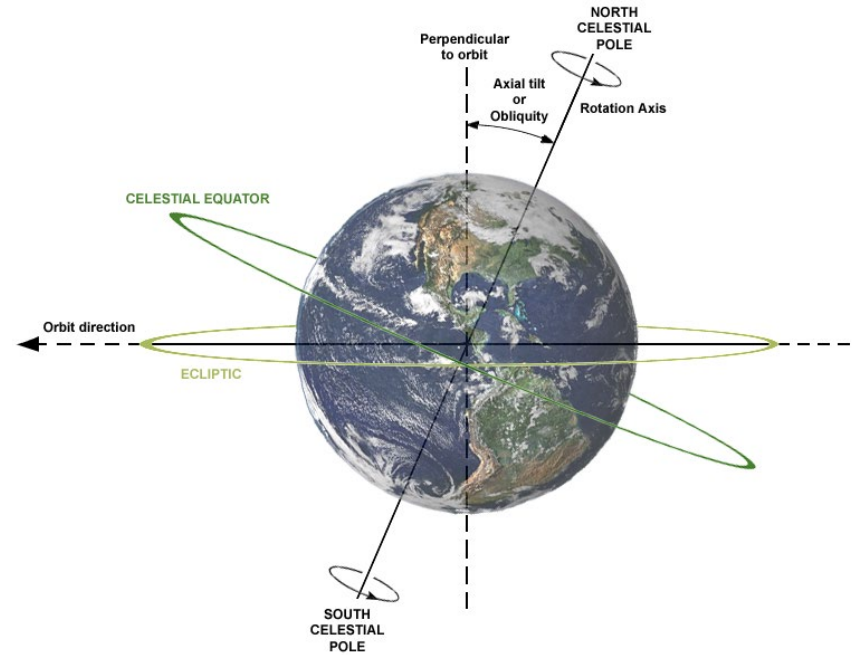
# Solar Constant



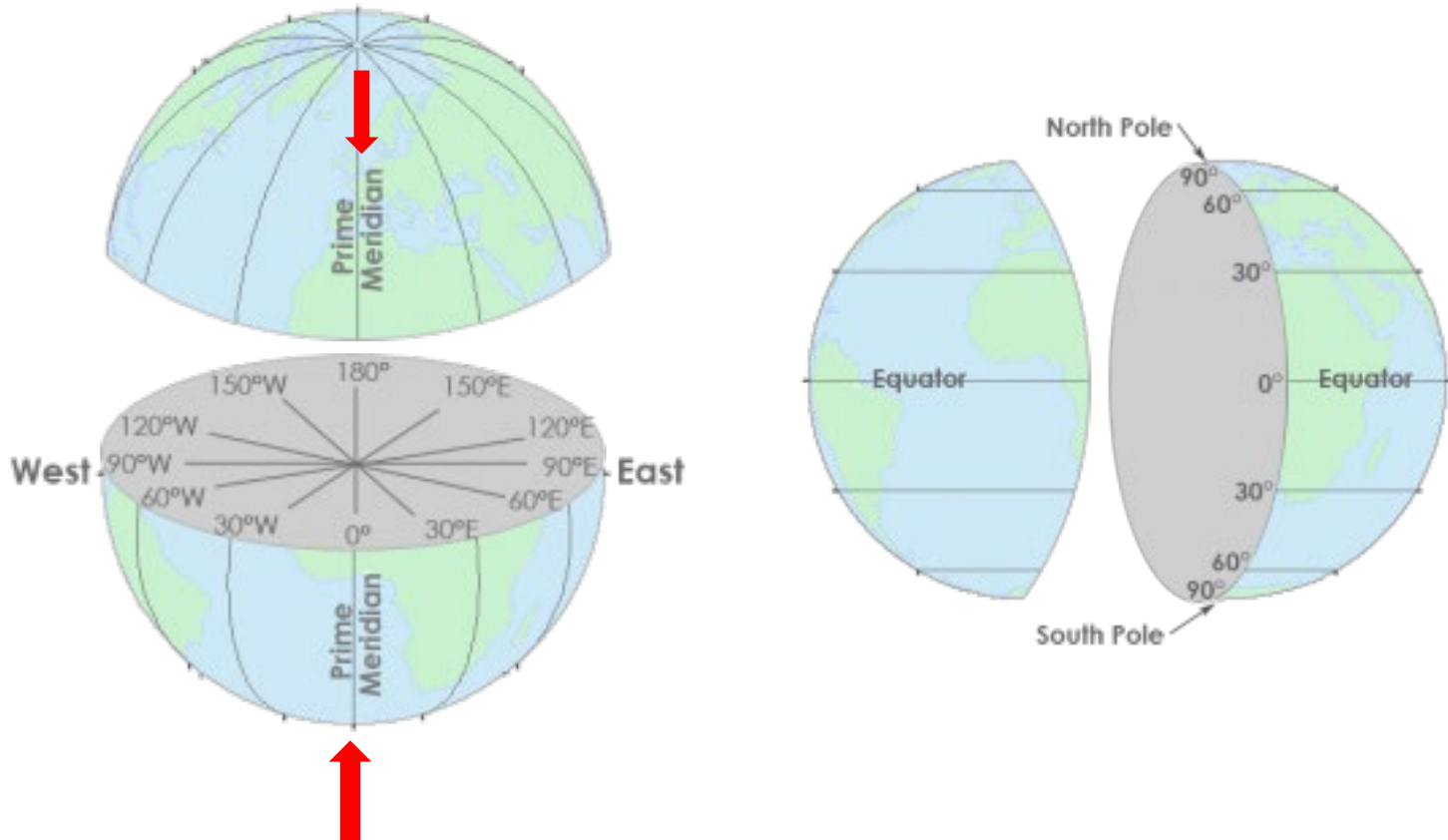
- $R =$  Average Sun to earth distance
  - $P = 3.9512 \times 10^{26}$  watts
  - $I = P/A; A = 4\pi R^2$
- > Perihelion: 147,100,000 km (91,420,479 mi)  
 $I_{\max} = 1419 \text{ W/m}^2$
- > Aphelion: 152,100,000 km (94,525,254 mi)  
 $I_{\min} = 1327 \text{ W/m}^2$

# The Earth

Diameter: 7,926 miles (12,756 km)  
Rotating at  $15^\circ/\text{hr}$ ; 1,040 miles/hr (at Equator)



# Longitude, Latitude





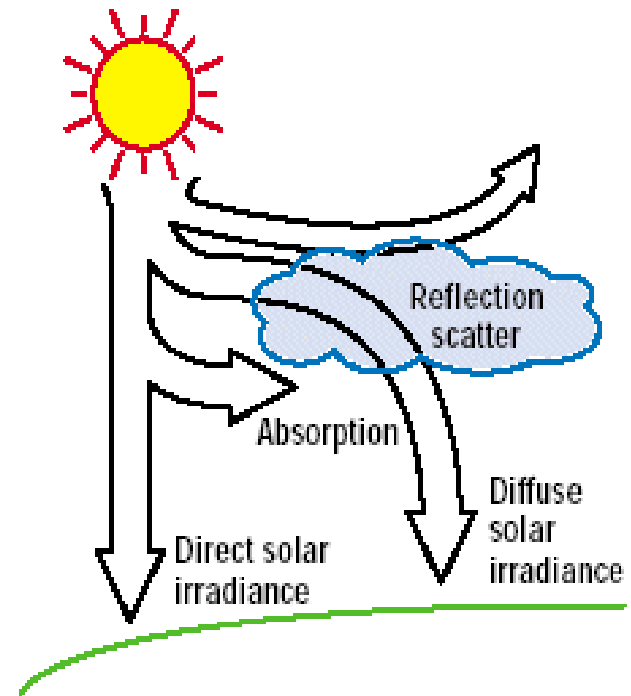
# Solar Insolation

## Pyranometer

Units: (W/m<sup>2</sup>) or (Btu/(hr-ft<sup>2</sup>))

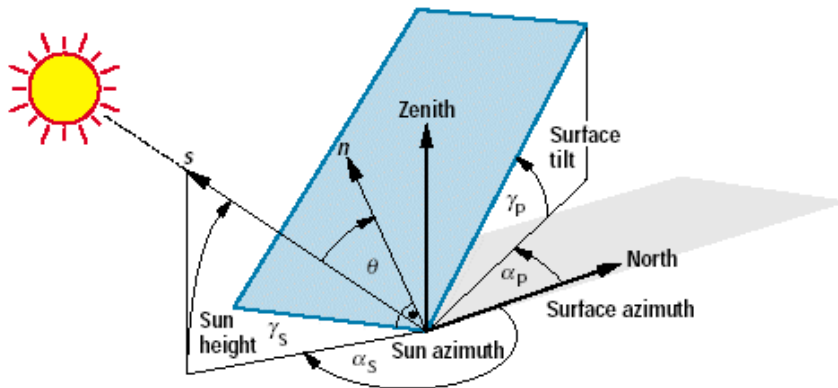


## Direct & Diffuse Insolation

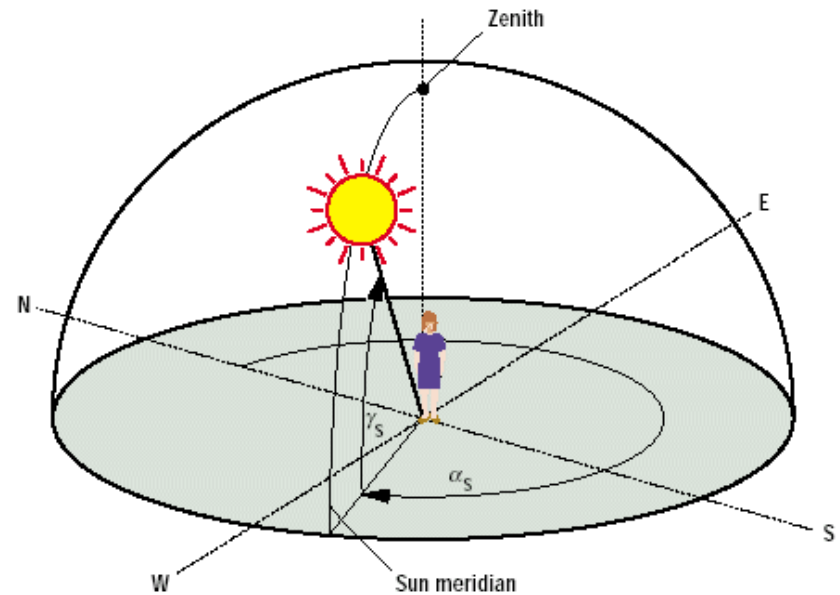


# Solar Insolation on Surfaces

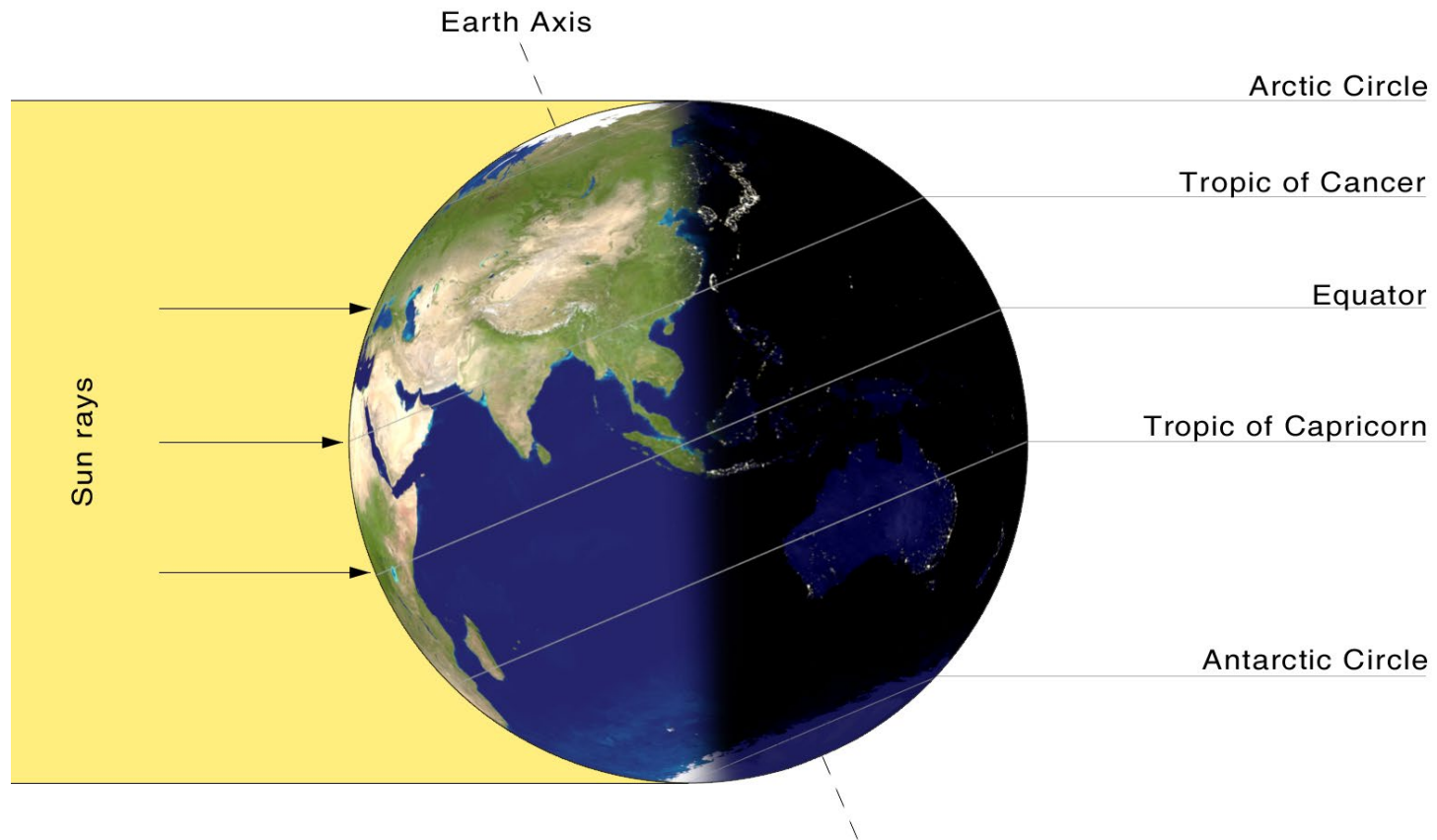
## On Tilted Surface



## On Horizontal Surface

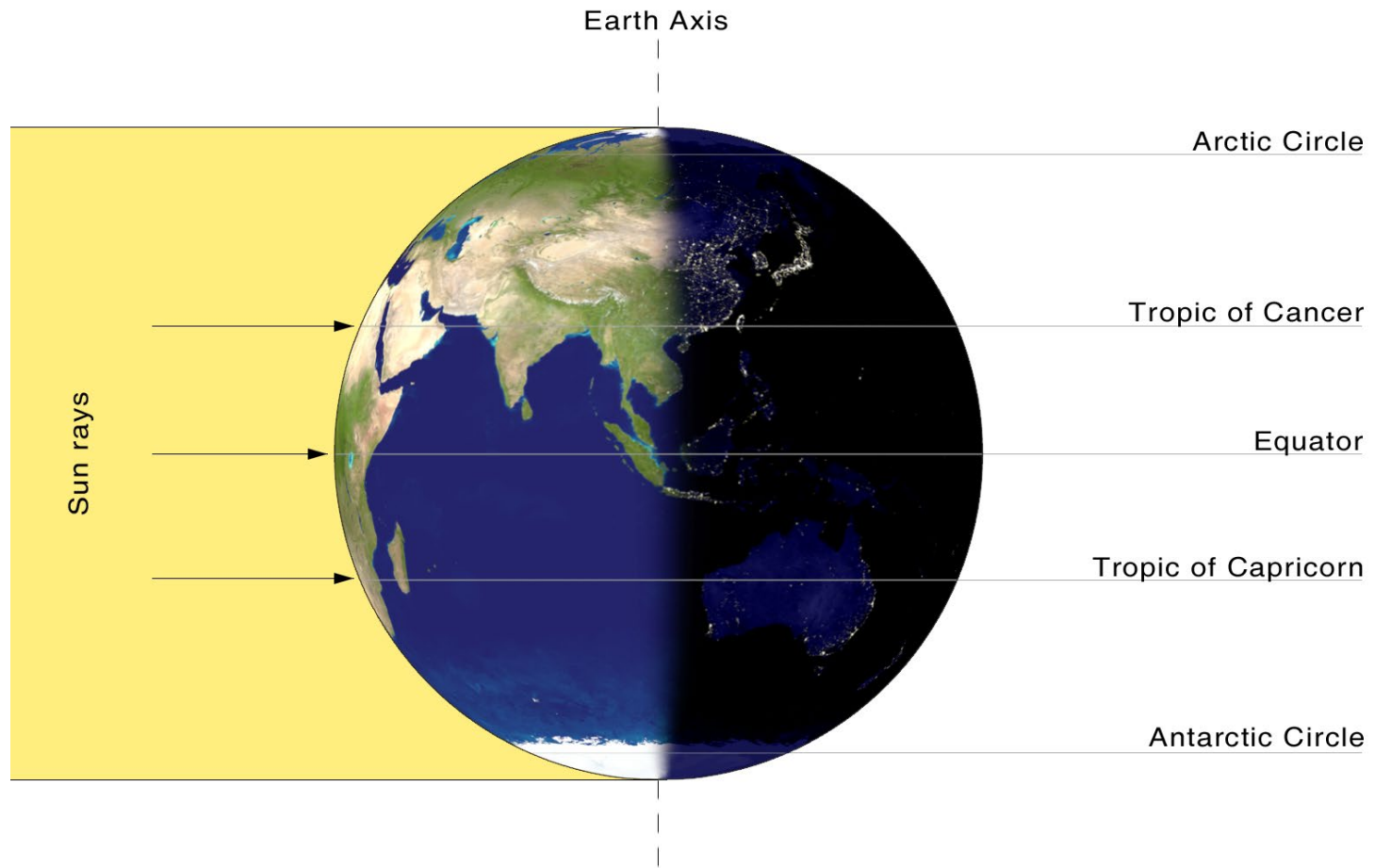


# Summer -North Hemisphere Winter - South Hemisphere

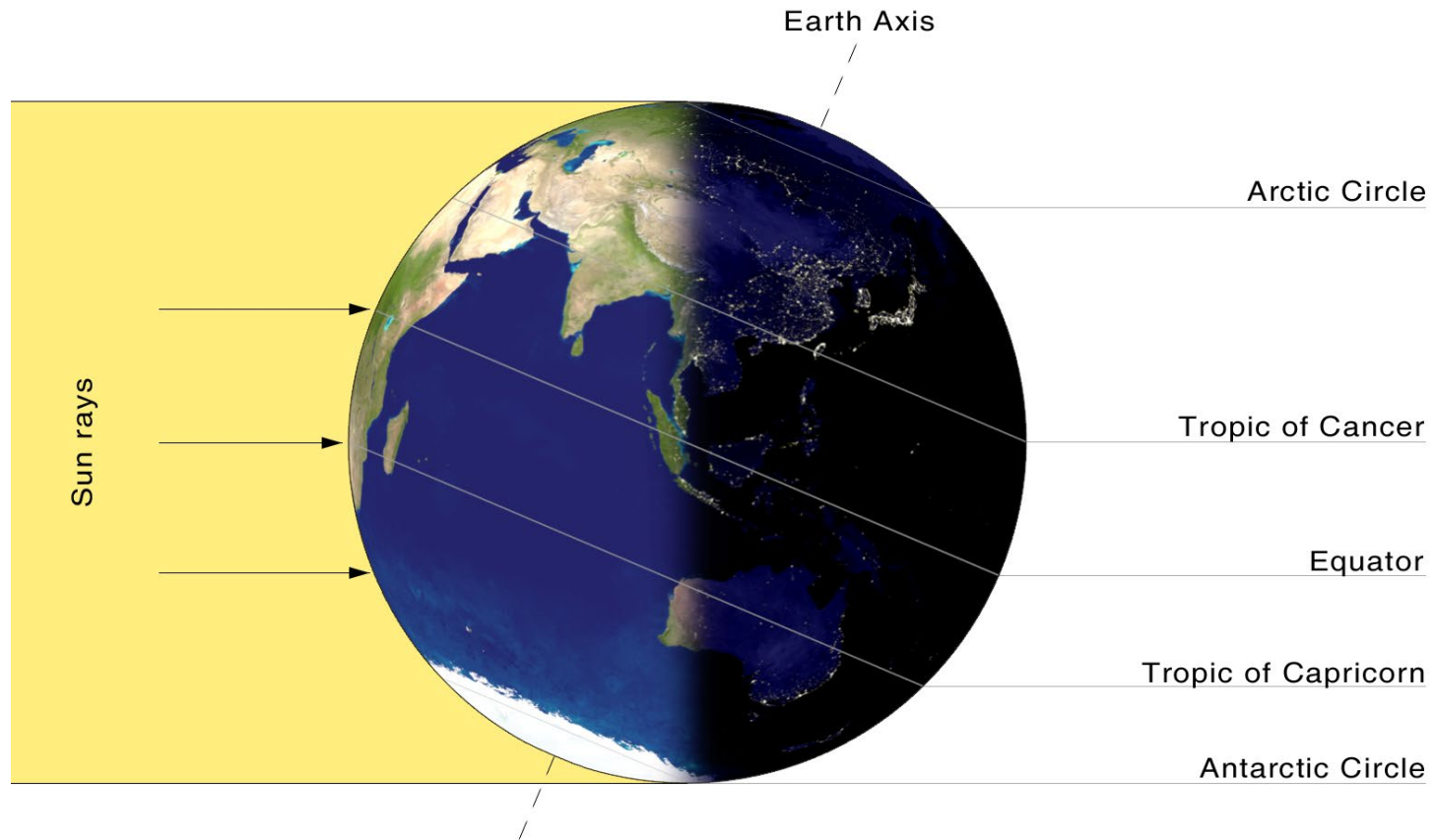




# March & September Equinox



# Winter - North Hemisphere Summer – South Hemisphere



# ASHRAE Clear Sky Equations



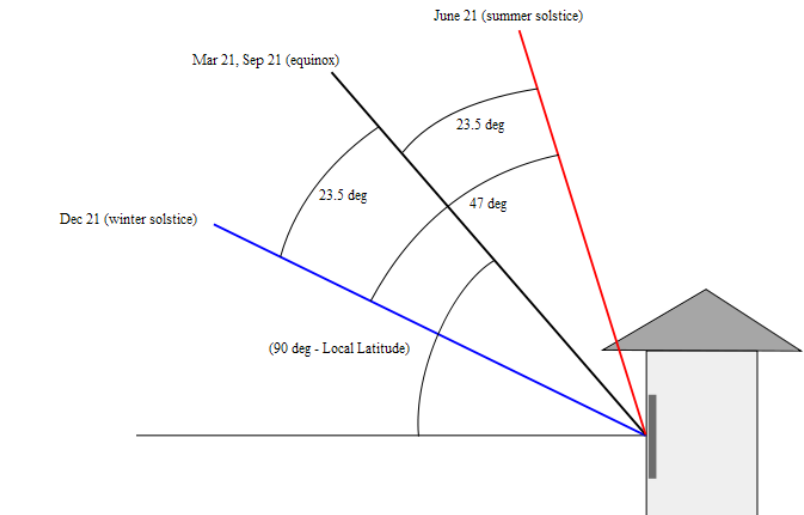
# ASHRAE Clear Sky Equations

## Reference History:

ASHRAE, Fundamentals Handbook, Chapter 29, 1997.

Solar Thermal Engineering, Lunde, 1980.

Solar Radiation of Surfaces on Clear Days," ASHRAE 1963

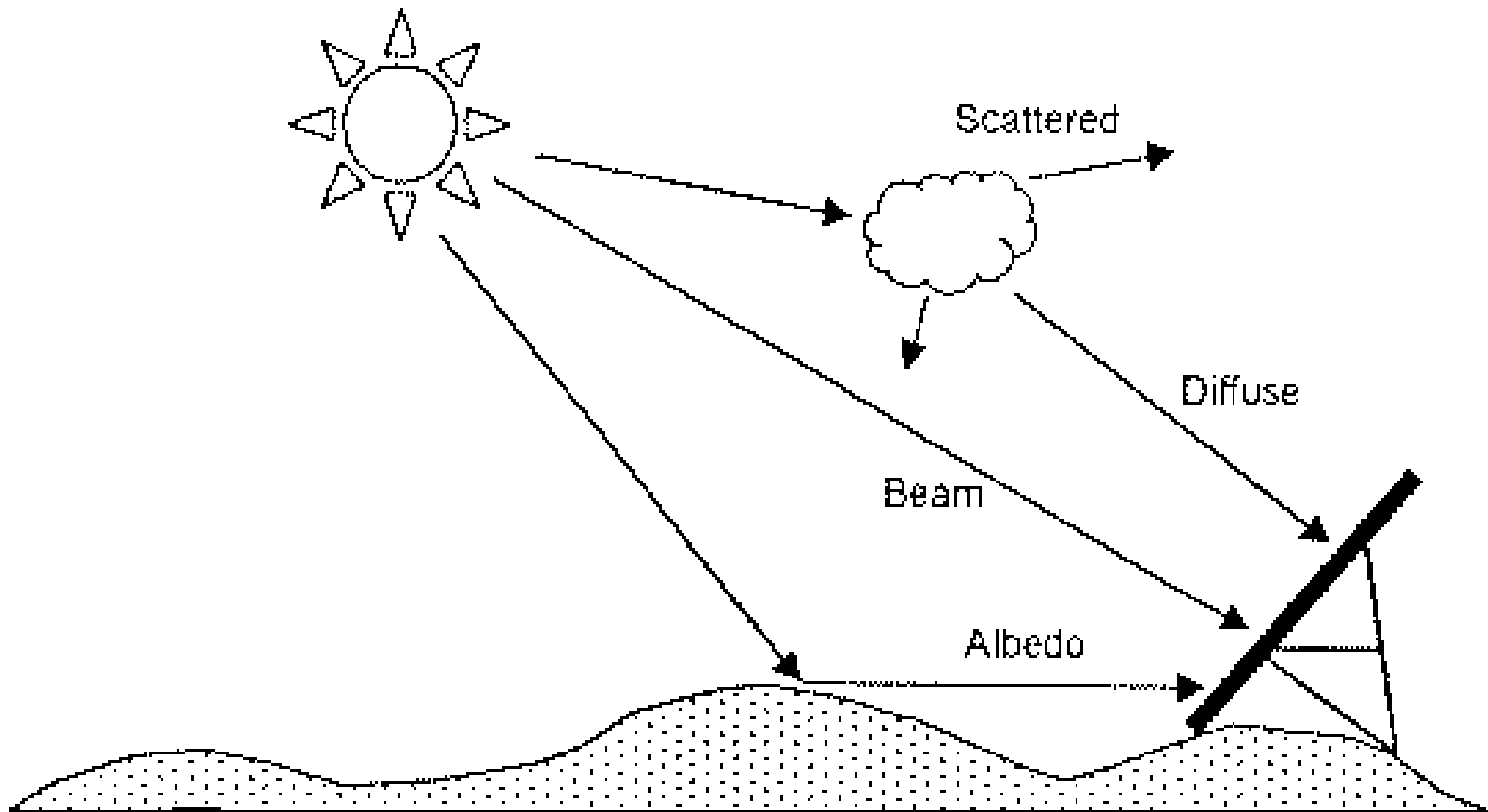


# Solar Insolation Parameters

$$[1.0 \text{ Btu}/(\text{h}\cdot\text{ft}^2) = 3.155 \text{ w}/\text{m}^2]$$

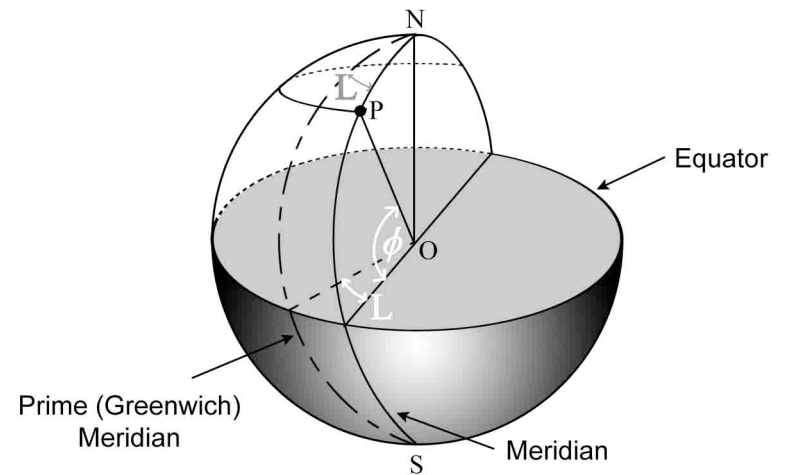
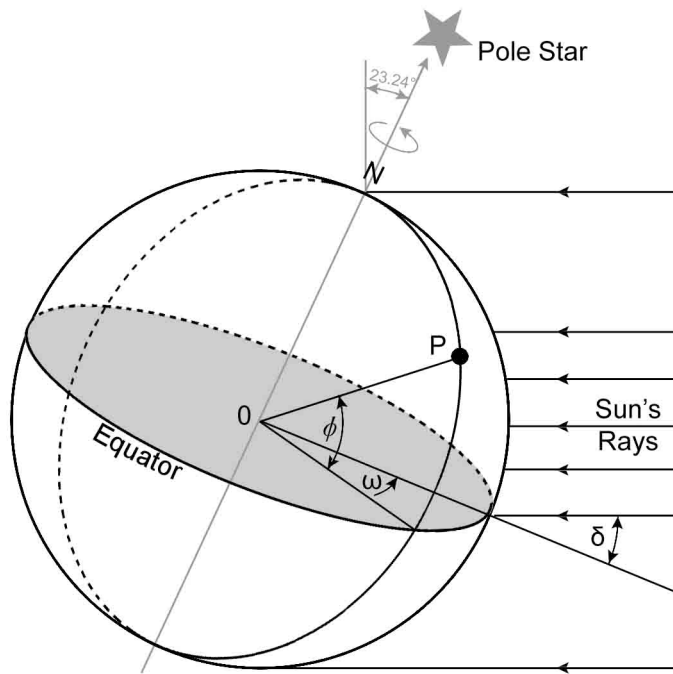
							DECLINA-	
			A	A'	B	C	TION	EQT
MONTH	DATE	DAY NO.	(BTU)/(HR-SF)	(W/SM)	(Dim Less)	(Dim Less)	(DEG)	(MIN)
JANUARY	21	21	390	1230	0.142	0.058	-19.76	-11.26
FEBRUARY	21	52	385	1215	0.144	0.060	-10.73	-14.19
MARCH	21	80	376	1186	0.156	0.071	0.00	-7.84
APRIL	21	111	360	1136	0.180	0.097	11.78	1.19
MAY	21	141	350	1104	0.196	0.121	20.17	3.54
JUNE	21	172	345	1088	0.205	0.134	23.45	-1.45
JULY	21	202	344	1085	0.207	0.136	20.57	-6.05
AUGUST	21	233	351	1107	0.201	0.122	12.13	-2.80
SEPTEMBER	21	264	365	1152	0.177	0.092	0.40	7.71
OCTOBER	21	294	378	1193	0.160	0.073	-11.09	15.83
NOVEMBER	21	325	387	1221	0.149	0.063	-19.97	13.43
DECEMBER	21	355	391	1234	0.142	0.057	-23.43	1.38

$$I_{\text{Total}} = I_{\text{Beam}} + I_{\text{Ground}} + I_{\text{Diffuse}}$$

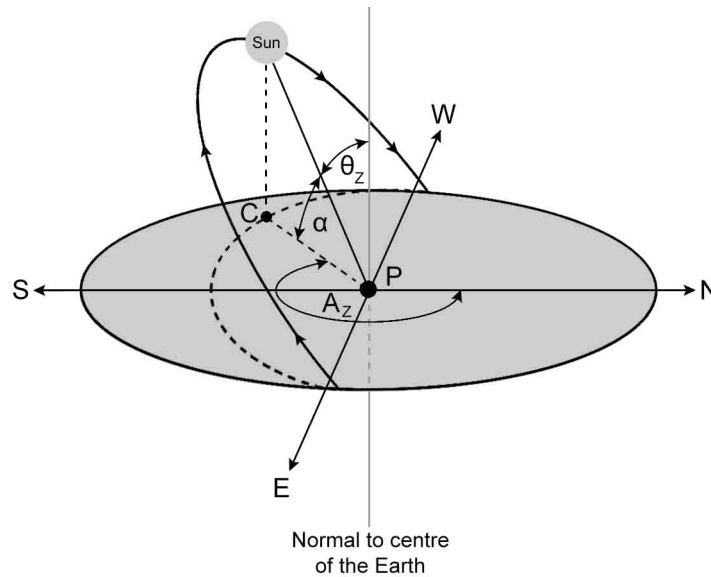




# The Sun and the Rotating Earth



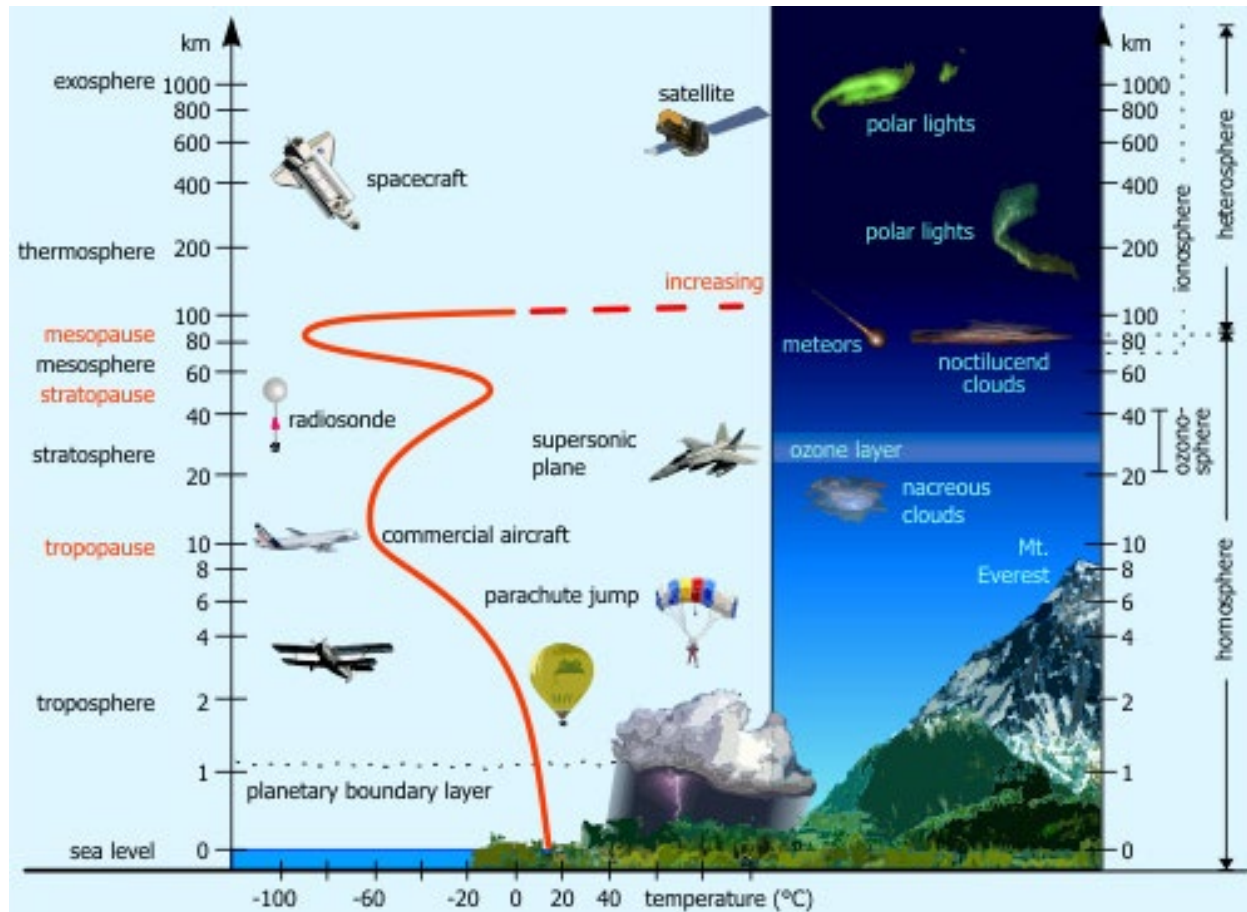
# Insolation on Flat Plane



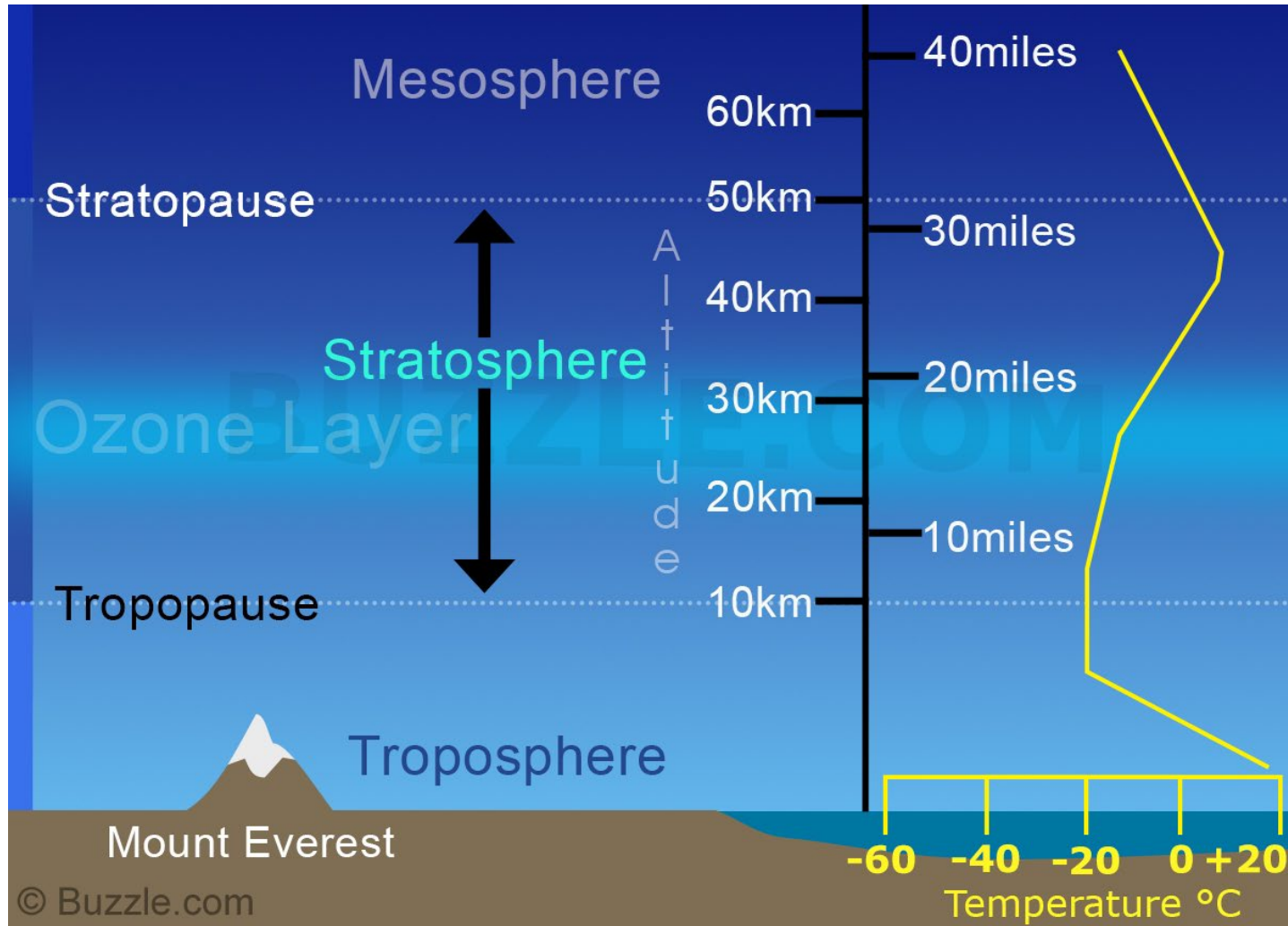
# Atmospheric Effects

$$I_{DN} = A \exp [-P/P_o \cdot B/\cos(\theta_z)]$$

$$P/P_o = \exp[-0.0000361 \cdot \text{Altitude(ft)}]$$

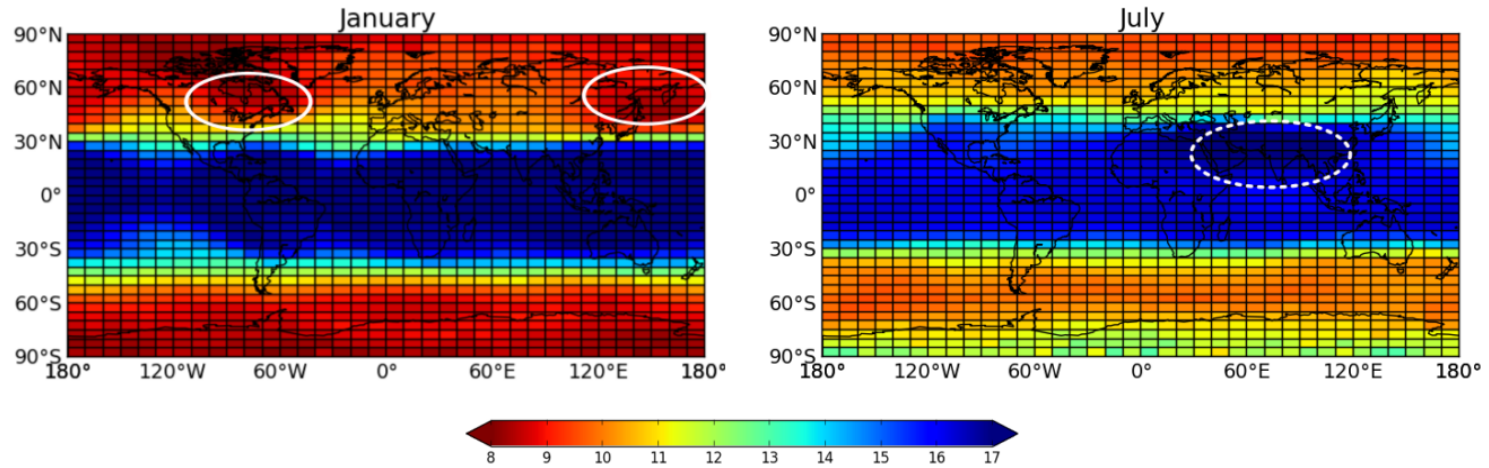


# Tropopause altitude is reduced in Northern Winter



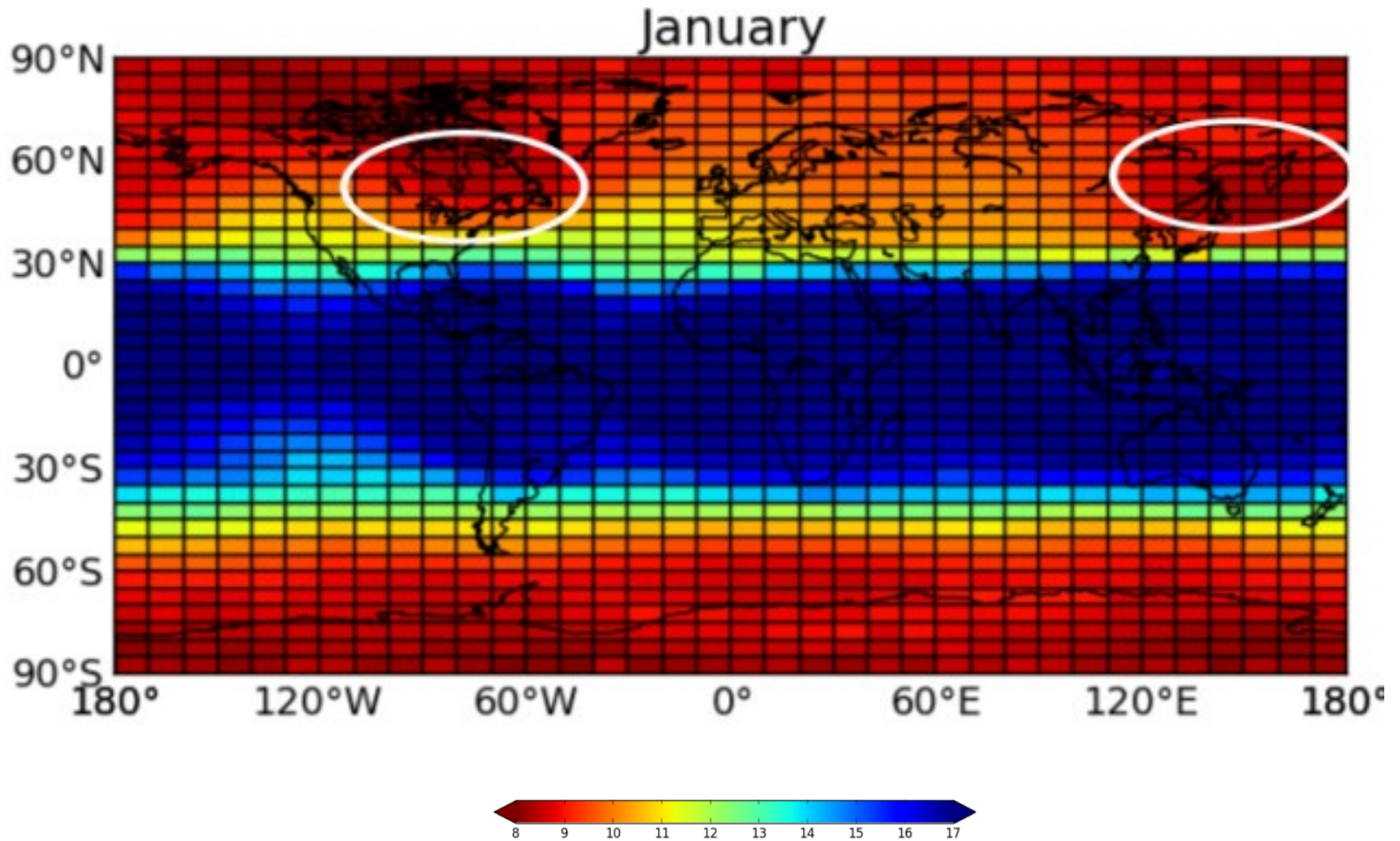
# Tropopause Altitude

Characteristics of tropopause parameters as observed with GPS radio occultation, Rieckh et al., 2014



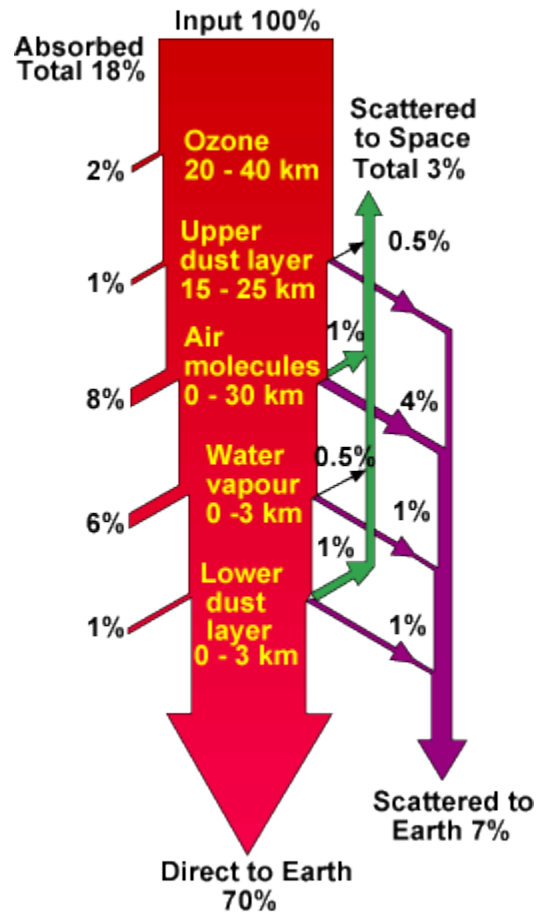
**Figure 6.** Mean altitude (km) of first tropopauses for January and July from 2007 to 2013. White circles denote areas of exceptionally low (solid) and high (dashed) tropopauses within the respective latitude band.





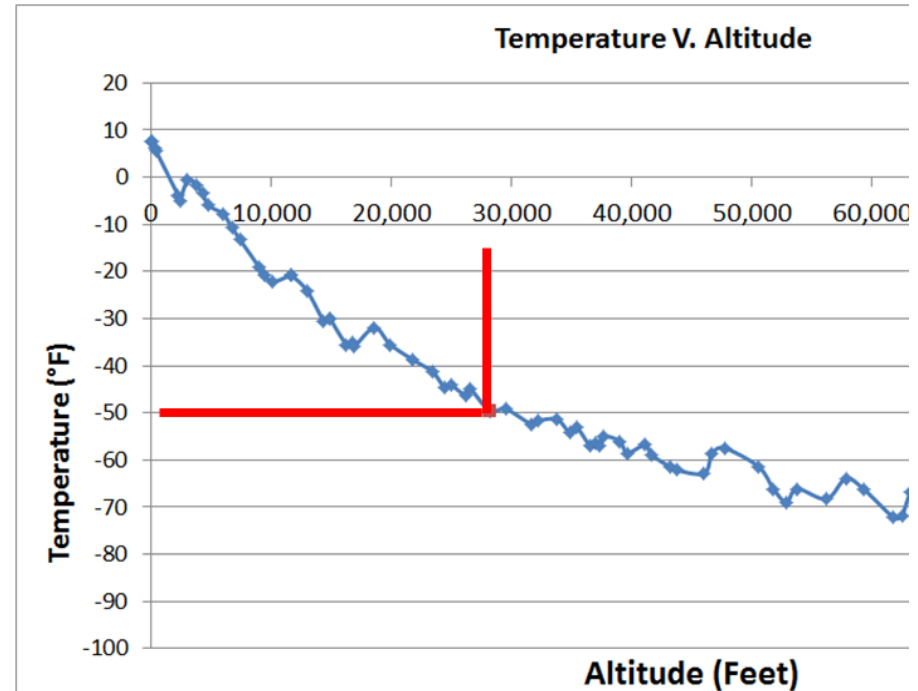
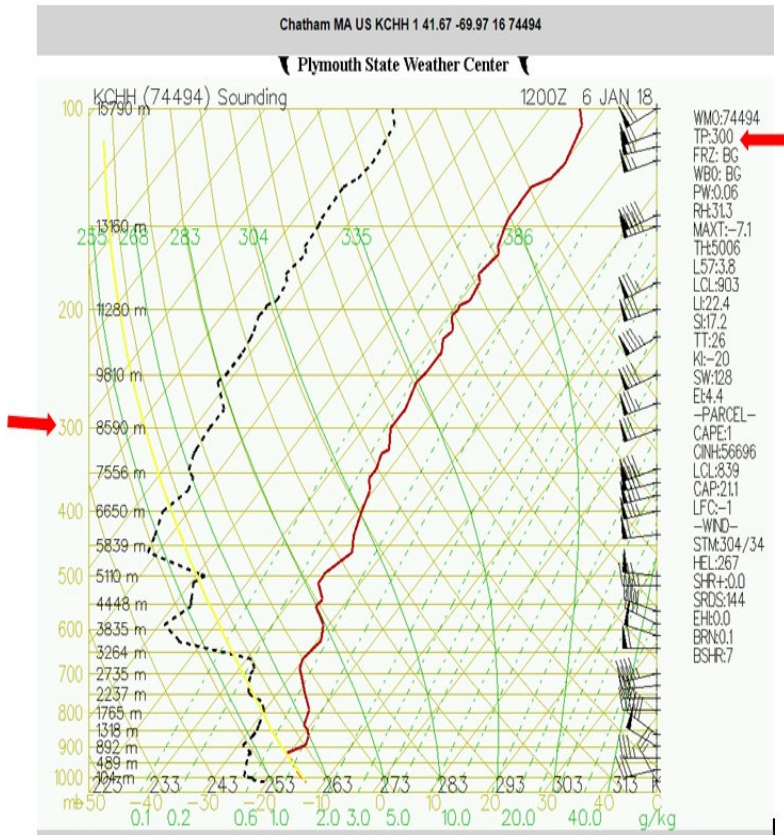
**Figure 6.** Mean altitude (km) of first tropopauses for January and July from 2007 to 2013. White circles denote areas of exceptionally low (solid) and high (dashed) tropopauses within the respective latitude band.

# Solar Insolation Atmospheric Filtering



# Troposphere, Tropopause: Elevation & Temperature Cold Winter Day (1/6/2018 – Chatham, MA)

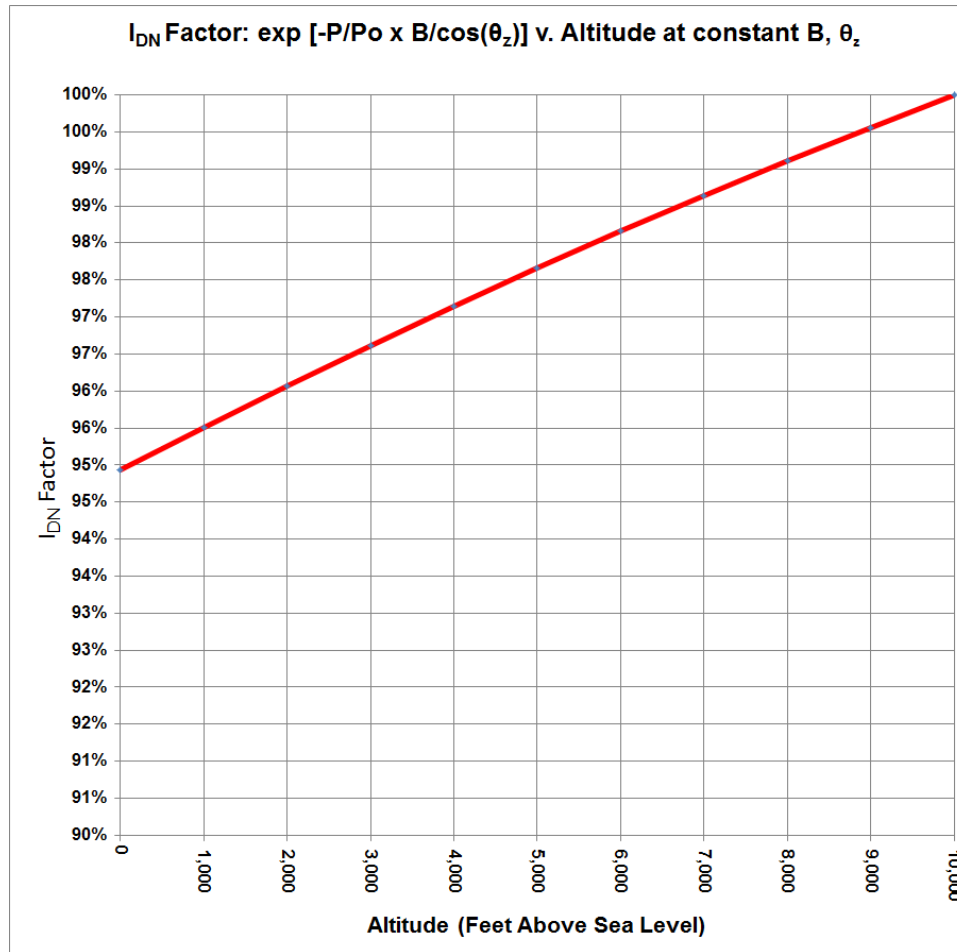
Tropopause (Indicated)



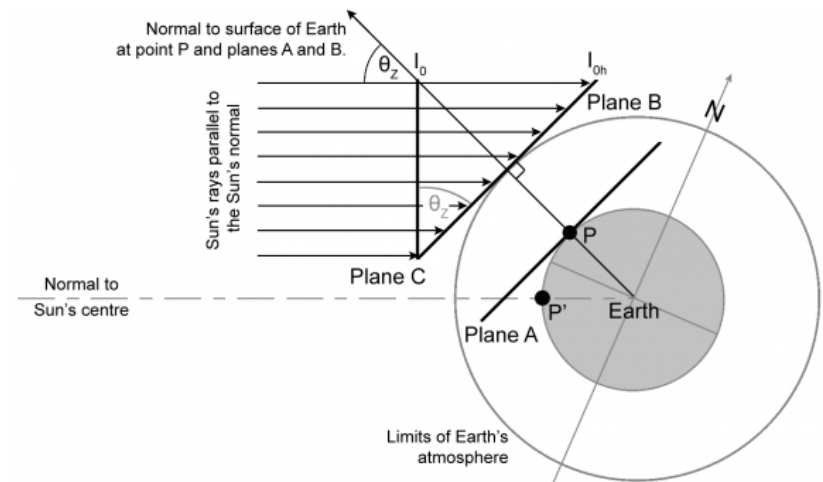
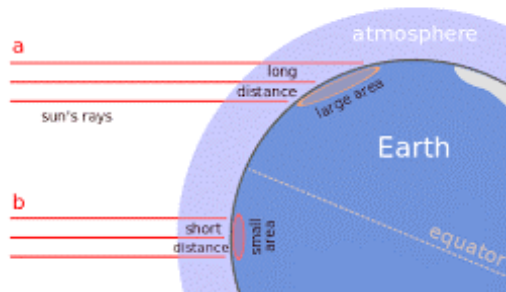
# IDN Factor v. Altitude

$$I_{DN} = A \text{ EXP } [-P/P_0 \times B/(\cos(\theta_z))]$$

$$P/P_0 = \text{EXP}[-0.0000361 \times \text{Altitude(ft)}]$$



# Atmospheric Mass & The Cosine Effect





# Air Mass (AM) Determination Using Cosine Law & Quadratic Formula substitution

Cosine Law:

$$(R+H)^2 = Z^2 + R^2 - 2 \cdot Z \cdot R \cdot \cos\{180 - \theta_z\}$$

Note:  $\cos\{180 - \theta_z\} = -\cos\{\theta_z\}$

$$0 = Z^2 + Z \cdot 2 \cdot R \cdot \cos\{\theta_z\} - (R+H)^2 + R^2$$

Solving for Z using Quadratic Formula:

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

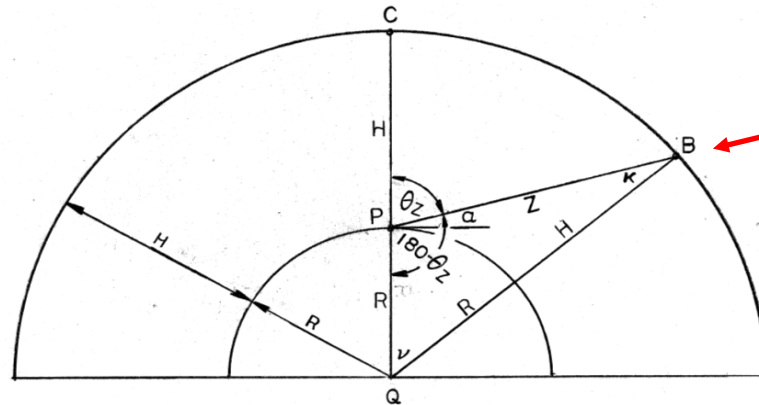
$$Z = \frac{-2 \cdot R \cdot \cos\{\theta_z\} + [(2 \cdot R \cdot \cos\{\theta_z\})^2 - 4(1)(-(R+H)^2 + R^2)]^{(1/2)}}{2}$$

Simplifying:

$$Z = -R \cdot \cos\{\theta_z\} + [(R \cdot \cos\{\theta_z\})^2 + ((2HR + H^2))]^{(1/2)}$$

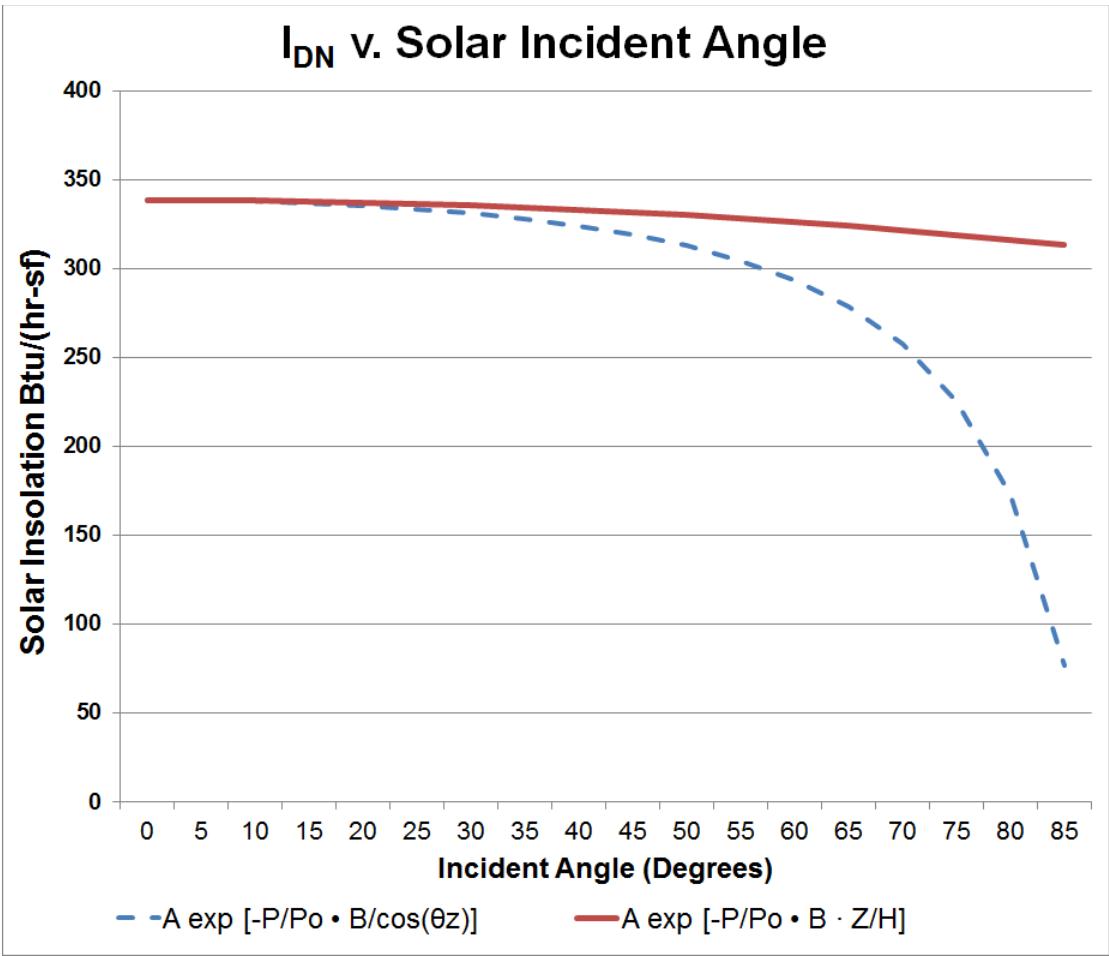
$$\text{Air mass} = \mathbf{AM} = \mathbf{Z/H}: Z/H = \frac{-R \cdot \cos\{\theta_z\} + [(R \cdot \cos\{\theta_z\})^2 + ((2HR + H^2))]^{(1/2)}}{H}$$

$$Z/H = [ (R/H \cdot \cos\{\theta_z\})^2 + 2R/H + 1 ]^{(1/2)} - R/H \cdot \cos\{\theta_z\}$$



Solar altitude @  $\alpha$

# Insolation at low $\alpha$ 50%-100% more



# Solar Equations Horizontal Surface

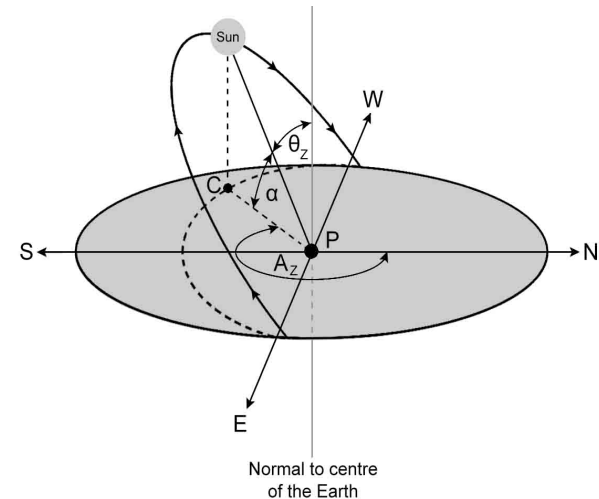
Solar Azimuth ( $\psi$ ) {degrees away from south}

$$\cos(\psi) = \frac{[\sin(\alpha) \sin(\Phi) - \sin(\delta)]}{[\cos(\alpha) \cos(\Phi)]}$$

Zenith Angle ( $\theta_z$ ): {Incident Angle}

$$\cos(\theta_z) = \sin(\alpha) = \cos(\Phi) \cos(\delta) \cos(\omega) + \sin(\Phi) \sin(\delta)$$

$$H_{\text{global}} = I_{\text{DN}} \sin(\alpha) + CI_{\text{DN}}$$



# Solar Equations on a Tilted Surface

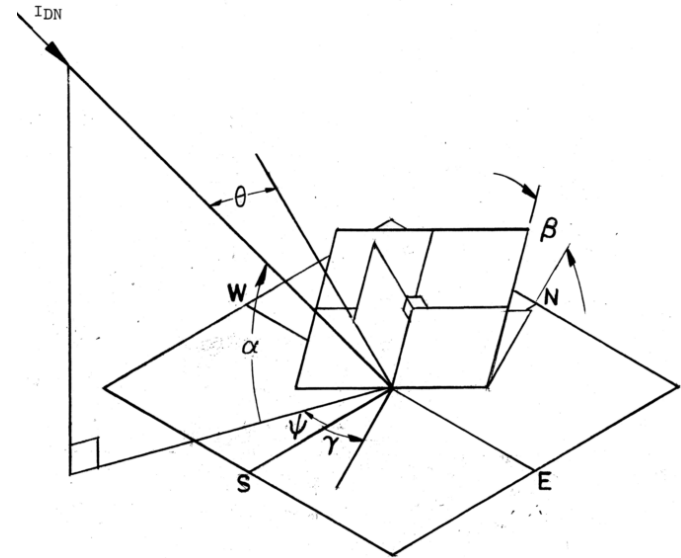
Tilted Surface [ $\gamma$ ] from south (True South Only):

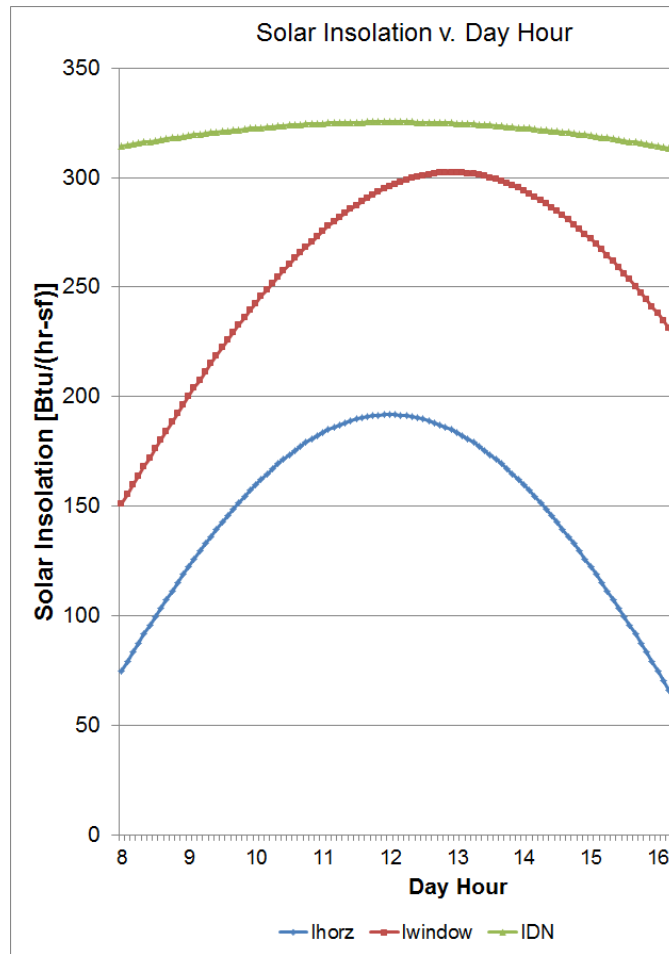
$$\cos(\theta) = \cos(\Phi - \beta)\cos(\delta)\cos(\omega) + \sin(\Phi - \beta)\sin(\delta)$$

~Sunrise, Sunset:  $\pm \cos(\omega_s) = -\tan(\Phi - \beta)\tan(\delta)$   
 $\pm 24/360 \times \arccos[-\tan(\Phi - \beta)\tan(\delta)]$

Tilted Surface [ $\gamma$ ] from south (+  $\gamma$  ~ West, -  $\gamma$  ~ East)

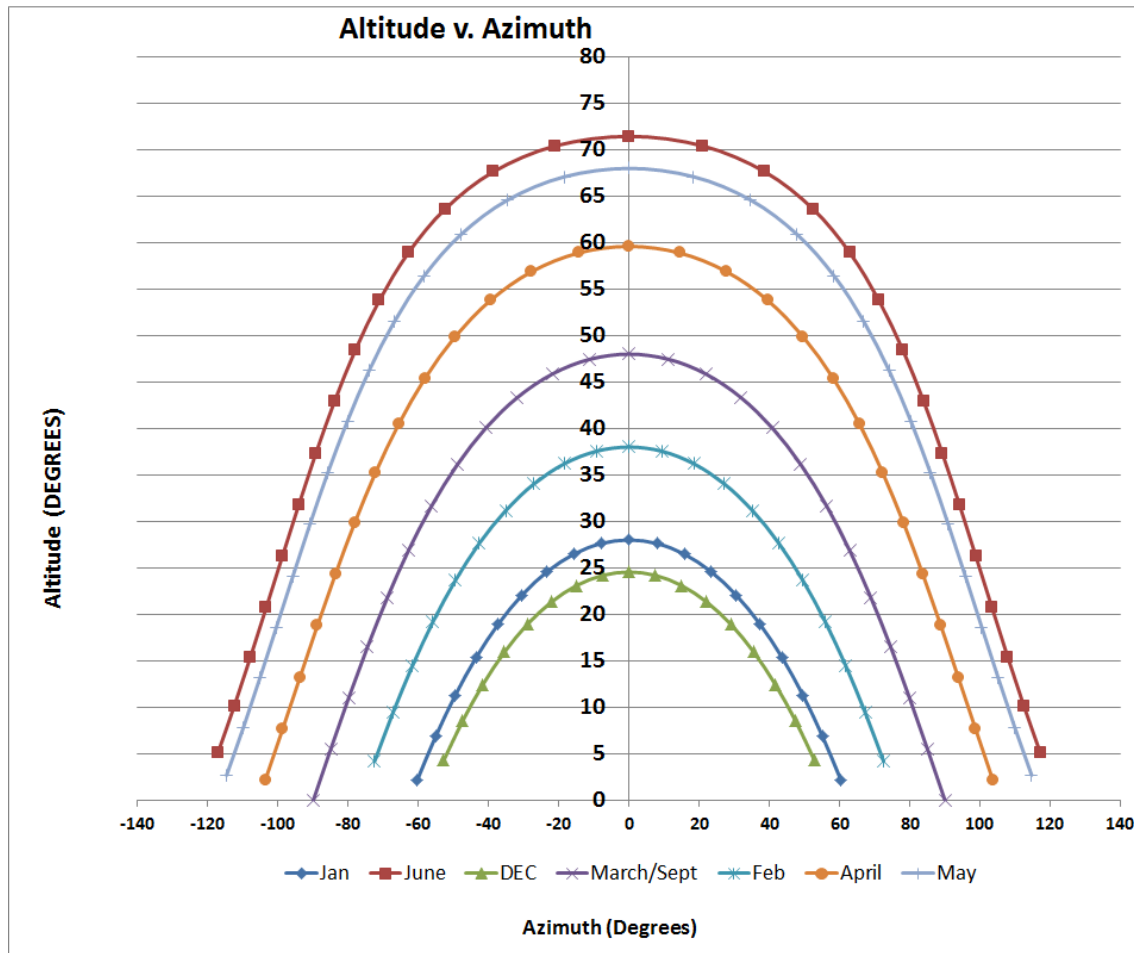
$$\cos(\theta) = \cos(\alpha)\cos(\psi - \gamma)\sin(\beta) + \sin(\alpha)\cos(\beta)$$



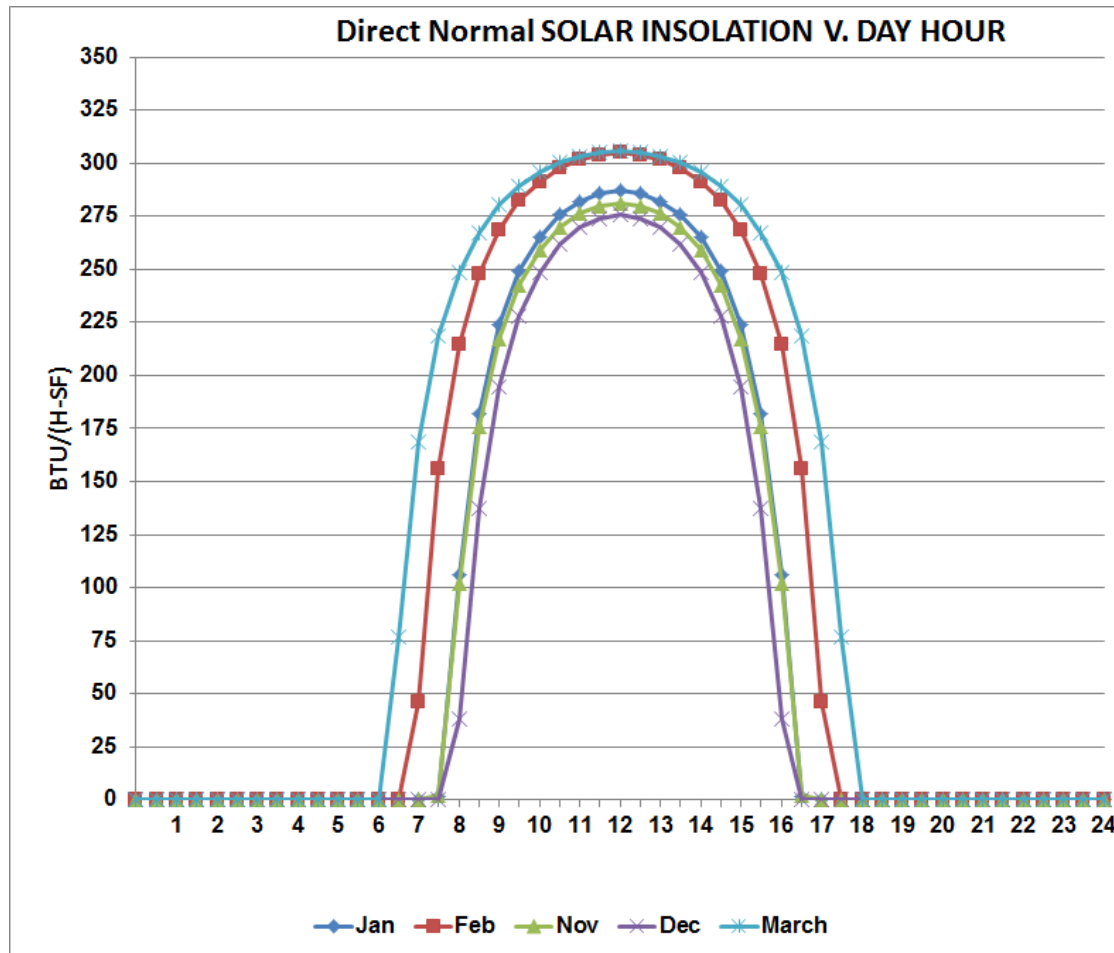




# @ 40° North Latitude



# @ 40° North Latitude

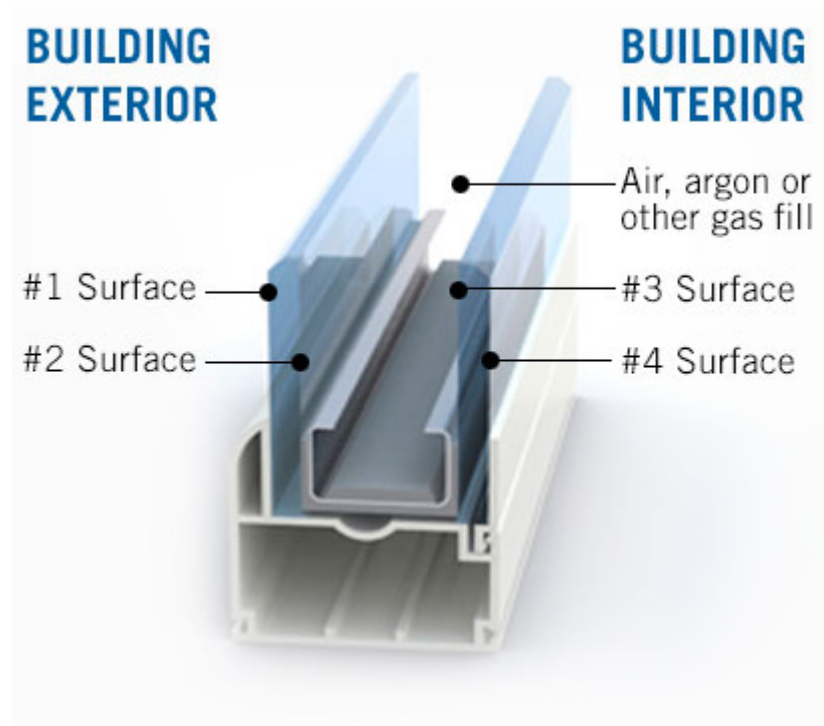


# Answer 1) Determination of solar insolation [“Solar\_Sample\_Calc\_Sensitivity.EXE”]:

	A	B	C		
	391.0	0.142	0.057		
Elev		0.0		FT (Above Sea Level)	
$\rho$ (Reflectivity):		0.00		[Unitless]	
$\Phi$		40.000		Deg	0.698 Rad
Day Number		355			
$\gamma$	..	10.0		Deg	0.175 Rad
$\beta$		90.00		Deg	1.571 Rad
Solar Time		14.000		hr	
$\omega$ [Hour angle]		30.00		Degrees	0.5236 Radians
$\delta$ [Declination Angle]		-23.429		Deg	-0.4089 Rad
COS( $\theta_z$ )		0.353			
( $\theta_z$ )		69.32		Degrees	1.210 Radians
$\alpha$ [Solar Altitude]		20.68		Degrees	0.361 Radians
Cos ( $\psi$ )		0.87151			
$\psi$		29.365		Degrees	0.5125 Radians
COS( $\theta$ )		0.88264177			
( $\theta$ )		28.04		Degrees	0.4893 Rad

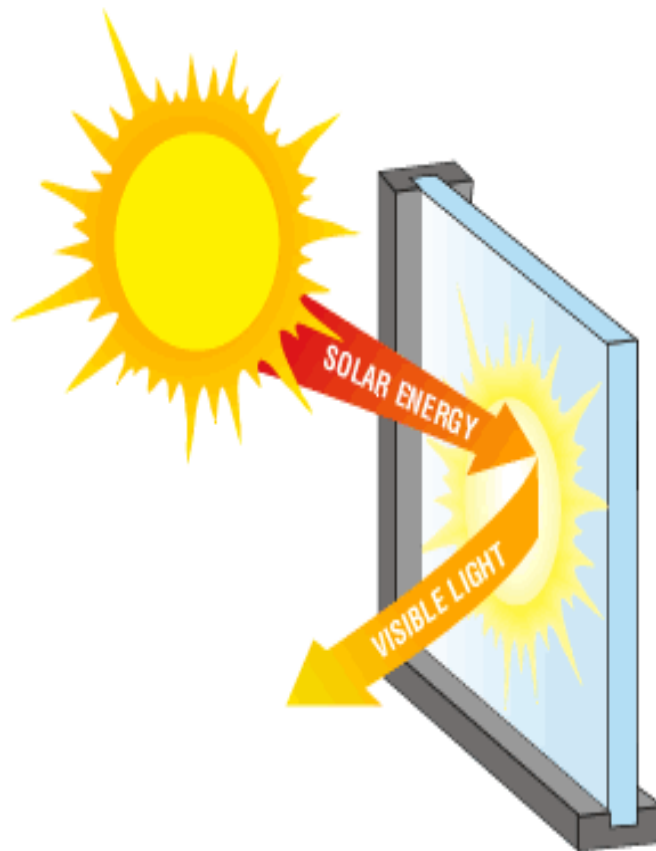
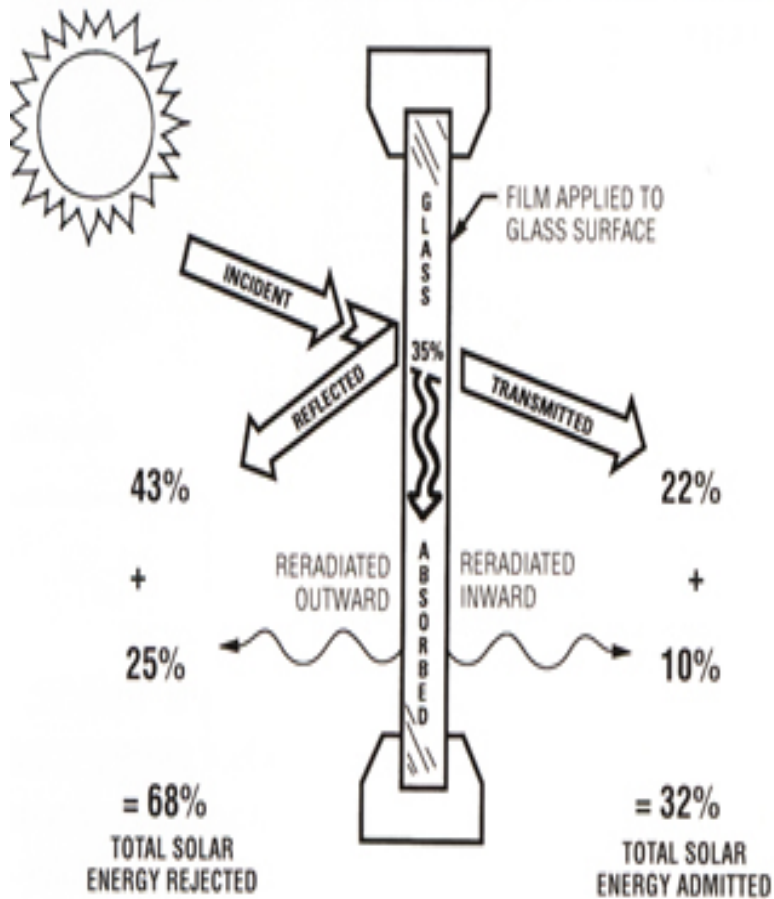
Temp:	30.0 °F		
P/Po	1.000		
AM (Exact)	1.054		
IDN	336.6 Btu/(hr-sf)		
Sky Refraction	2.9%		
Sky Refraction	9.6 Btu/(hr-sf)		
Ground Reflection	0.0%		
Ground Reflection	0.00 Btu/(hr-sf)		
Total Diff	9.59 Btu/(hr-sf)		
Direct	297.1 Btu/(hr-sf)		
<b>Total:</b>	<b>306.7 Btu/(hr-sf)</b>		
	1 Btu/(hr-sf) =	3.15464	Watt/m <sup>2</sup>
<b>Total:</b>	<b>967.6</b>	<b>Watt/m<sup>2</sup></b>	

# Typical Insulated Glass Unit (IGU)



# Window Performance

*Glass with Film Applied to its Interior Surface*



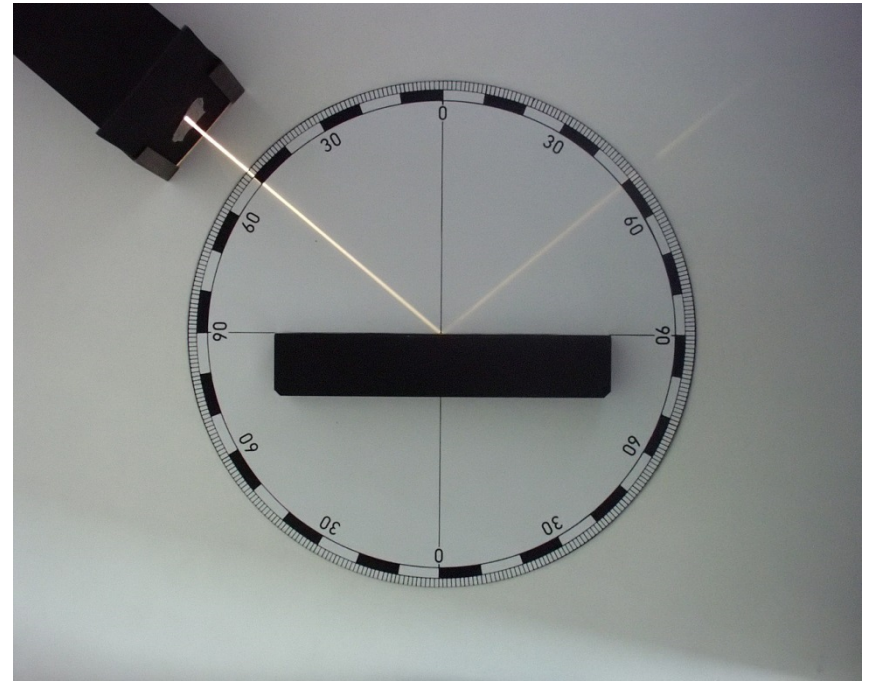


# Window Reflected Sunlight

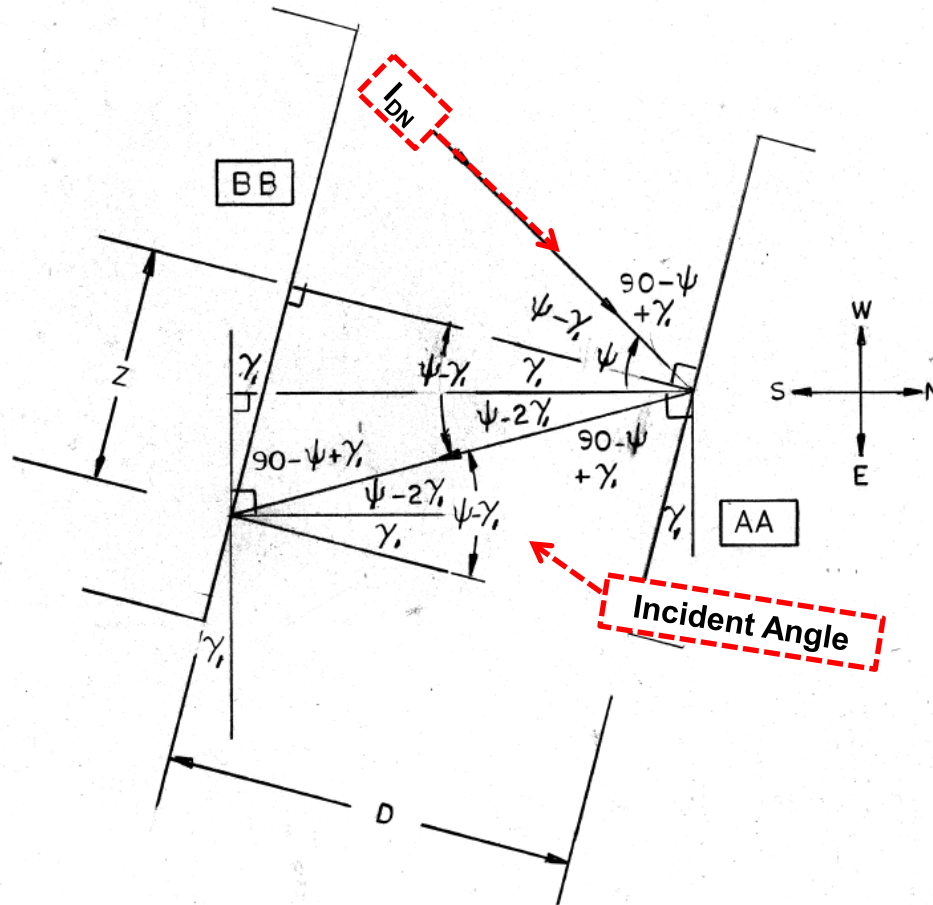
Solar Glare Reflection from Window



Angle of Reflection = Angle of Incidence



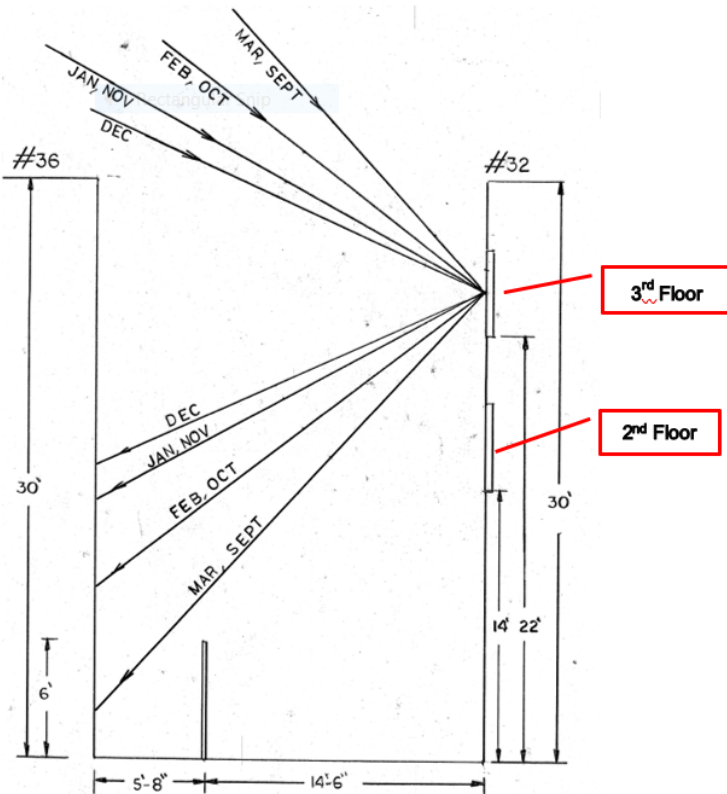
# Aerial View



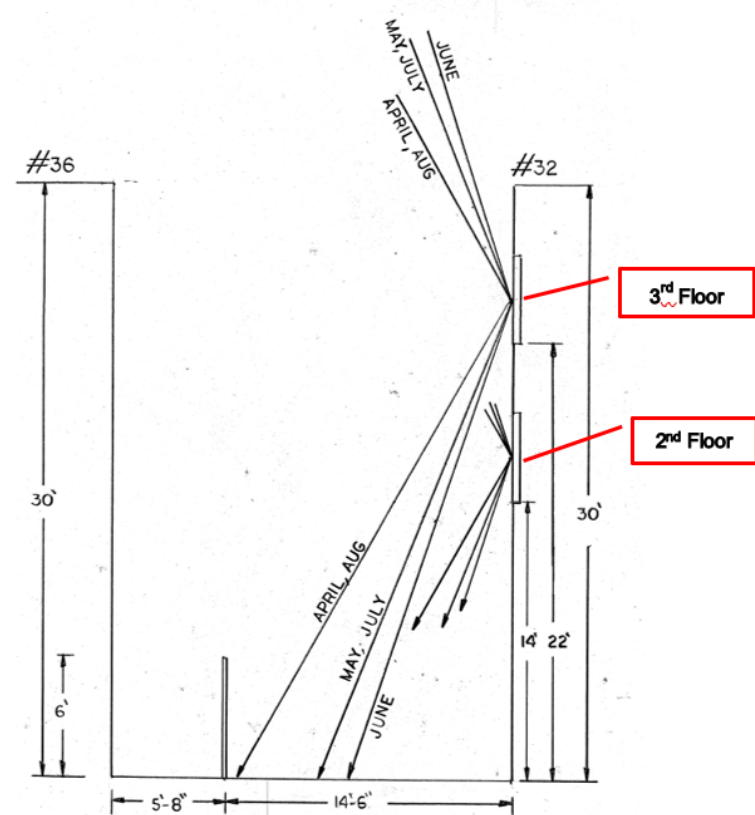


# [Angle of Reflection = Angle of Inflection]

## September-March



## April-August



For Sun Reflecting onto the Ground (Isometric View)

$$I_{\text{Reflect}} = I_{\text{DN}} \times (\text{Concentrating Factor})$$

**For sunlight reflection onto the ground:**

$$JJ \cdot \cos(\psi - \gamma_1) < D$$

$$\tan(\alpha) = H_T / JJ; \quad JJ = H_T / \tan(\alpha)$$

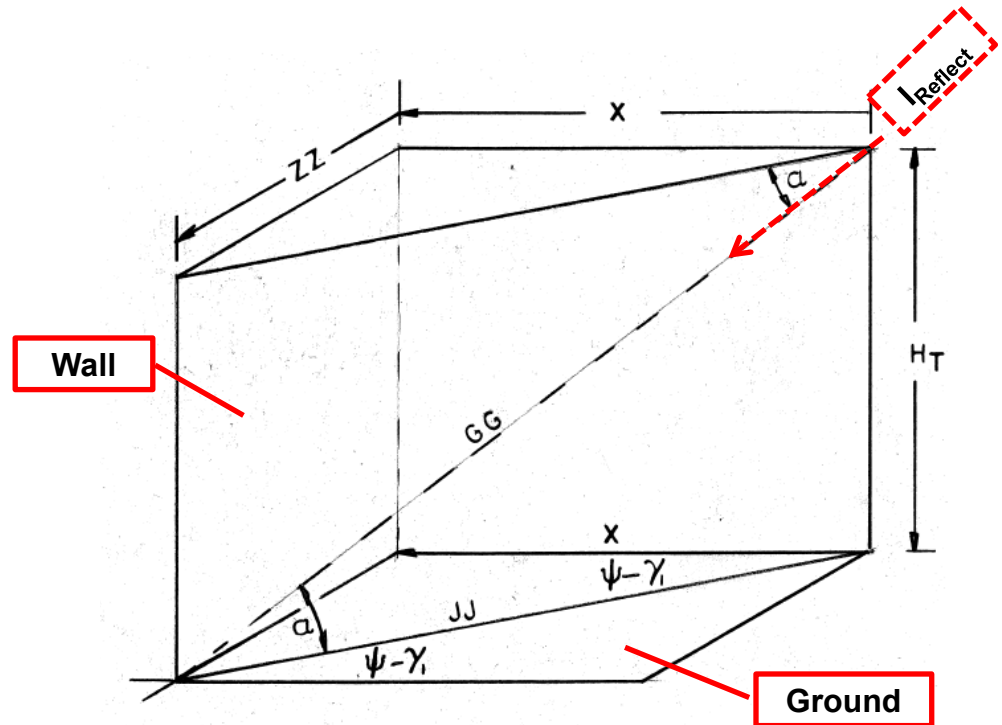
$$ZZ = JJ \cdot \sin(\psi - \gamma_1)$$

$$X = JJ \cdot \cos(\psi - \gamma_1)$$

$$GG^2 = H_T^2 + JJ^2$$

**For sunlight reflection onto the wall:**

$$JJ \cdot \cos(\psi - \gamma_1) \geq D$$



## For Sun Reflecting onto the Wall (Isometric View)

$$I_{\text{Reflect}} = I_{\text{DN}} \times (\text{Concentrating Factor})$$

**For Sunlight reflecting on the wall:**

$$J \cdot \cos(\psi - \gamma_1) \geq D$$

$$\tan(\psi - \gamma_1) = Z/D; \quad Z = D \cdot \tan(\psi - \gamma_1)$$

$$J^2 = Z^2 + D^2$$

$$\tan(\alpha) = Y/J; \quad Y = J \cdot \tan(\alpha)$$

$$\cos(\psi - \gamma_1) = D/J$$

$$G^2 = Y^2 + J^2$$

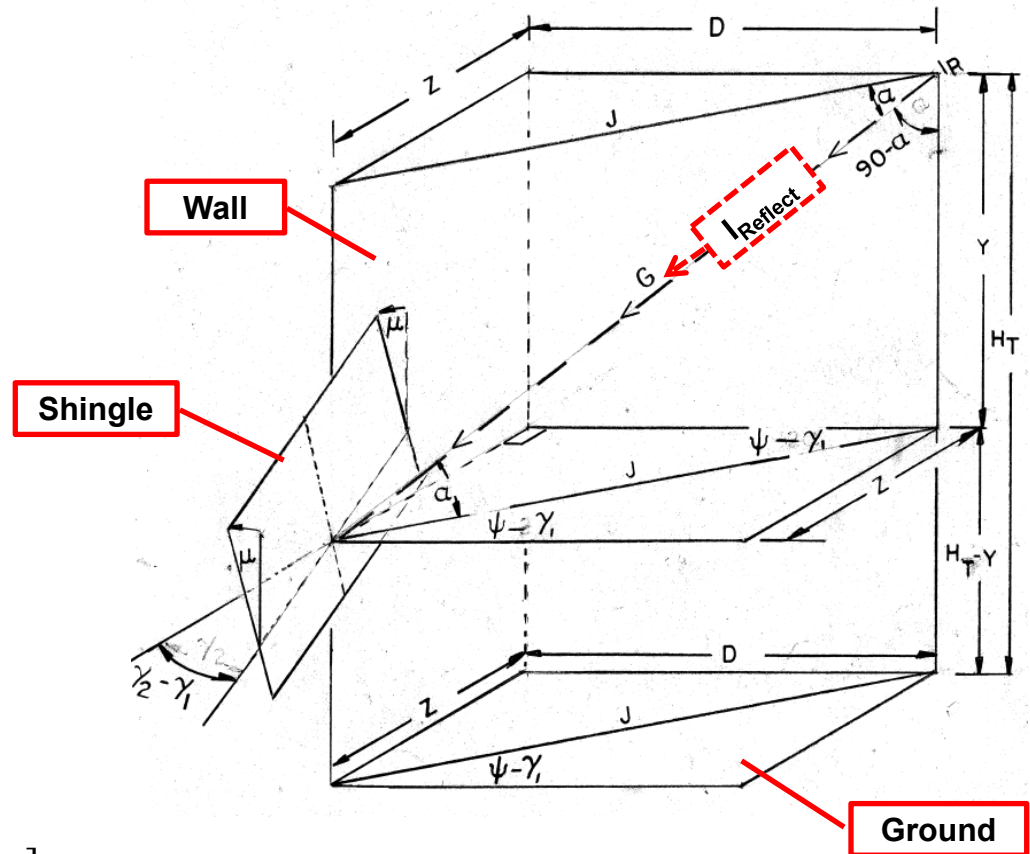
$$\cos(\alpha) = J/G$$

$$I_{\text{shingle}} = I_{\text{R}} \cdot \cos(\alpha - \mu) \cdot \cos(\psi - \gamma_1 - \{\gamma_2 - \gamma_1\})$$

Incident Angle Factor =

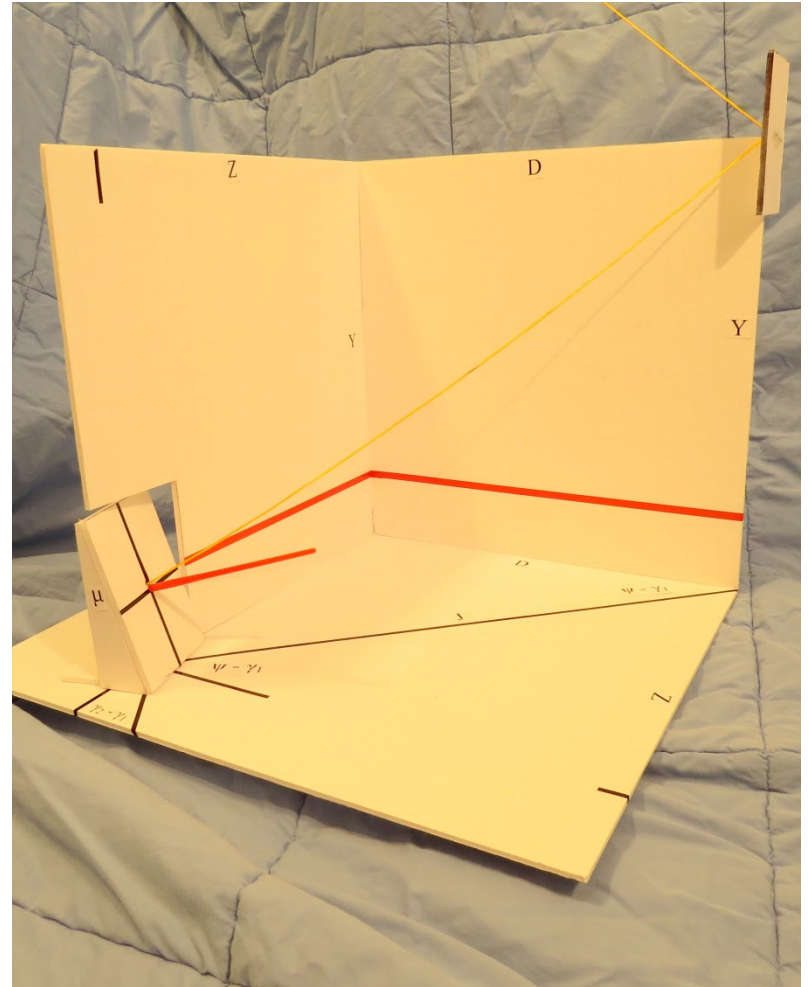
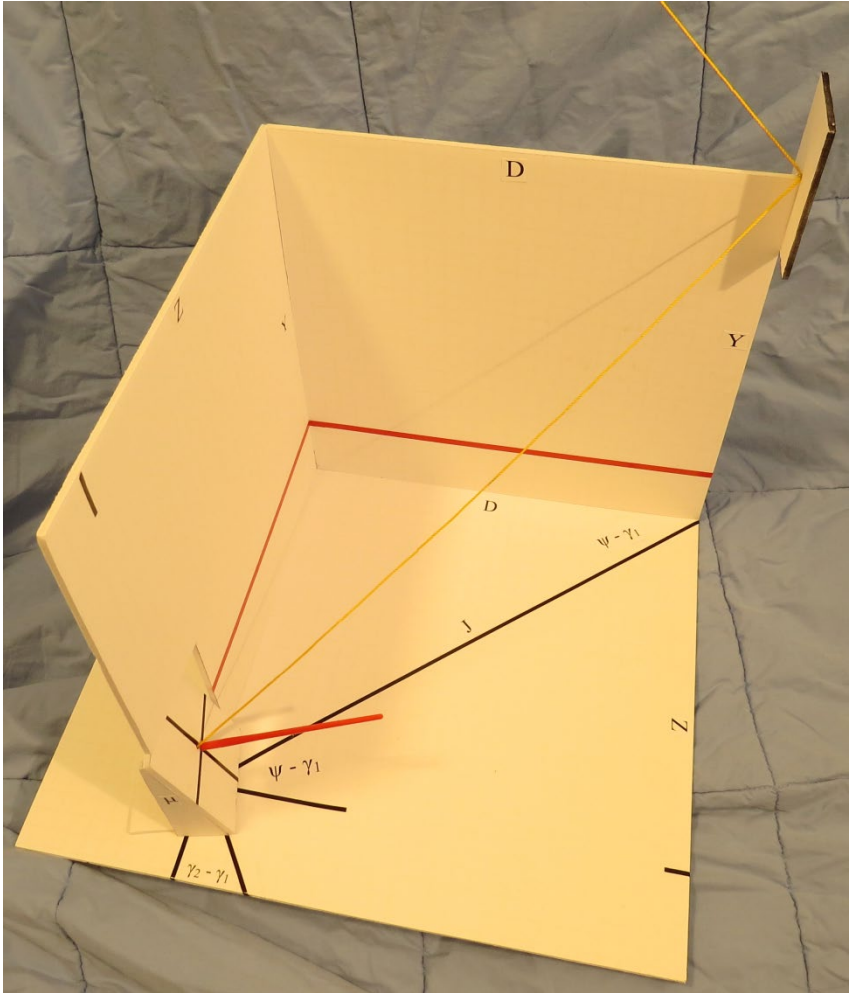
$$[\cos(\alpha - \mu) \cdot \cos(\psi - \gamma_1 - \{\gamma_2 - \gamma_1\})]$$

$$\text{Incident Angle} = A \cos[\text{Incident Angle Factor}]$$





# 3-D Model





# Excel Analysis

Sun Factor	7.0		
<b>IR=</b>	<b>2,147.12 Btu/(hr-sf)</b>		
<b>Tan(<math>\psi - \gamma</math>) = Z/D; Z=D•Tan(<math>\psi - \gamma</math>)</b>			
D=	30 Ft		
$\psi$	29.365 Degrees	0.513 Radians	
$\gamma$	10.00 Deg	0.175 Rad	
Z	10.54 Ft		
<b><math>J^2 = Z^2 + D^2</math></b>			
J =	31.8 Ft		
<b>Tan(<math>\alpha</math>) = Y/J; Y= J•Tan(<math>\alpha</math>)</b>			
<b><math>\alpha</math> =</b>	<b>20.68 Degrees</b>	<b>0.36 Radians</b>	
<b>Y=</b>	<b>12.00 Ft</b>		
<b>Cos(<math>\psi - 2 \gamma</math>) = D/J</b>			
<b><math>G^2 = Y^2 + J^2</math></b>			
G=	33.99 Ft		
	0.93557071		
	0.93557071		
<b>Cos(<math>\alpha</math>) = J/G</b>			

<b>Ishingle = IR•Cos(<math>\alpha - \mu</math>) •Cos(<math>\psi - 2\gamma_1 - \{\gamma_2 - \gamma_1\}</math>)</b>			
$\mu$ =	7.0 Degrees	0.122 Radians	
$\gamma_2$ =	10.0 Degrees	0.175 Radians	
$\gamma_1$ =	10.0 Degrees	0.175 Radians	
$\gamma_2 - \gamma_1$	0.0 Degrees	0.000 Radians	
<b>Incident Angle Factor = [Cos(<math>\alpha - \mu</math>) •Cos(<math>\psi - 2\gamma_1 - \{\gamma_2 - \gamma_1\}</math>)]</b>			
<b>Incident Angle Factor =</b>	<b>0.95868</b>		
<b>Incident Angle = ACOS[Incident Angle Factor]</b>			
<b>Incident Angle =</b>	0.288457589 Radians	16.527 Degrees	
<b>Ishingle = IR•Cos(Incident Angle)</b>			
<b>Ishingle =</b>	<b>2,058.4 Btu/(hr-sf)</b>		

# Sensitivity Analysis Using Analytic Models

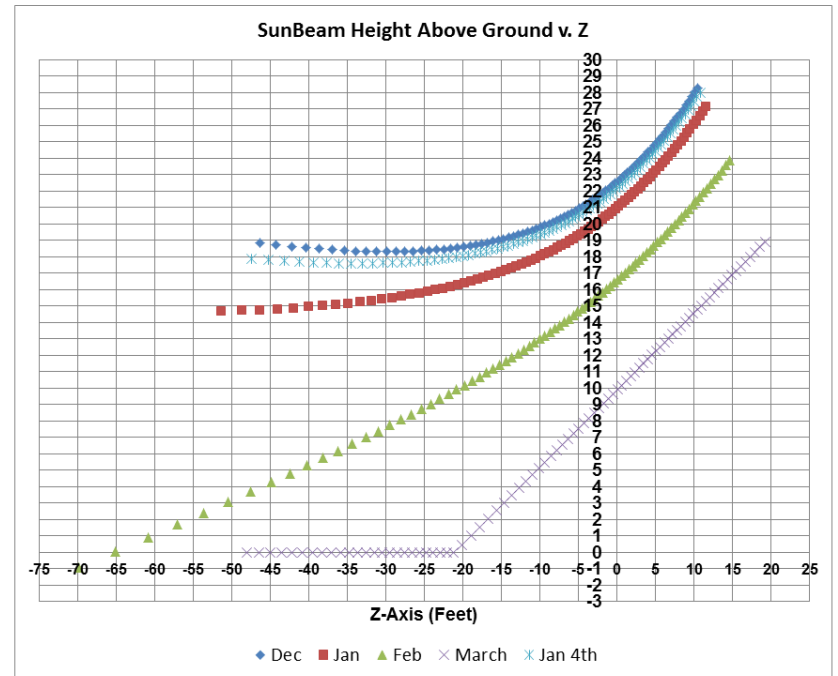
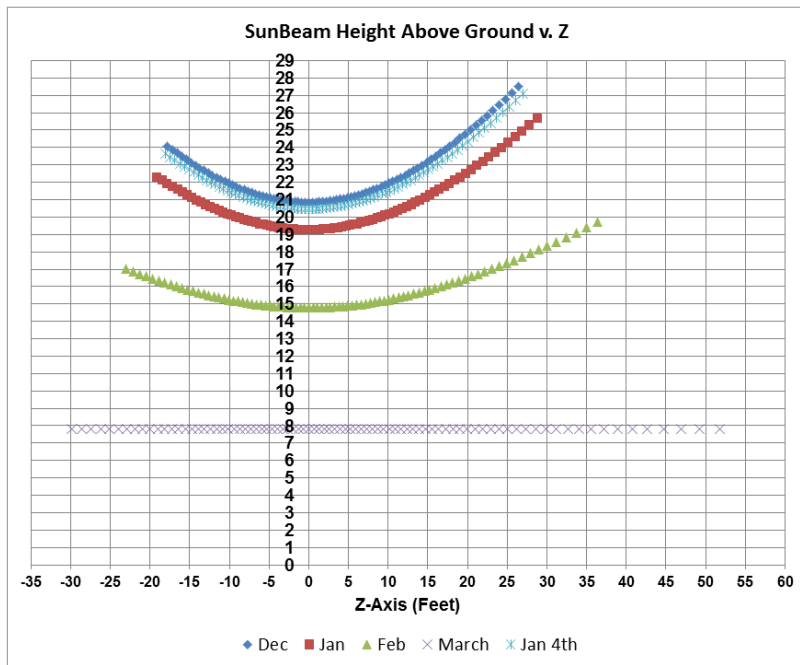
# Sunbeam Height Above Ground v. Z [ $\phi=42^\circ$ ]

$$\gamma = 0^\circ$$

$$\gamma = 25^\circ$$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma$ = 0.0 Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.

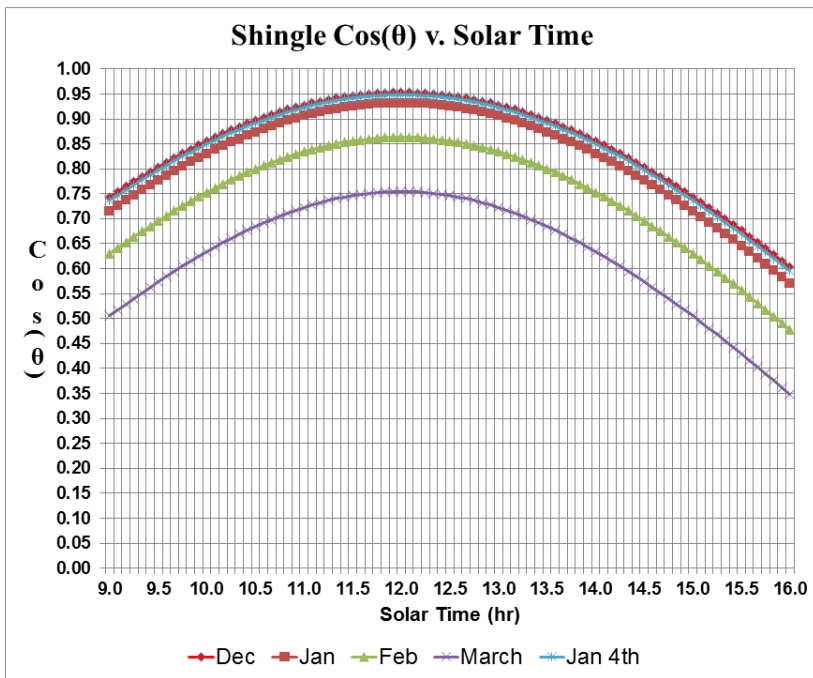
D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma$ = 25.0 Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.



# Shingle $\text{Cos}(\theta)$ v. Solar Time [ $\phi=42^\circ$ ]

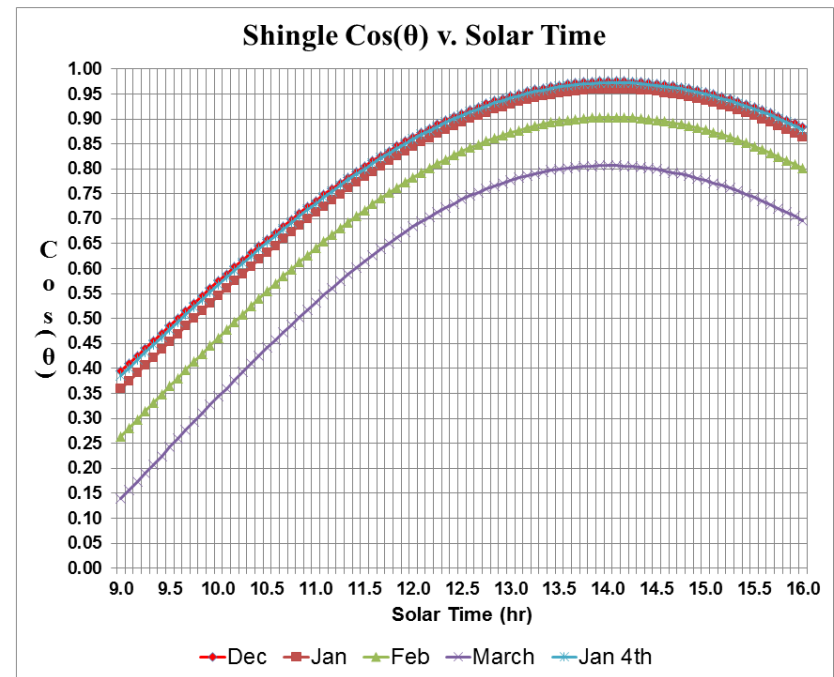
$$\gamma = 0^\circ$$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 0.0$  Degrees  
 Time Start 9.0 hr.      Time End: 16.0 hr.



$$\gamma = 25^\circ$$

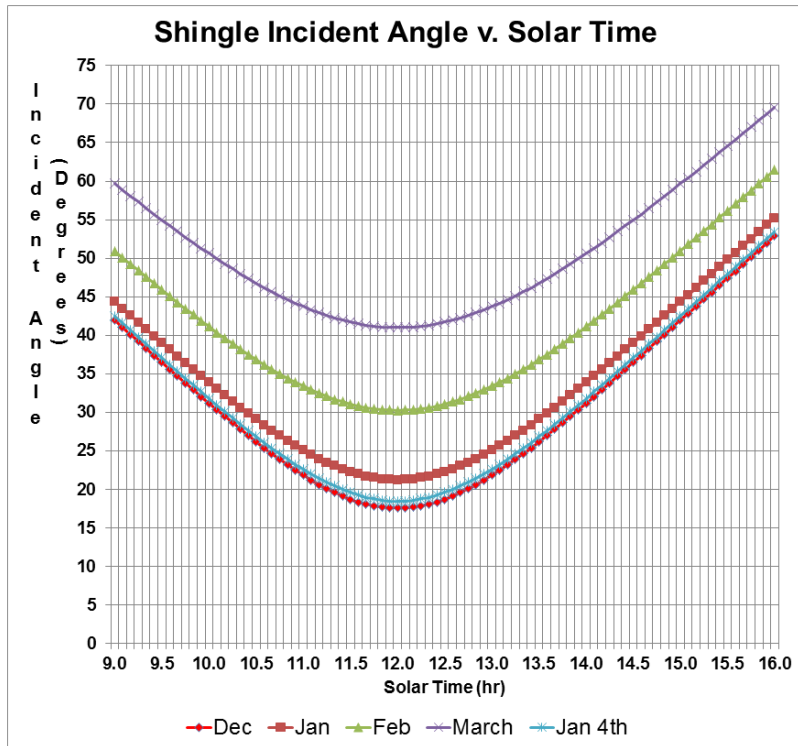
D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 25.0$  Degrees  
 Time Start 9.0 hr.      Time End: 16.0 hr.



# Shingle Incident Angle v. Solar Time [ $\phi=42^\circ$ ]

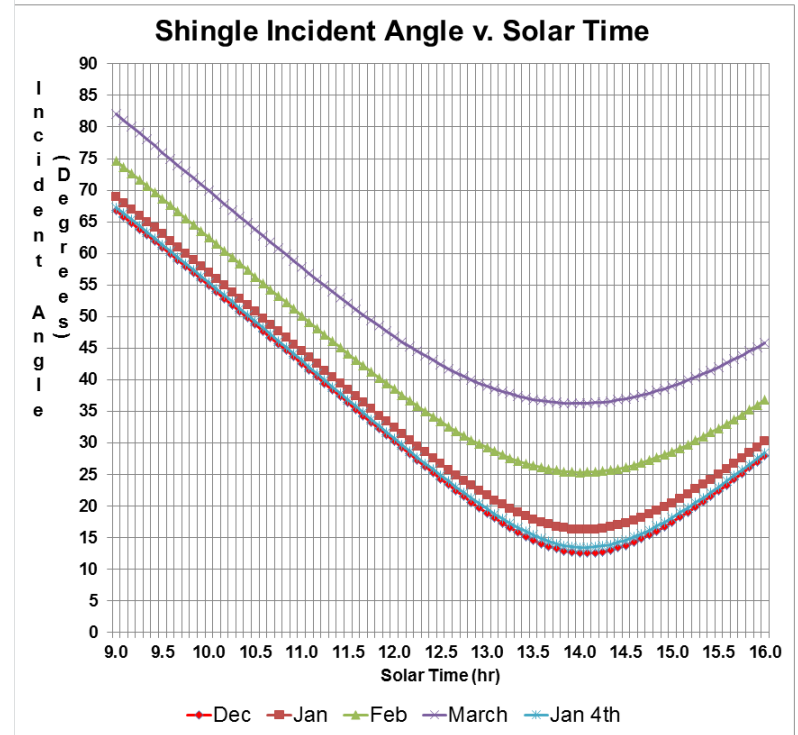
$$\gamma = 0^\circ$$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 0.0$  Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.

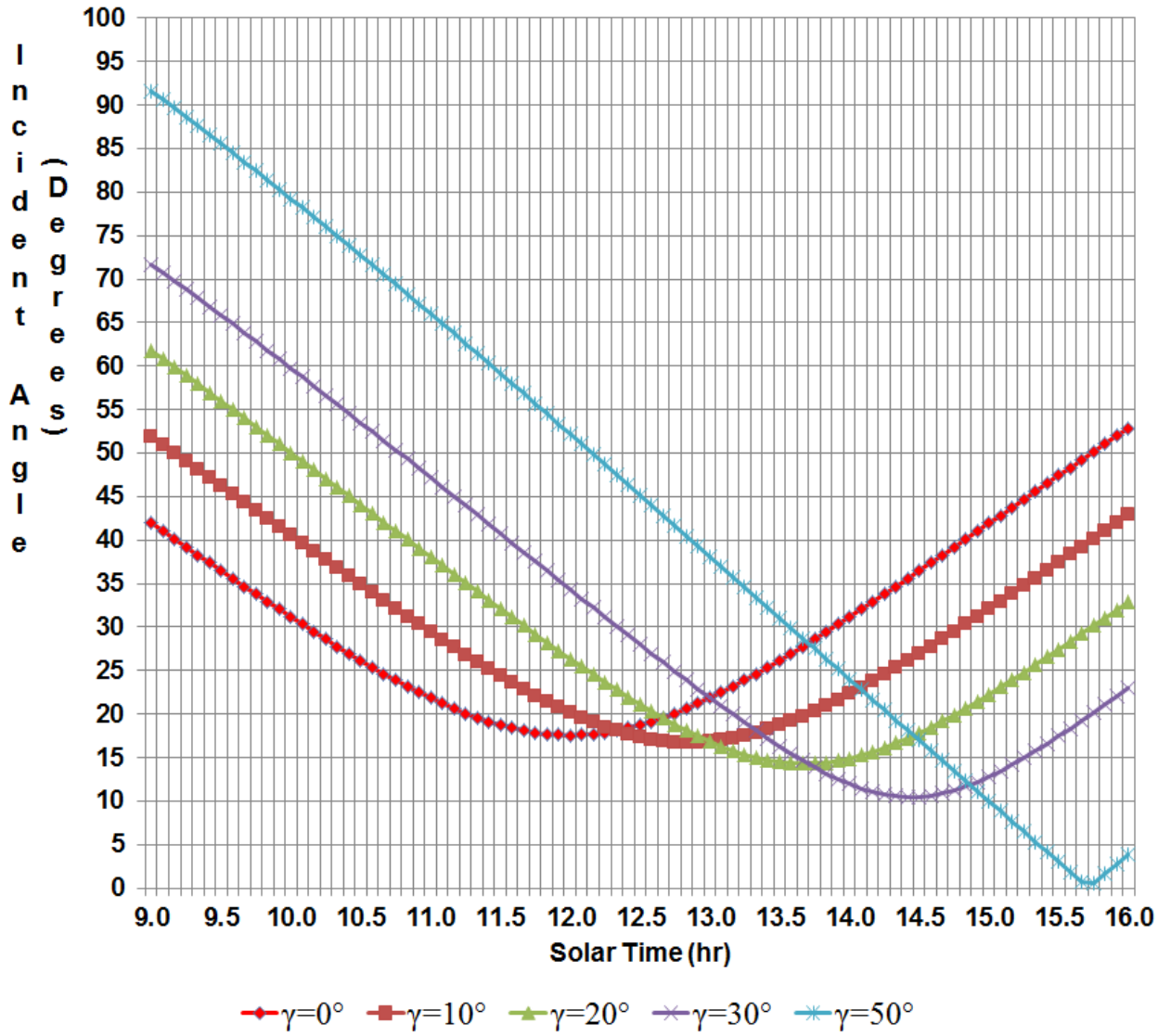


$$\gamma = 25^\circ$$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 25.0$  Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.



# Shingle Incident Angle v. Solar Time



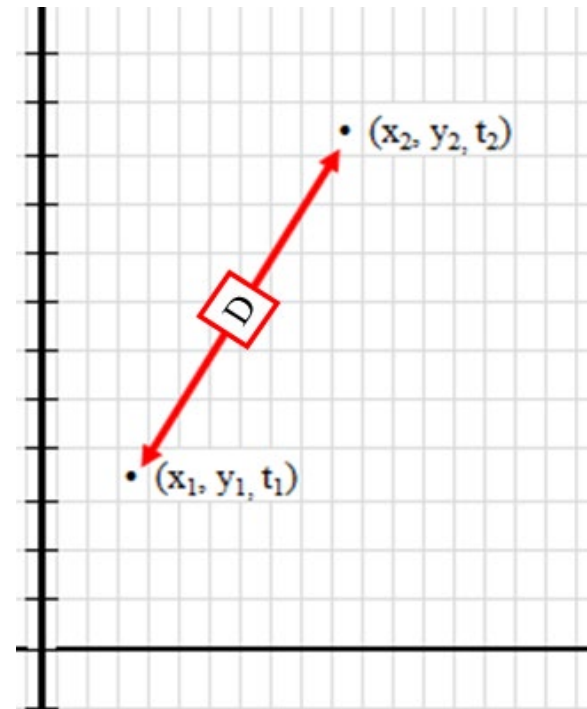
# Sunbeam Linear Velocity

## [Velocity Between Two Points]

The Euclidean distance between two points of the plane with Cartesian coordinates:

$$D = [(x_2 - x_1)^2 + (y_2 - y_1)^2]^{(1/2)}$$

$$\text{Velocity} = D / (t_2 - t_1)$$

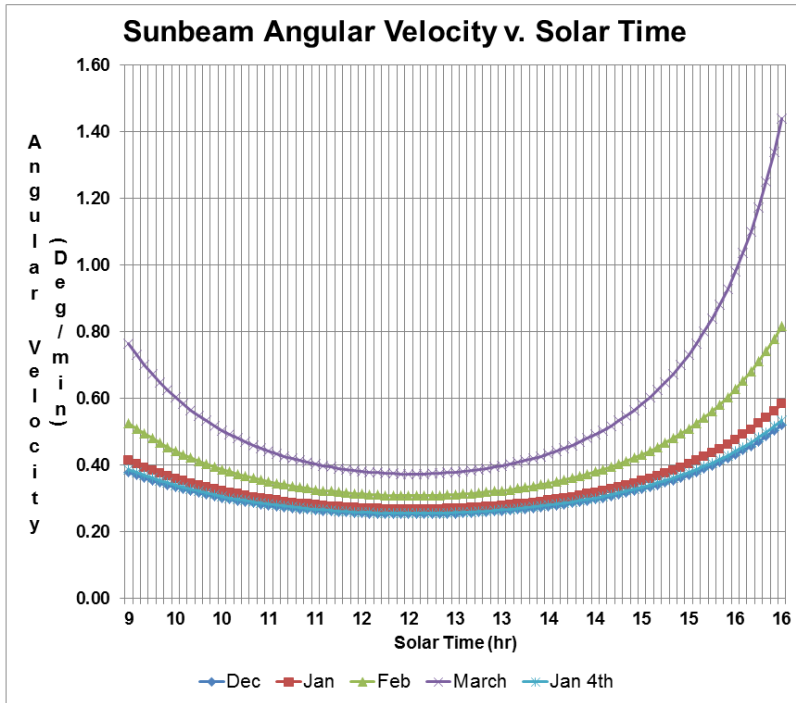




# Sunbeam Angular Velocity v. Solar Time [ $\phi=42^\circ$ ]

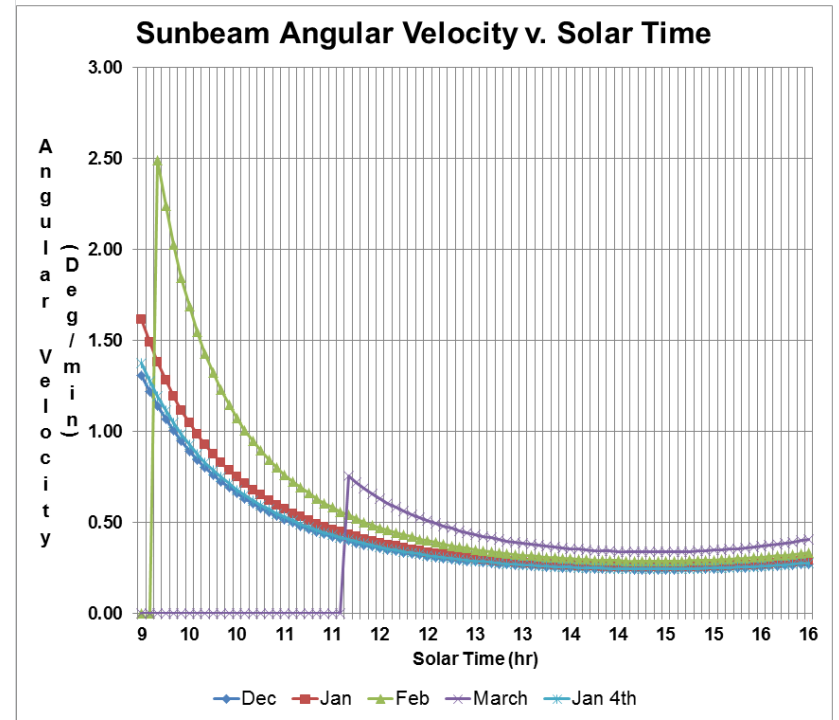
$$\gamma = 0^\circ$$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma$ = 0 Degrees  
 Time Start 9.0 hr.      Time End: 16.0 hr.



$$\gamma = 25^\circ$$

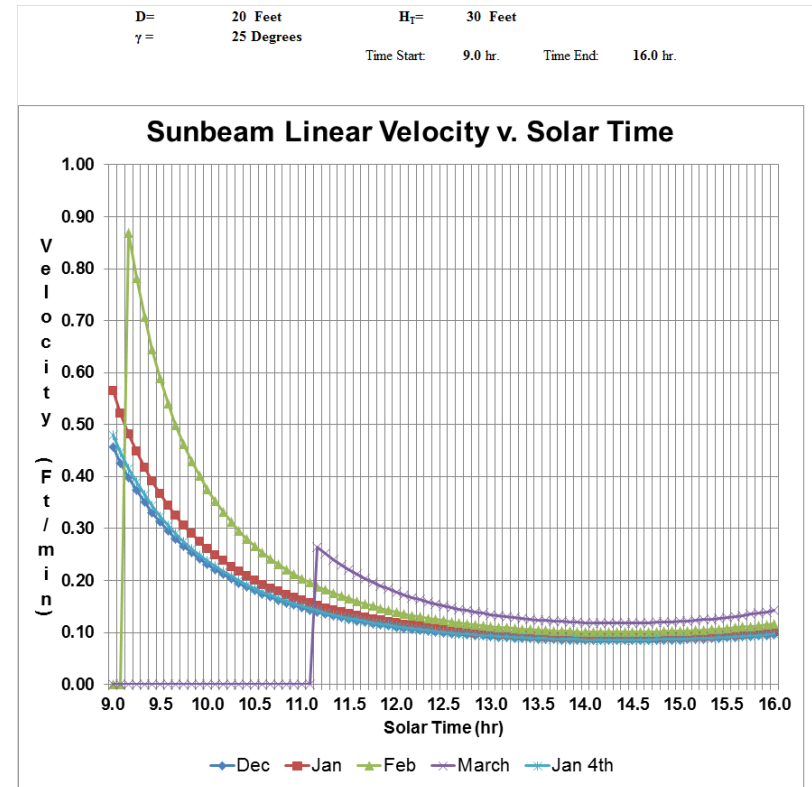
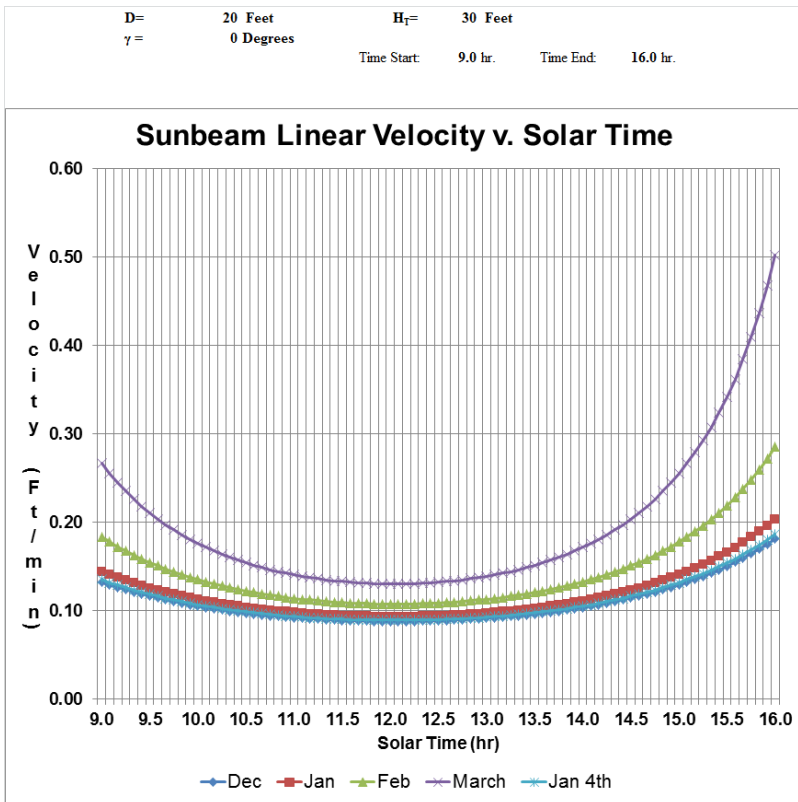
D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma$ = 25 Degrees  
 Time Start 9.0 hr.      Time End: 16.0 hr.



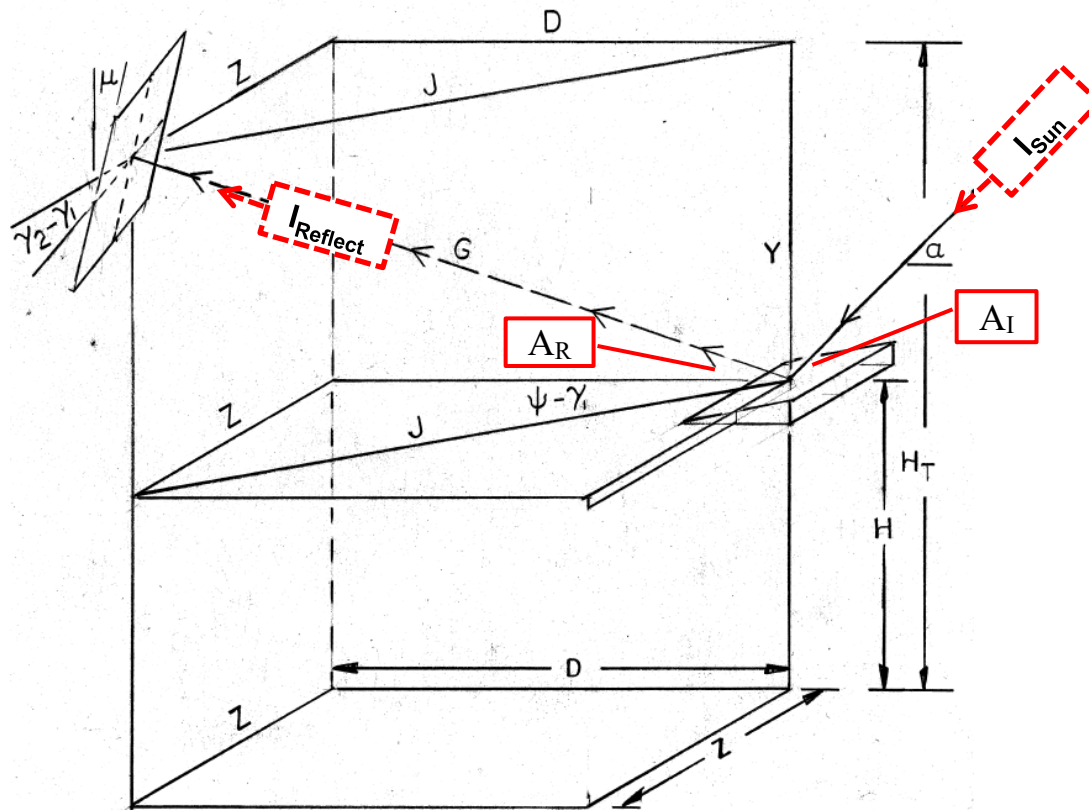
# Sunbeam Linear Velocity v. Solar Time [ $\phi=42^\circ$ ]

$$\gamma = 0^\circ$$

$$\gamma = 25^\circ$$

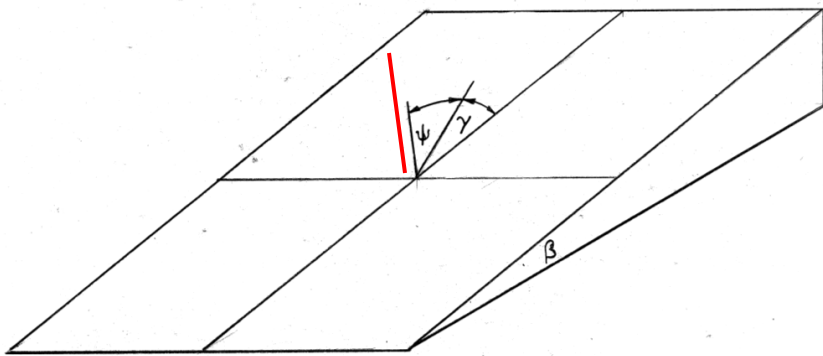


# Reflection from Inclined Glass Surface

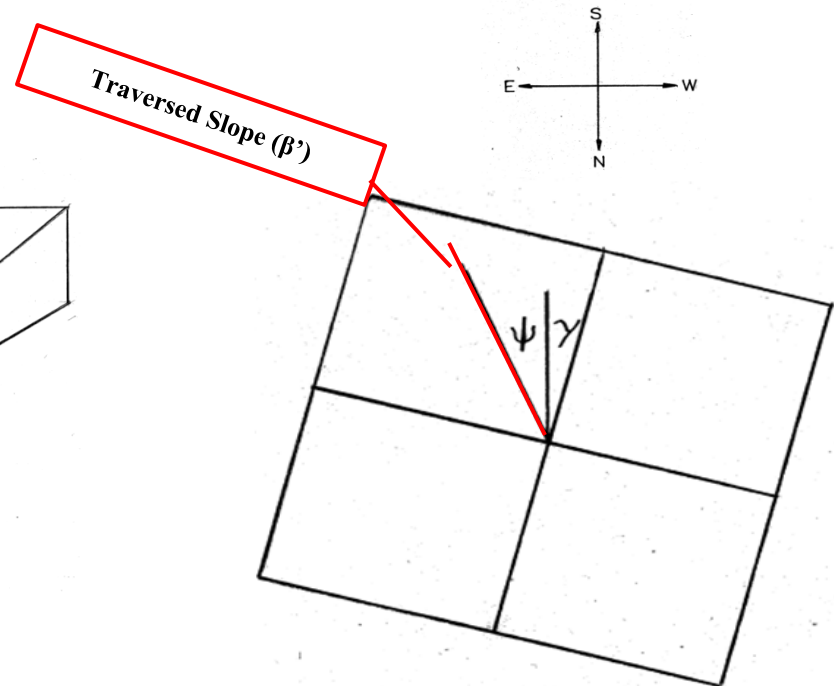


# Traversed Slope( $\beta'$ ) of Inclined Reflective Surface

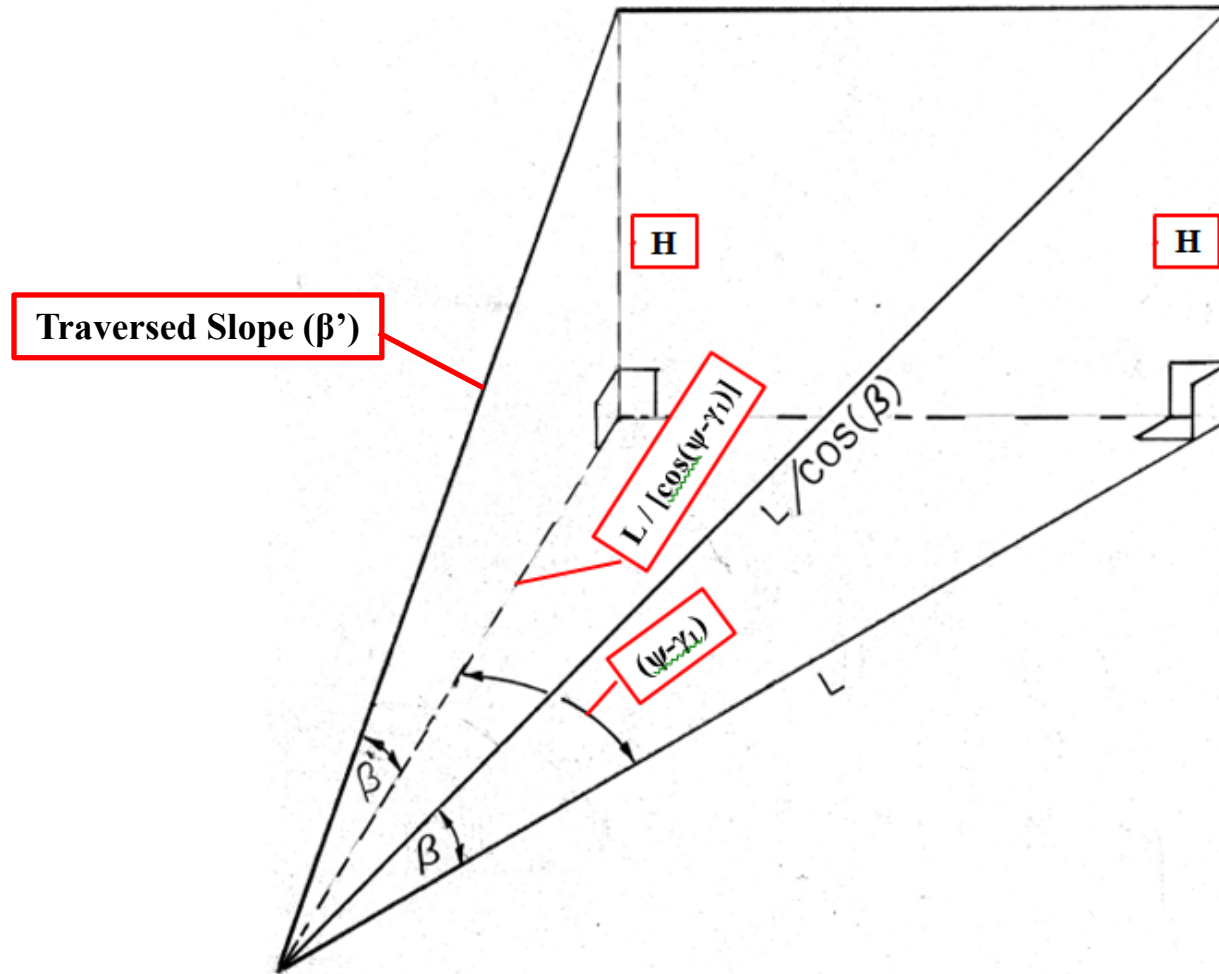
## Isometric View



## Plan View



# Sectioned Isometric View of Inclined Surface



# Reflection from Inclined Glass Surface Theory

**For Sunlight reflecting on the wall:**

$$J \cdot \cos(\psi - \gamma_1) \geq D$$

$$\tan(\psi - \gamma_1) = Z/D; \quad Z = D \cdot \tan(\psi - \gamma_1)$$

$$J^2 = Z^2 + D^2; \quad J = (Z^2 + D^2)^{0.5}$$

$$\text{Inflection Angle } (A_I) = \alpha - \beta'$$

$$\text{Reflected Angle } (A_R) = A_I - \beta'$$

$$\tan(A_R) = Y/J; \quad Y = J \cdot \tan(A_R)$$

$$\cos(\psi - \gamma_1) = D/J$$

$$G^2 = Y^2 + J^2$$

$$\cos(A_R) = J/G$$

$$\text{Ishingle} = IR \cdot \cos(A_R - \mu) \cdot \cos(\psi - \gamma_1 - \{\gamma_2 - \gamma_1\})$$

Incident Angle Factor =

$$[\cos(A_R - \mu) \cdot \cos(\psi - \gamma_1 - \{\gamma_2 - \gamma_1\})]$$

$$\text{Incident Angle} = A \cos[\text{Incident Angle Factor}]$$

$$\tan(\beta) = H/L; \quad H = L \cdot \tan(\beta)$$

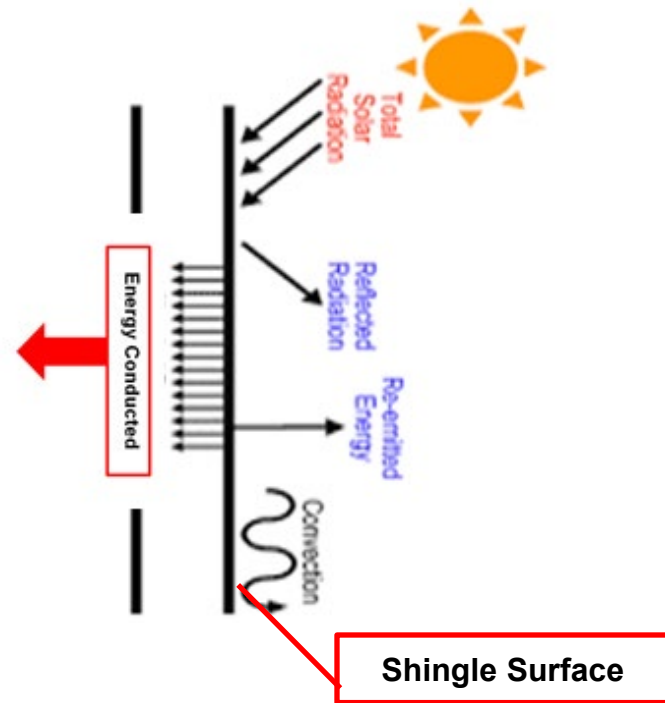
$$\begin{aligned} \tan(\beta') &= H / [L / \{\cos(\psi - \gamma_1)\}] \\ &= L \cdot \tan(\beta) / [L / \{\cos(\psi - \gamma_1)\}] \\ &= \tan(\beta) \cdot \cos(\psi - \gamma_1) \end{aligned}$$

$$B' = A \tan[\tan(\beta) \cdot \cos(\psi - \gamma_1)]$$

# Solar Radiation Surface Energy Balance

$$\sum Q = 0$$

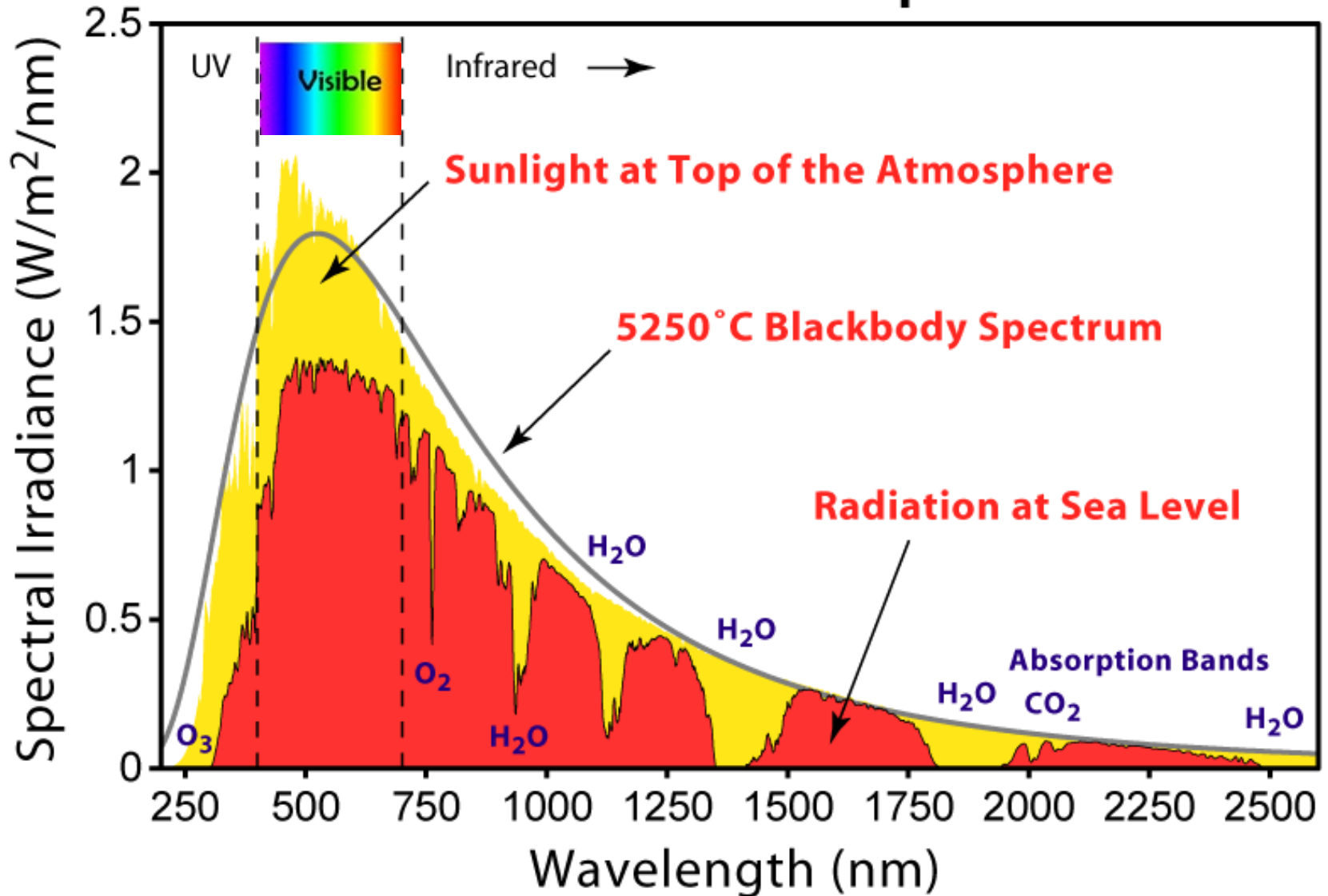
$$Q_{\text{Solar}} = Q_{\text{Reflected}} + Q_{\text{re-emitted}} + Q_{\text{Convection}} + Q_{\text{Surface Absorbed}}$$



**The solution to the above energy balance determines the temperature of the shingle surface at the equilibrium state.**



# Solar Radiation Spectrum



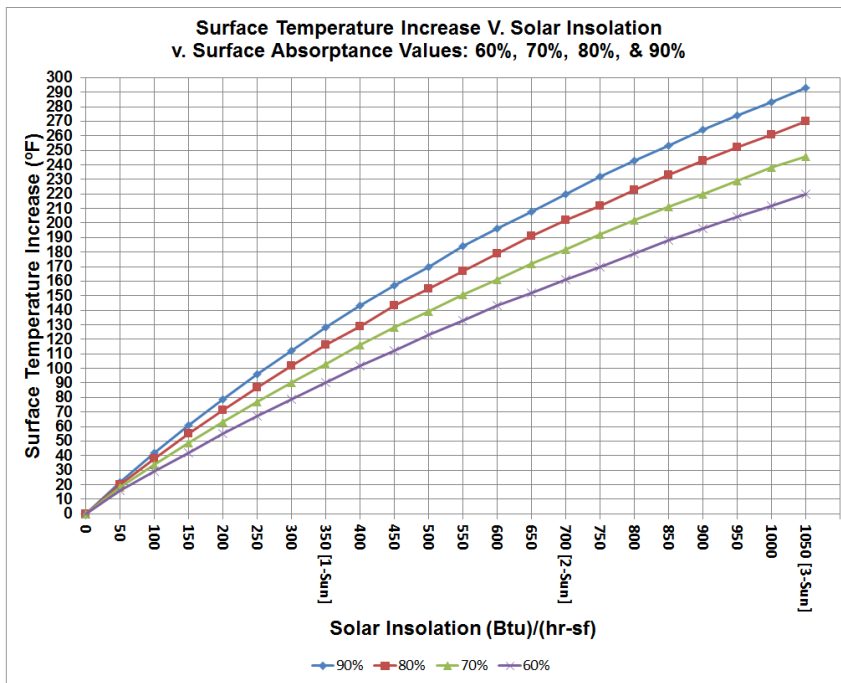
# Unpiloted Ignition Temperature

- **Western Red Cedar** 385°F
- Paper Birch 399°F
- White Pine 406°F
- White Oak 410°F
- Long Leaf Pine 428°F

Table 4.14A:

NFPA Fire Investigator Field Guide, 2<sup>nd</sup> Edition, 2013, pg. 103

# Solar Gain Shingle Surface Temperature Increase



Isolar Btu/(hr-sf)	Absorb	Tamb (°F)	ΔT (°F)	Shingle Temp (°F)
2,058.4	95%	20.0	460	480

Emissivity	0.90	Wind (mile/hr):	1.00	Tin:	72
		Wind (fps):	1.467	R-Value:	12

ΔT	Ts	Radiation	Convect 1	Convection	Envelope	Σ Q
0	20	0.0	0.0	0.0	-4.3	1959.8

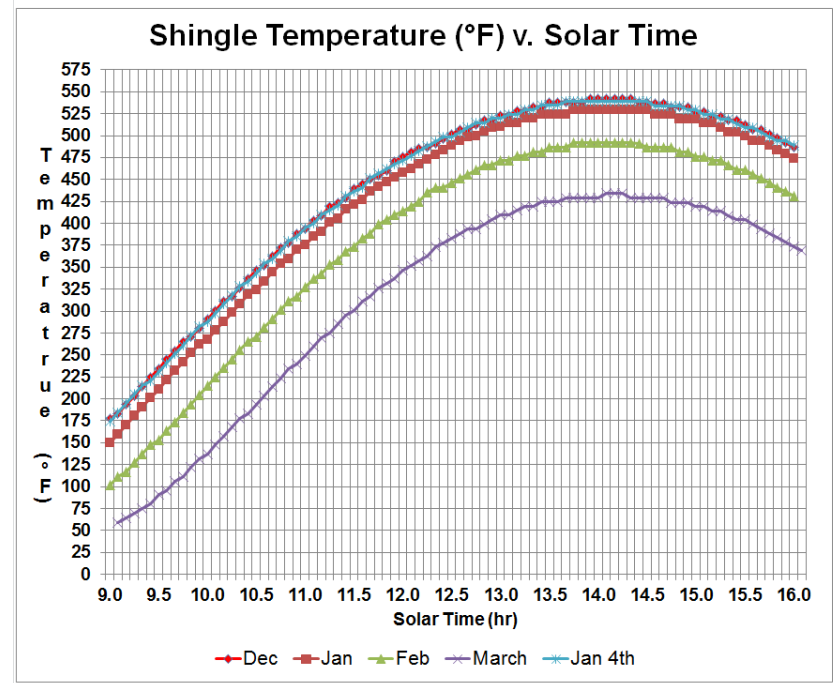
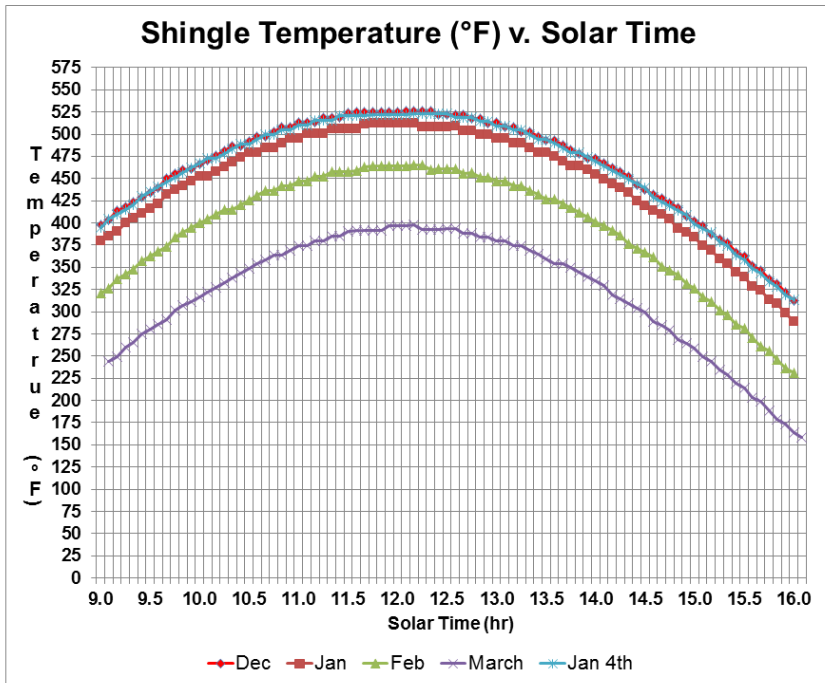
# Shingle Temperature (°F) v. Solar Time [ $\phi=42^\circ$ ]

$\gamma = 0^\circ$

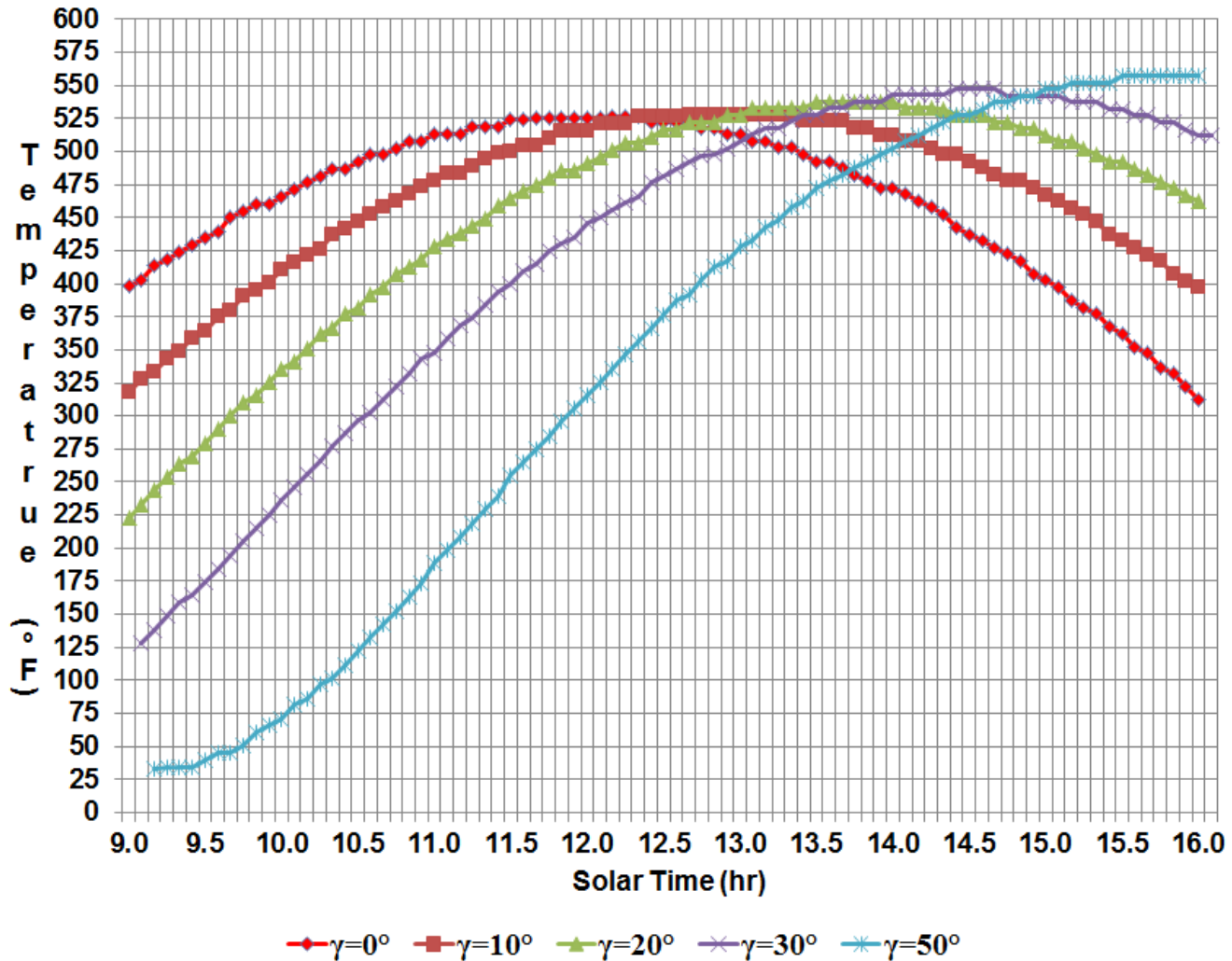
$\gamma = 25^\circ$

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 0.0$  Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.

D= 20 Feet      H<sub>r</sub>= 30 Feet  
 $\gamma = 25.0$  Degrees  
 Time Start: 9.0 hr.      Time End: 16.0 hr.



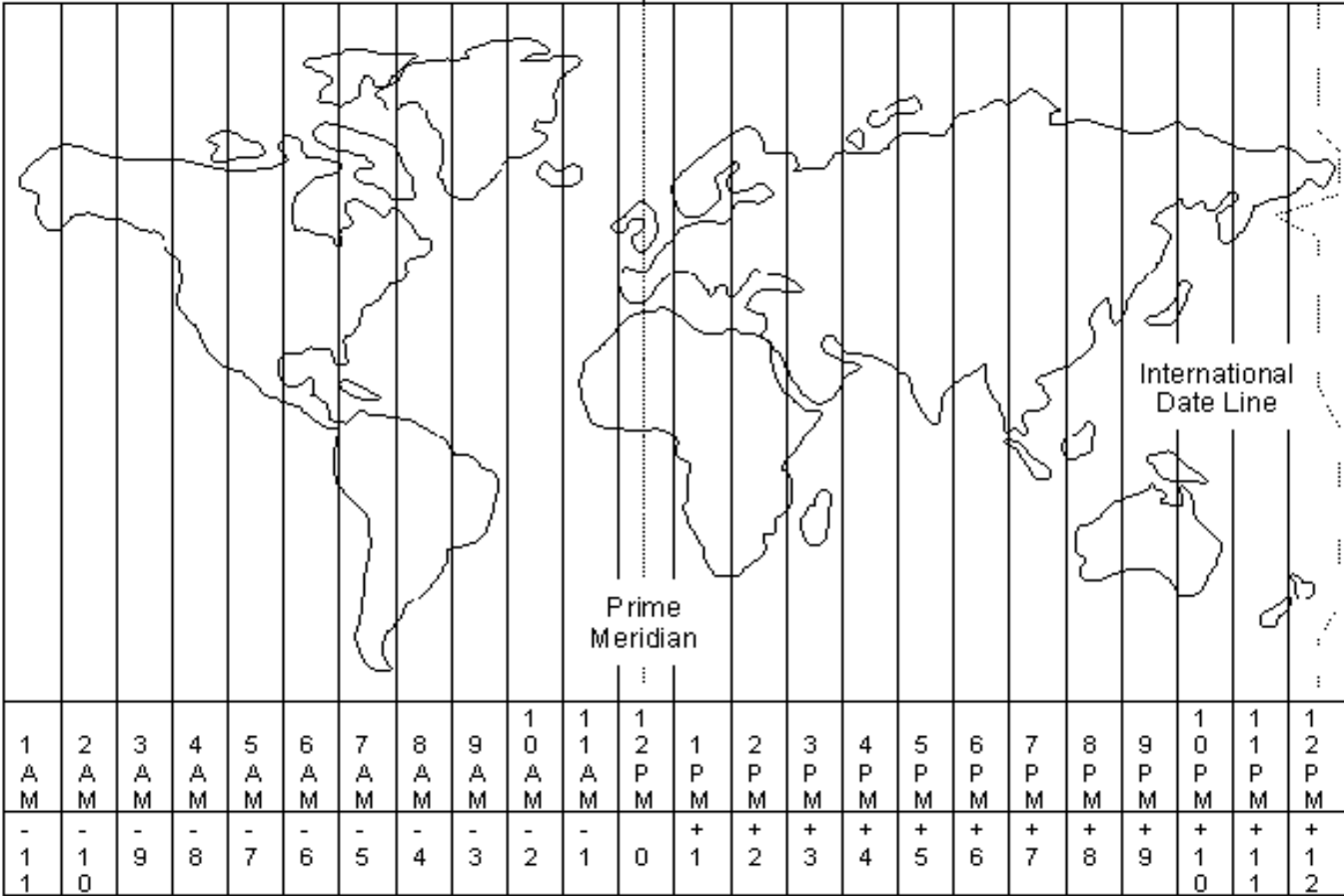
# Shingle Temperature (°F) v. Solar Time



# Actual Clock and Solar Time

## [Incident Time v. Solar Time]

# Global Time Zones



GMT, Greenwich Mean Time, London (Zulu)



# Time Zones in USA

## Earth Rotates 15° per hour



# Solar Time

- **APPARENT SOLAR TIME (AST)**
- **AST = LCT + TZ – LONG/15 + EQT/60**
- **AST=12.0 at solar noon.**
- **LCT = Local Clock Time**
- **TZ:**

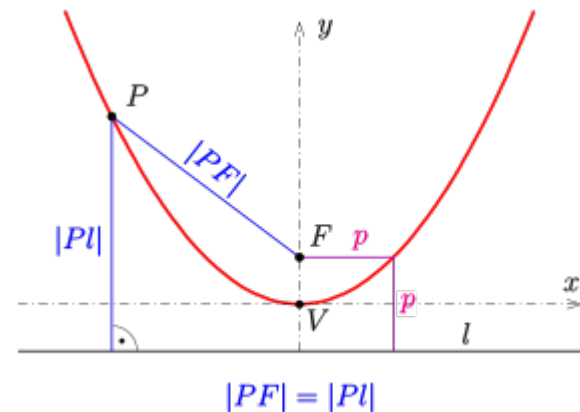
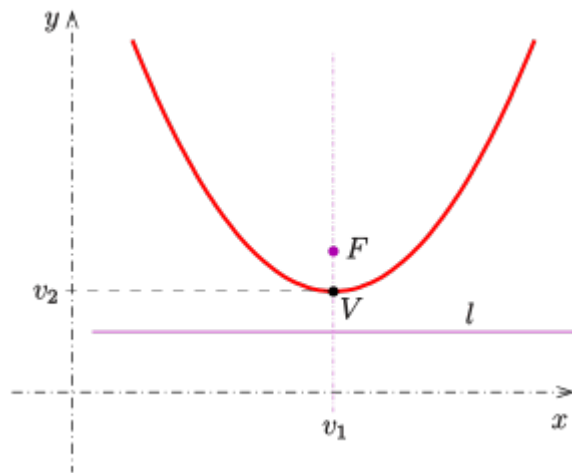
<b>EDT: +4,</b>	<b>EST: +5</b>
<b>CDT: +5,</b>	<b>CST: +6</b>
<b>MDT: +6,</b>	<b>MST: +7</b>
<b>PDT: +7,</b>	<b>PST: +8</b>
- **LONG = LOCAL LONGITUDE (+West, - East)**
- **EQT = 9.87sin(2B) - 7.53cos(B) – sin(B) [minutes]**
- **B =  $2\pi(N-81)/365$**

# Glass Deflection

# Properties of a Parabola

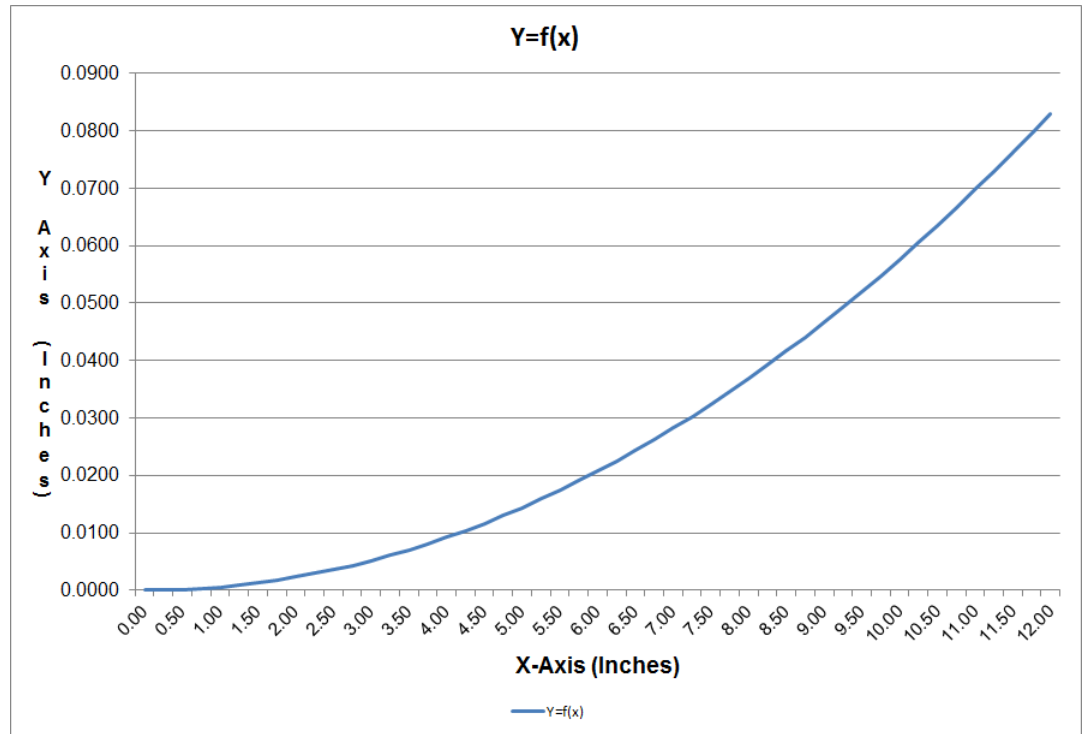
$$y = \frac{1}{4f}(x - v_1)^2 + v_2 = \frac{1}{4f}x^2 - \frac{v_1}{2f}x + \frac{v_1^2}{4f} + v_2.$$

$$P = 2f$$



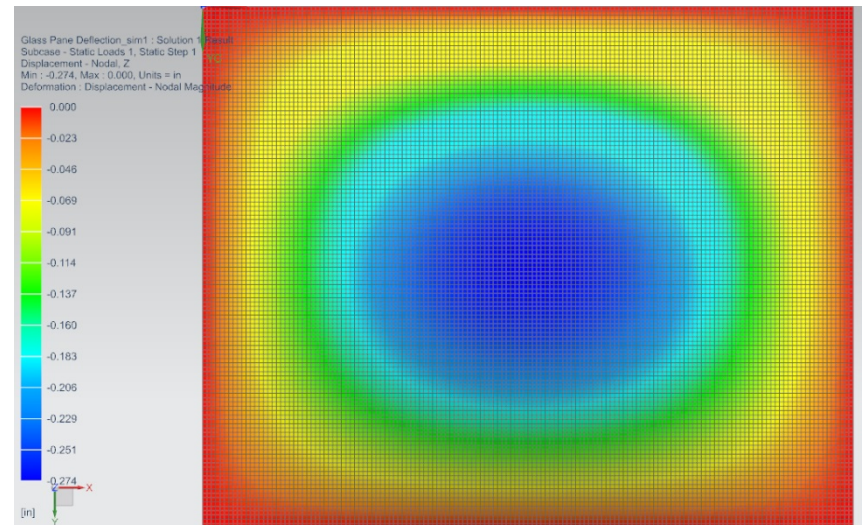
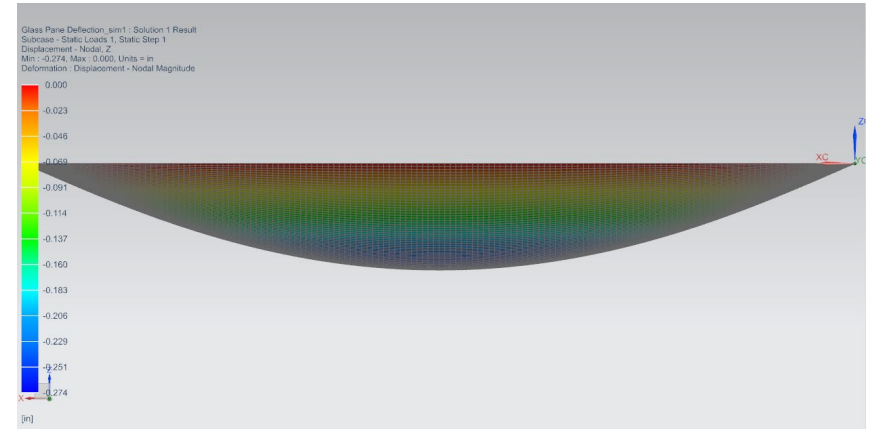
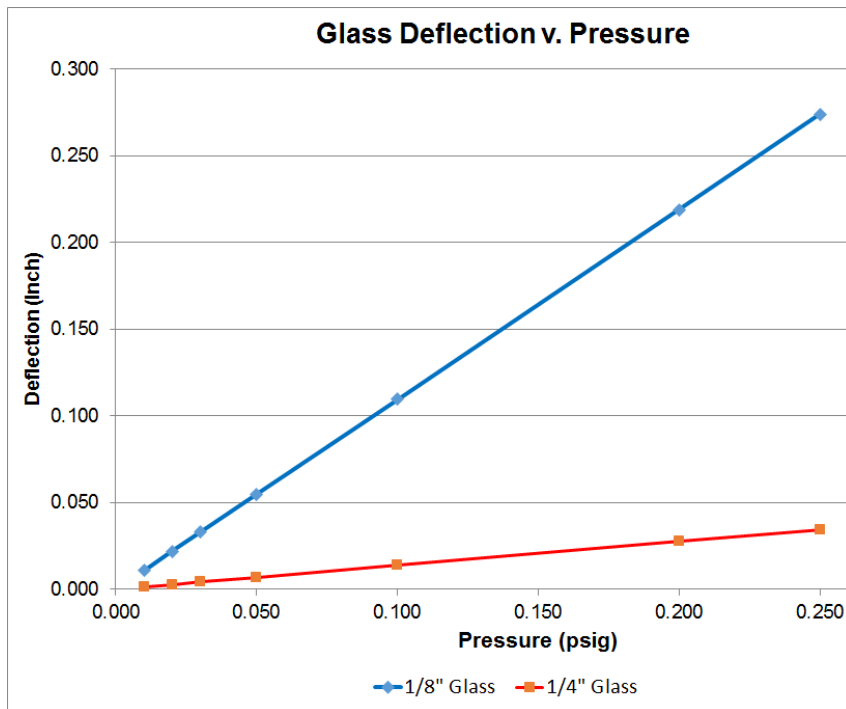
# Glass Deflection

Focus:	36.16 Ft
Window	24 In by
f	433.9 inch
X <sub>1</sub>	0.0 inch
Y <sub>1</sub>	0.0 inch
p	867.8 inch



# Window Deflection $\propto \Delta P, 1/t^3$

[NX Software by Siemens]

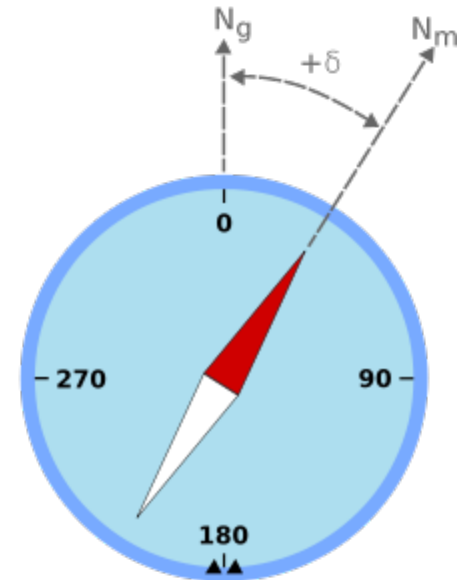
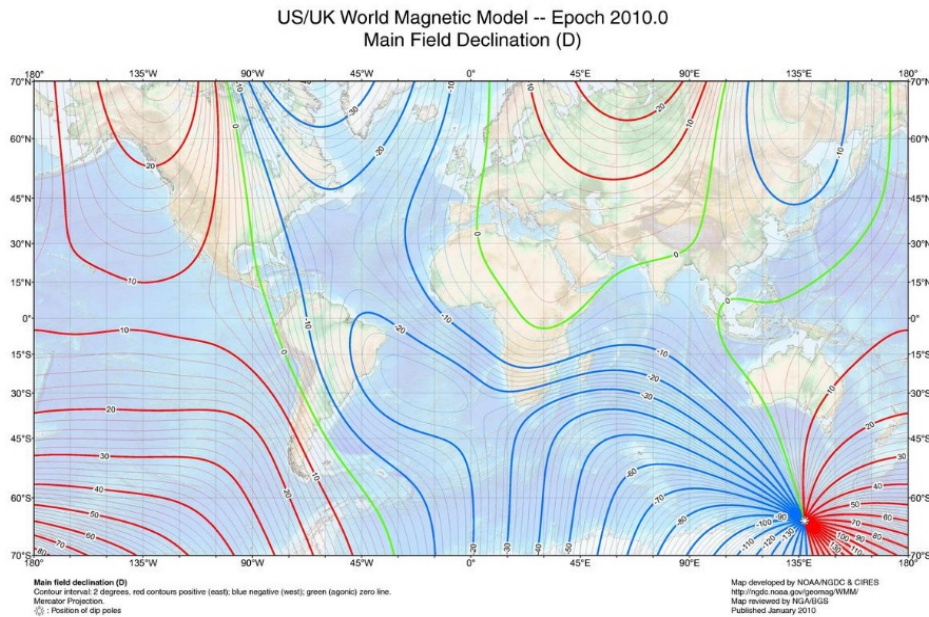


# Magnetic & True Orientation

# Geographic Coordinates

## Use of Satellite Data to Determine True Readings

Directional Headings, Magnetic Declination  
Use Surveyors compass  
[Cell phone compass is inaccurate]





# GPS Coordinates

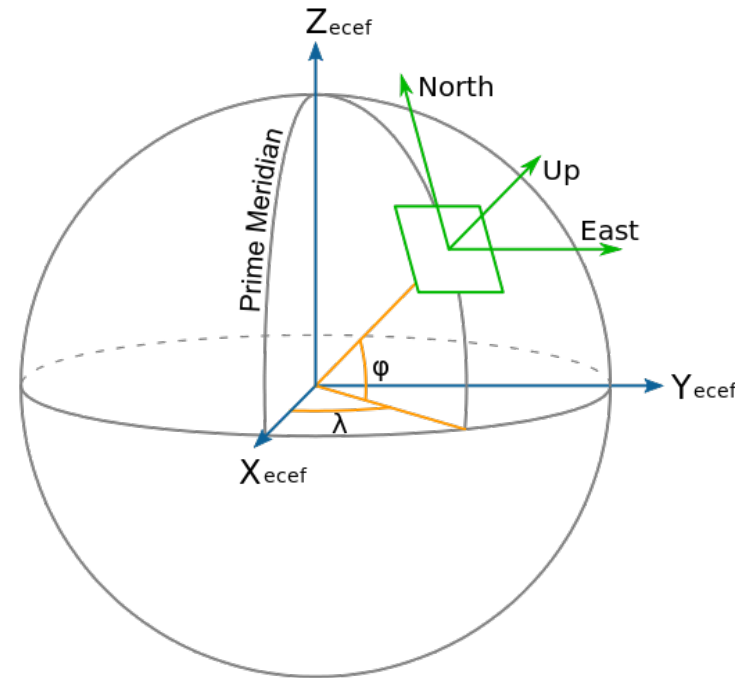
**DoubleTree** Hotel, 870 Williston Road  
South Burlington, Vermont

[www.latlong.net](http://www.latlong.net)

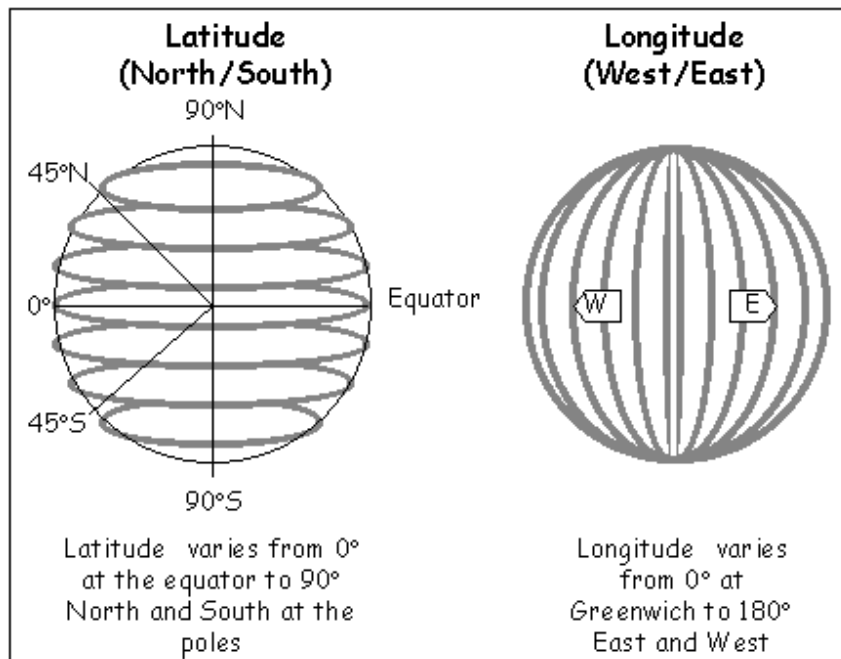
Lat: 44.472030° North

Long: -73.187140° West

**Convert to decimal  
coordinates**



# Building Orientation using Local Earth Radius & Satellite Data

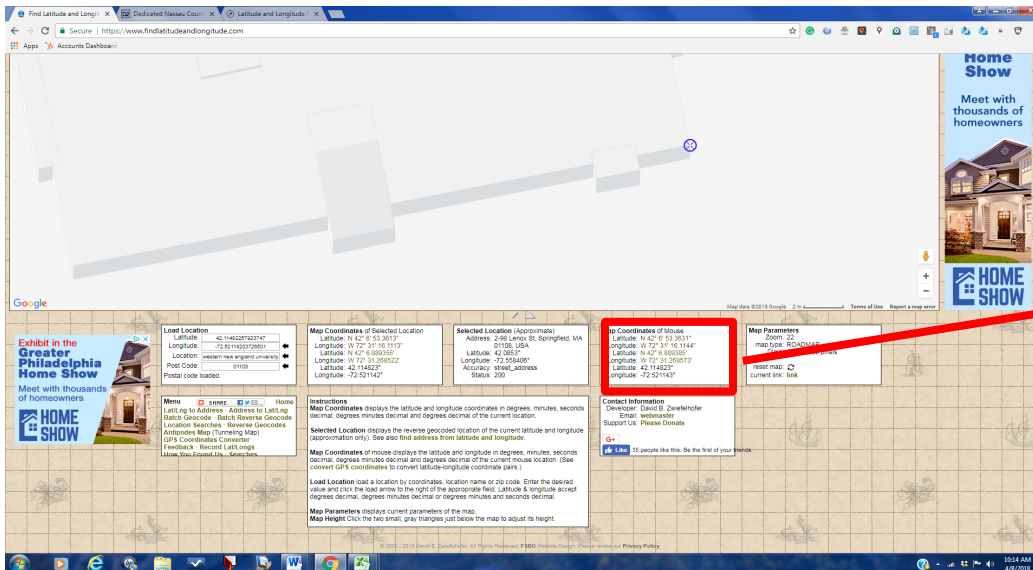


Earth Radius: 3,956 miles

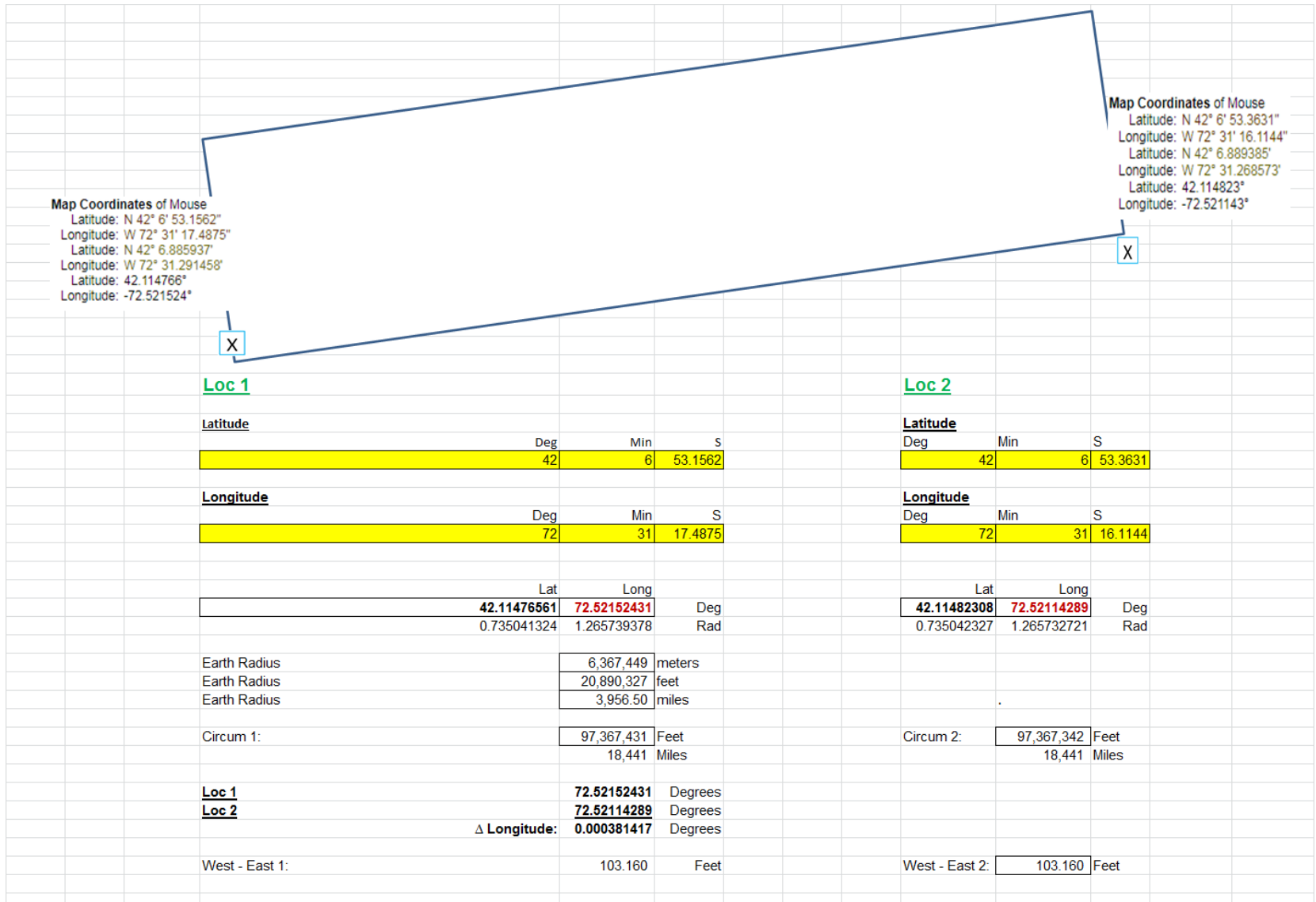
Local Earth Radius

= Radius at Equator x [Cos ( $\phi$ )]

# www.findlatitudeandlongitude.com



**Map Coordinates of Mouse**  
Latitude: N 42° 6' 53.3631"  
Longitude: W 72° 31' 16.1144"  
Latitude: N 42° 6.889385'  
Longitude: W 72° 31.268573'  
Latitude: 42.114823°  
Longitude: -72.521143°



**Loc 1**

<b>Latitude</b>			
	Deg	Min	S
	42	6	53.1562

<b>Longitude</b>			
	Deg	Min	S
	72	31	17.4875

	Lat	Long	
	42.11476561	72.52152431	Deg
	0.735041324	1.265739378	Rad

Earth Radius	6,367,449	meters
Earth Radius	20,890,327	feet
Earth Radius	3,956.50	miles

Circum 1:	97,367,431	Feet
	18,441	Miles

<b>Loc 1</b>	72.52152431	Degrees
<b>Loc 2</b>	72.52114289	Degrees
<b>Δ Longitude:</b>	0.000381417	Degrees

West - East 1:	103.160	Feet
----------------	---------	------

**Loc 2**

<b>Latitude</b>			
	Deg	Min	S
	42	6	53.3631

<b>Longitude</b>			
	Deg	Min	S
	72	31	16.1144

	Lat	Long	
	42.11482308	72.52114289	Deg
	0.735042327	1.265732721	Rad

Circum 2:	97,367,342	Feet
	18,441	Miles

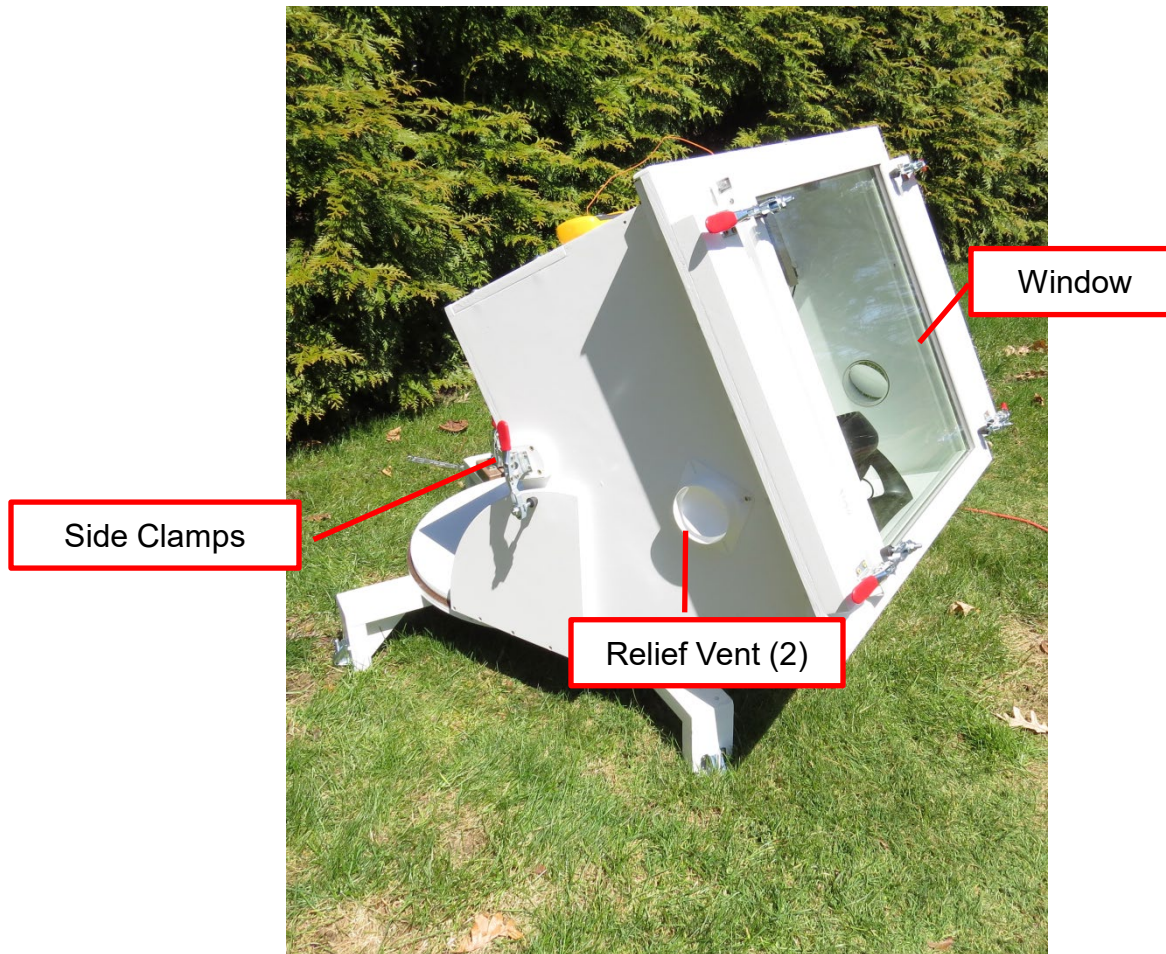
West - East 2:	103.160	Feet
----------------	---------	------

# Solar Reflections

# Isometric View

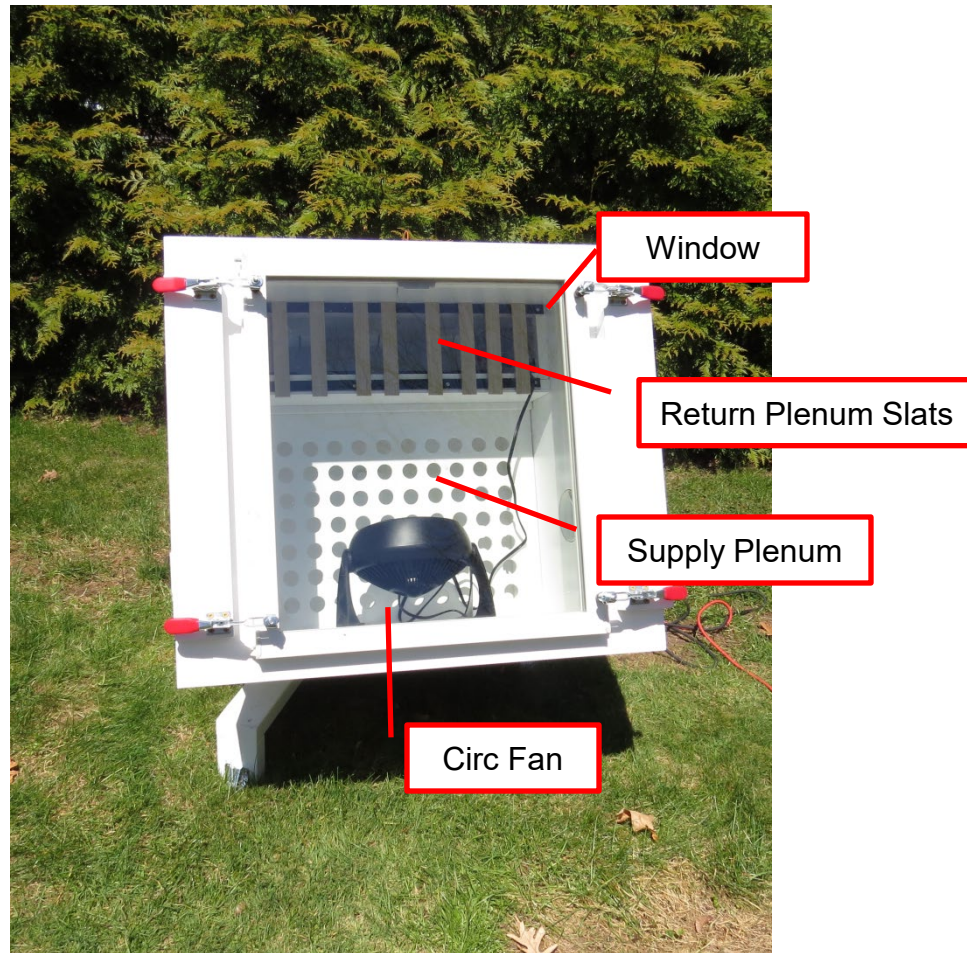
Base rotates on axis pin (not shown)

Side clamps allow pitch adjustment





# Front View



# Rear View

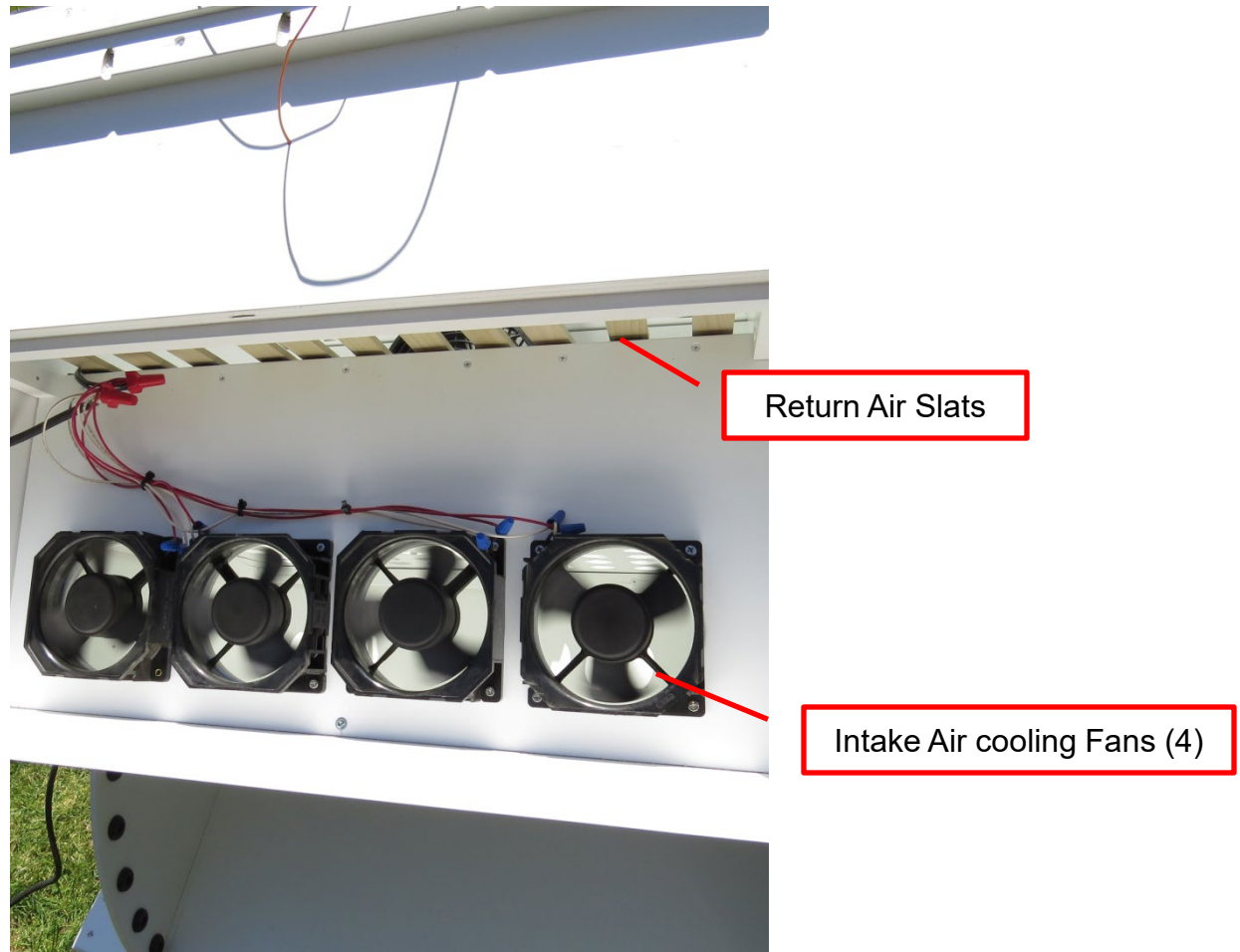


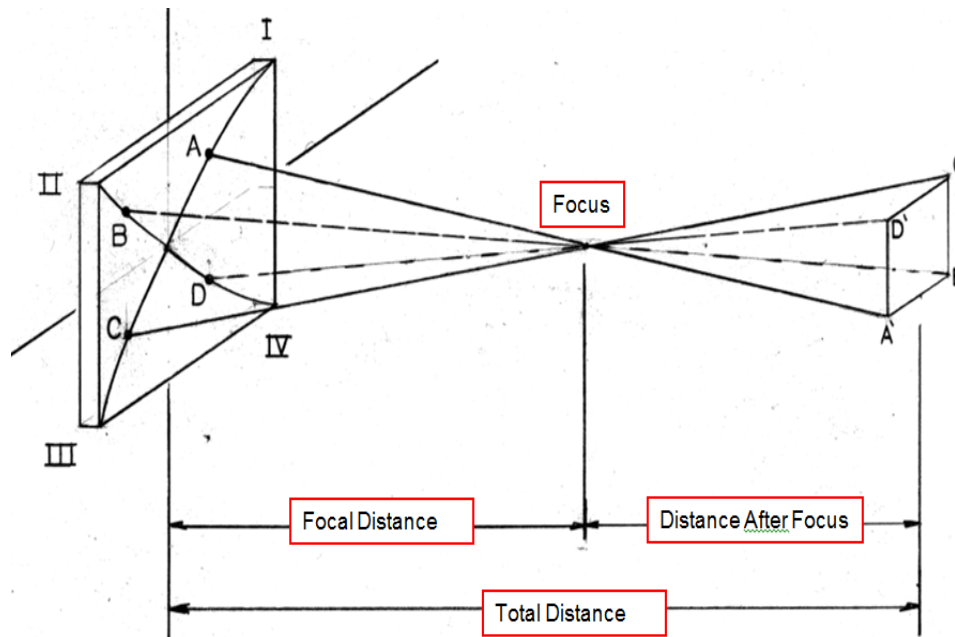
Temperature Monitor

Intake Air Vents



# Rear View with Cover Removed





## The Window surface is not a single Paraboloid

The window surface shape can be divided into four quadrants.

Each quadrant reflects light separately and collectively. Reflection direction by quadrant:

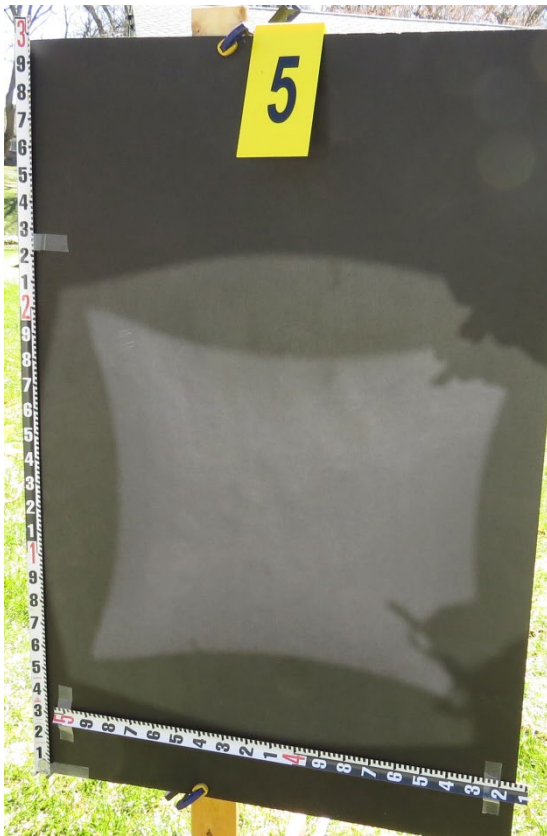
- |              |   |                |
|--------------|---|----------------|
| <b>I):</b>   | Right and Down; (Point <b>A</b> to Point <b>A'</b> ); | [Q1 on Photos] |
| <b>II):</b>  | Left and Down; (Point <b>B</b> to Point <b>B'</b> );  | [Q2 on Photos] |
| <b>III):</b> | Left and Up; (Point <b>C</b> to Point <b>C'</b> );    | [Q3 on Photos] |
| <b>IV):</b>  | Right and Up; (Point <b>D</b> to Point <b>D'</b> );   | [Q4 on Photos] |

# Typical View of Reflected Light on Black Foam Board Screen with Support Frame



Distances shown are from window to black screen

5'



10'



15'



20'

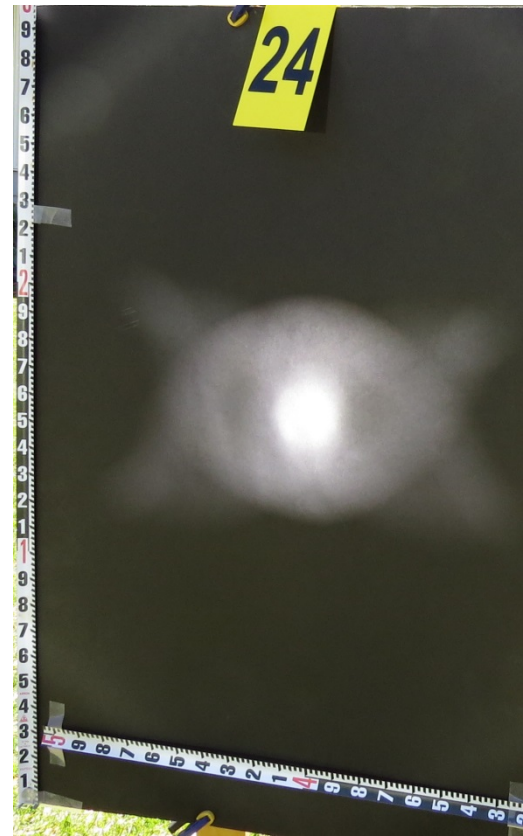




23'



24'

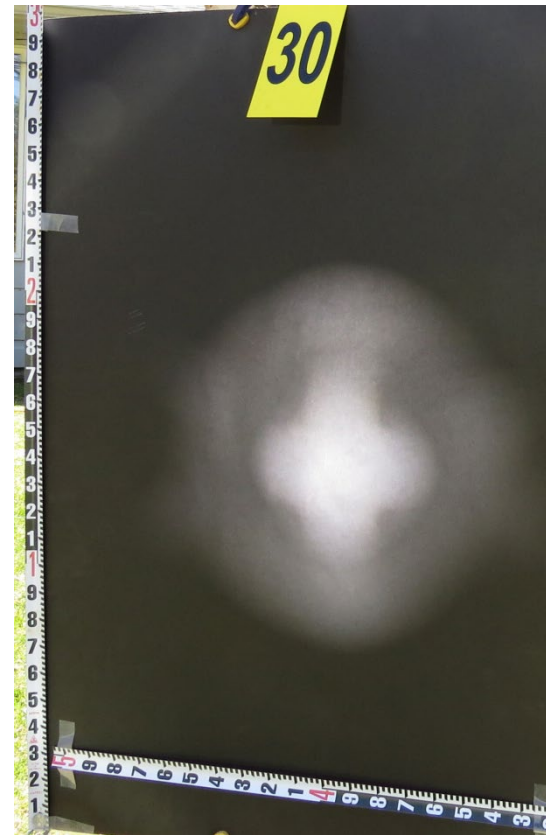


# Focal Distance: 22' – 25'

25'



30'



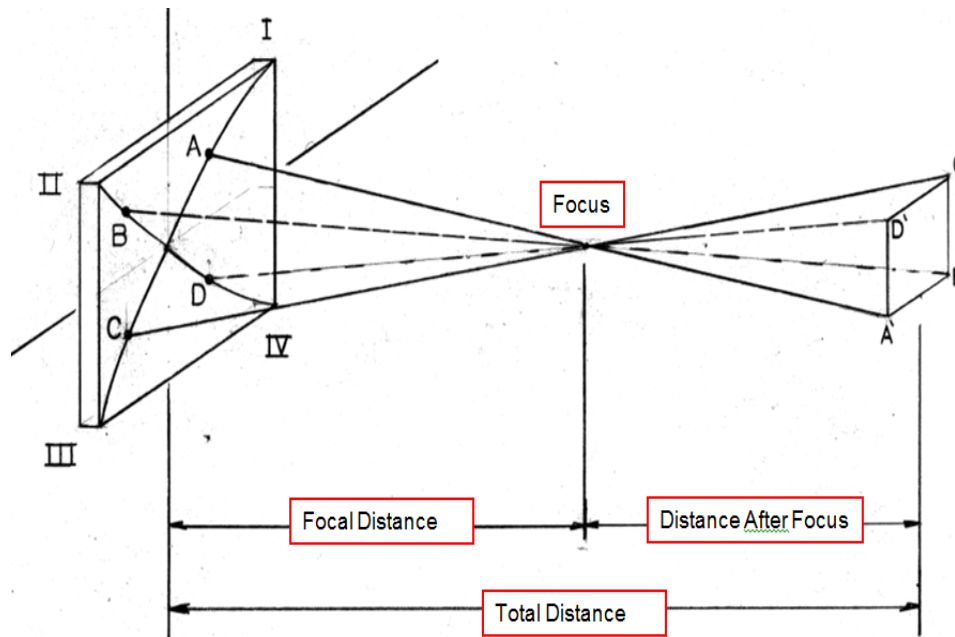
39'



40'







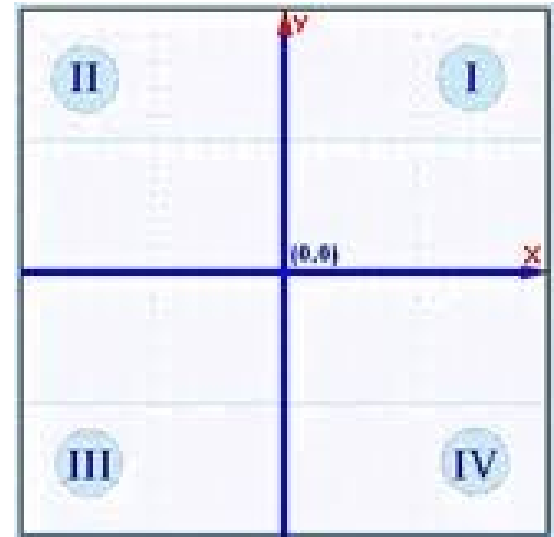
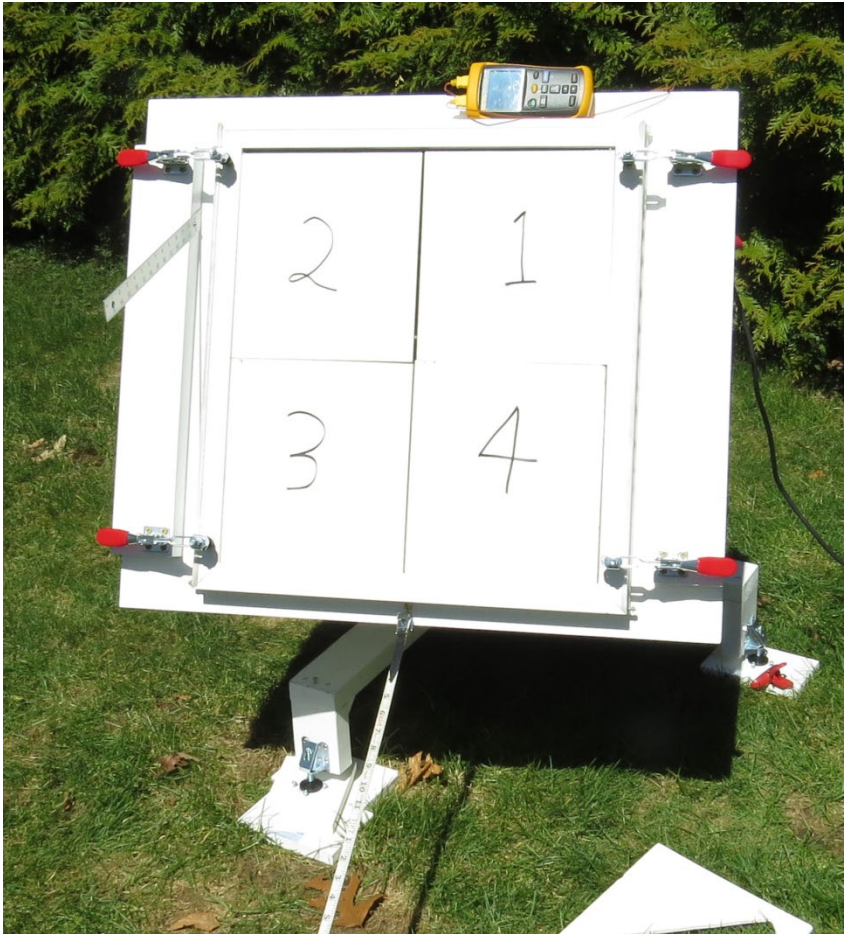
## The Window surface is not a single Paraboloid

The window surface shape can be divided into four quadrants.

Each quadrant reflects light separately and collectively. Reflection direction by quadrant:

- |              |   |                |
|--------------|---|----------------|
| <b>I):</b>   | Right and Down; (Point <b>A</b> to Point <b>A'</b> ); | [Q1 on Photos] |
| <b>II):</b>  | Left and Down; (Point <b>B</b> to Point <b>B'</b> );  | [Q2 on Photos] |
| <b>III):</b> | Left and Up; (Point <b>C</b> to Point <b>C'</b> );    | [Q3 on Photos] |
| <b>IV):</b>  | Right and Up; (Point <b>D</b> to Point <b>D'</b> );   | [Q4 on Photos] |

# Quadrants

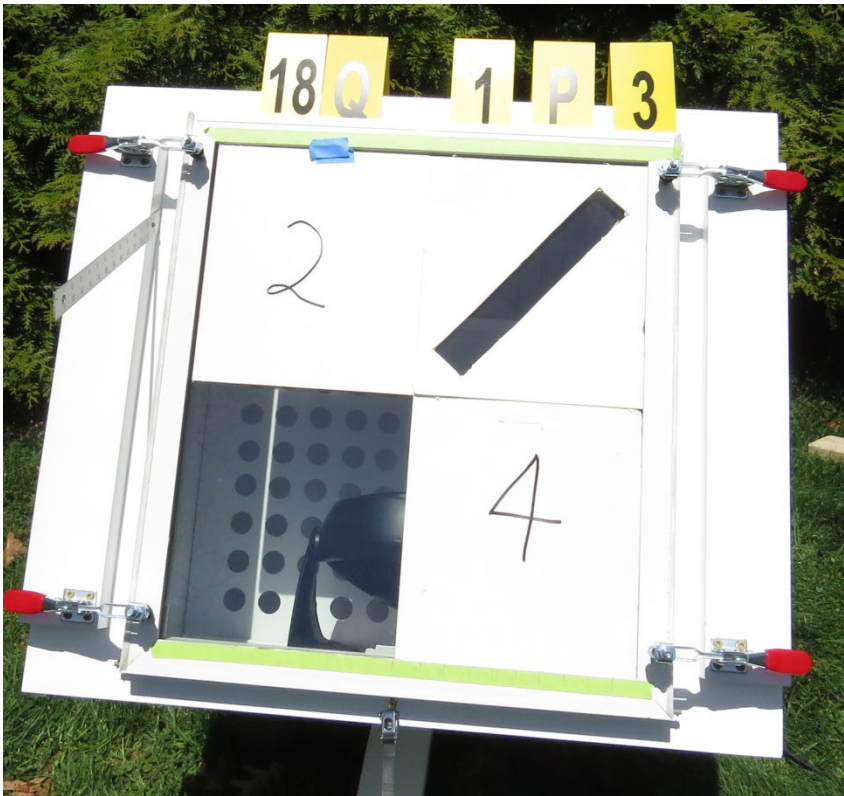


# Quadrant Evaluation



# Quadrant Evaluation

**18Q 1P 3**



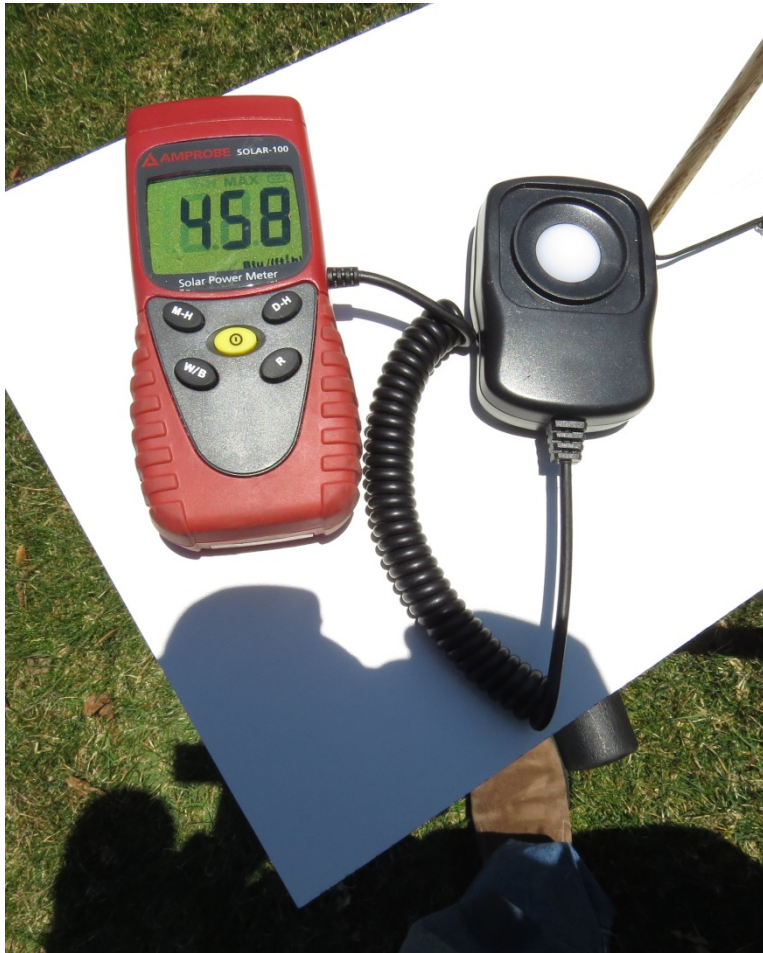
**18Q 1 P 3**



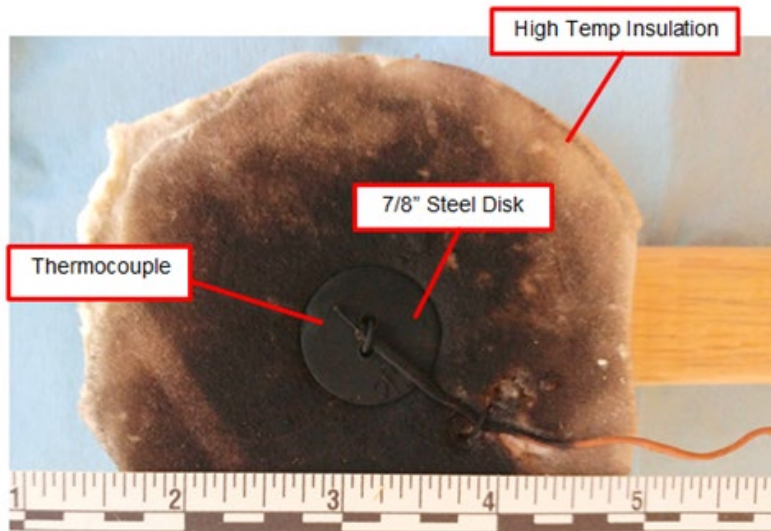
# Instrumentation



# Direct Normal Irradiation Readings [458 Btu/(hr-ft<sup>2</sup>)]



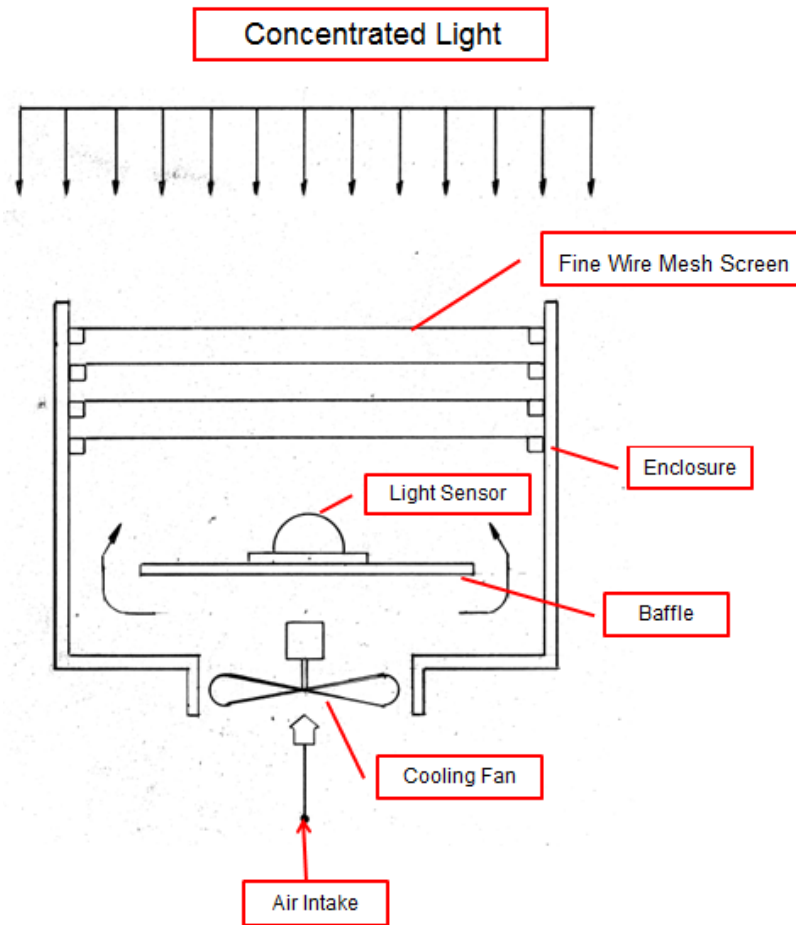
# Thermocouple on Blackened disk @ 21' (Absorbed Black Body Temp: 414°F)



# Concentrated Light Measuring Apparatus

[4-Layers of Wire Mesh Screen Shown Below]

[Patent Pending]

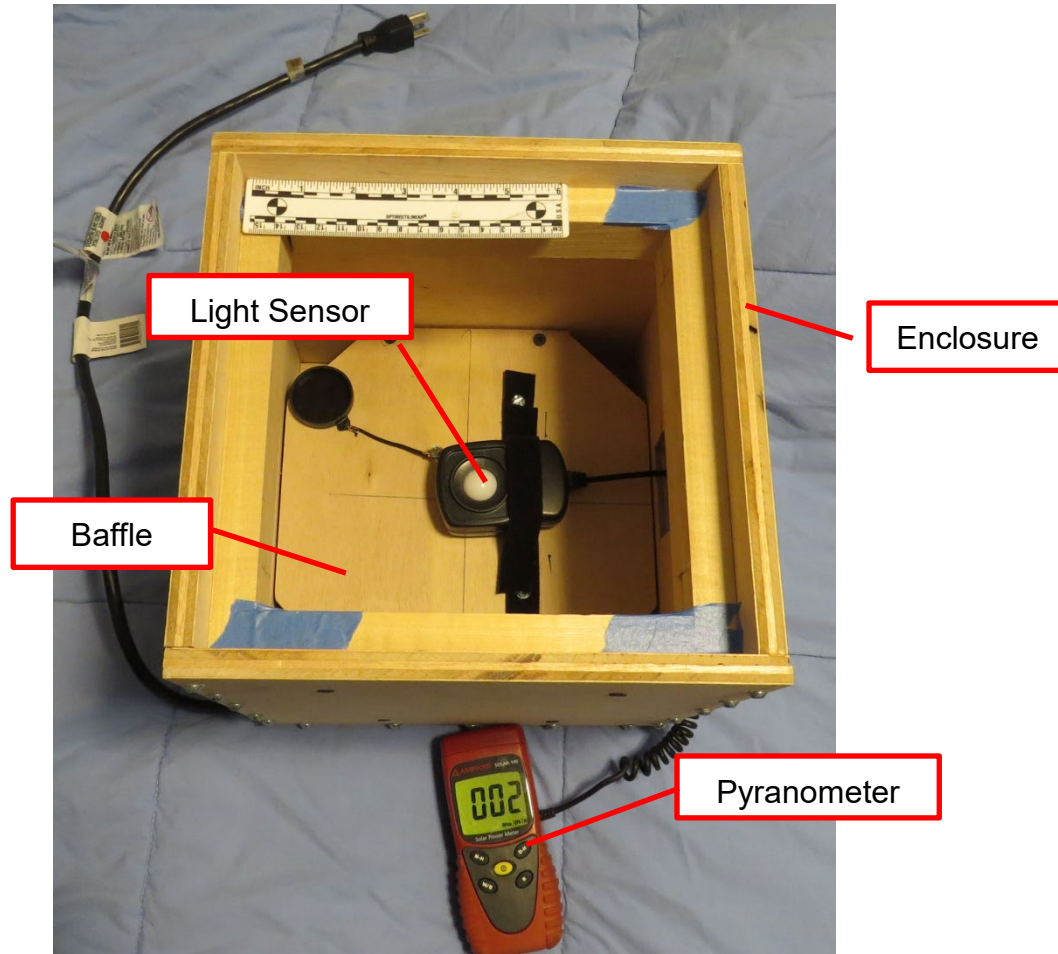




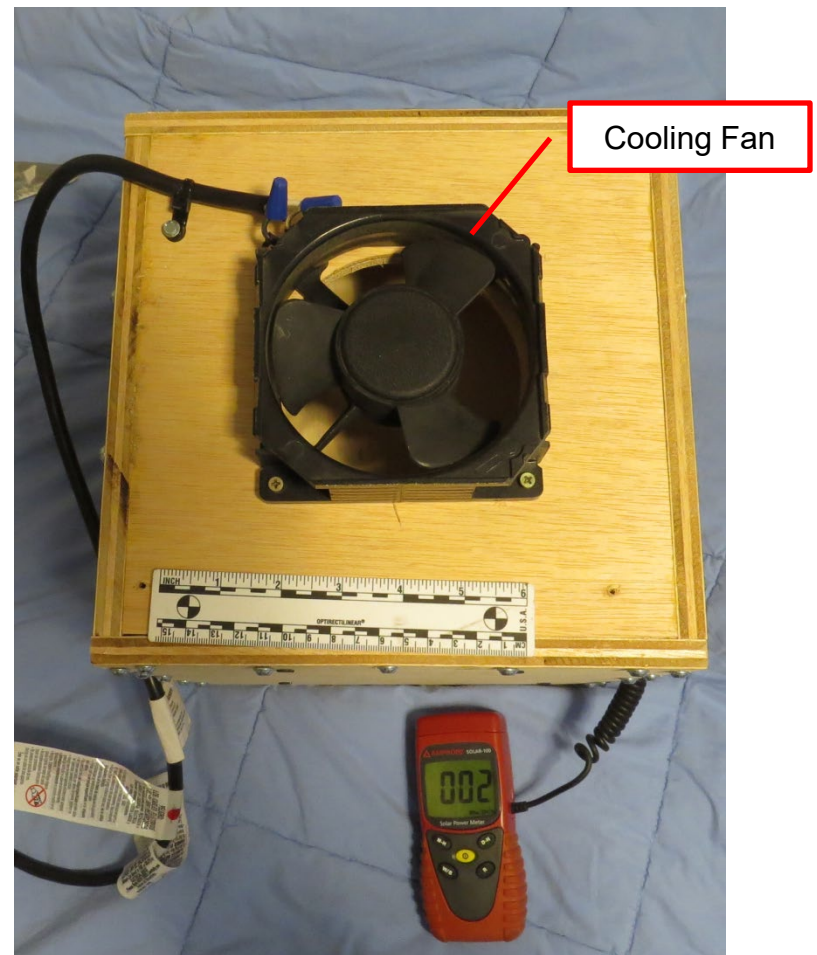
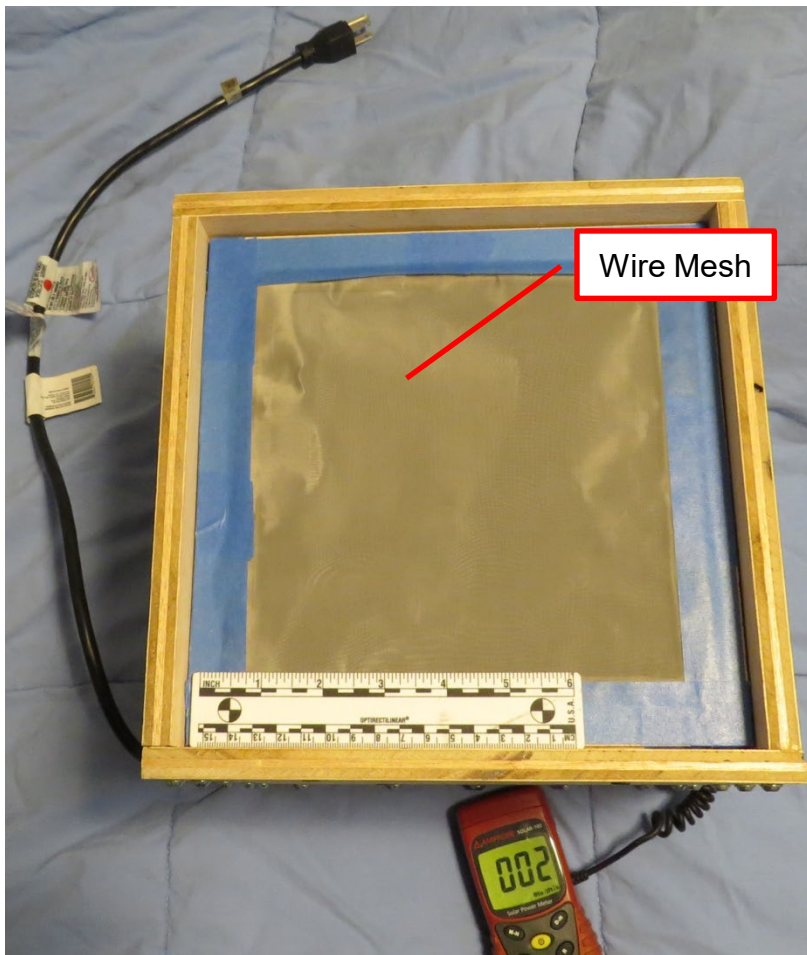
# Shade Coefficient

<b>Shade Coefficients per layer: 50.0%</b>		
<b><u>Layers</u></b>	<b><u>Shading</u></b>	<b><u>Light Transmission</u></b>
0	0.0%	100.0%
1	50.0%	50.0%
2	75.0%	25.0%
3	87.5%	12.5%
4	93.8%	6.3%
5	96.9%	3.1%
6	98.4%	1.6%

# Interior View (Wire Mesh Removed)



# Top & Bottom View (Wire Mesh Installed)



# Reflected sunlight > 12x Direct Sunlight





# Laser Survey Equipment



# Total Station



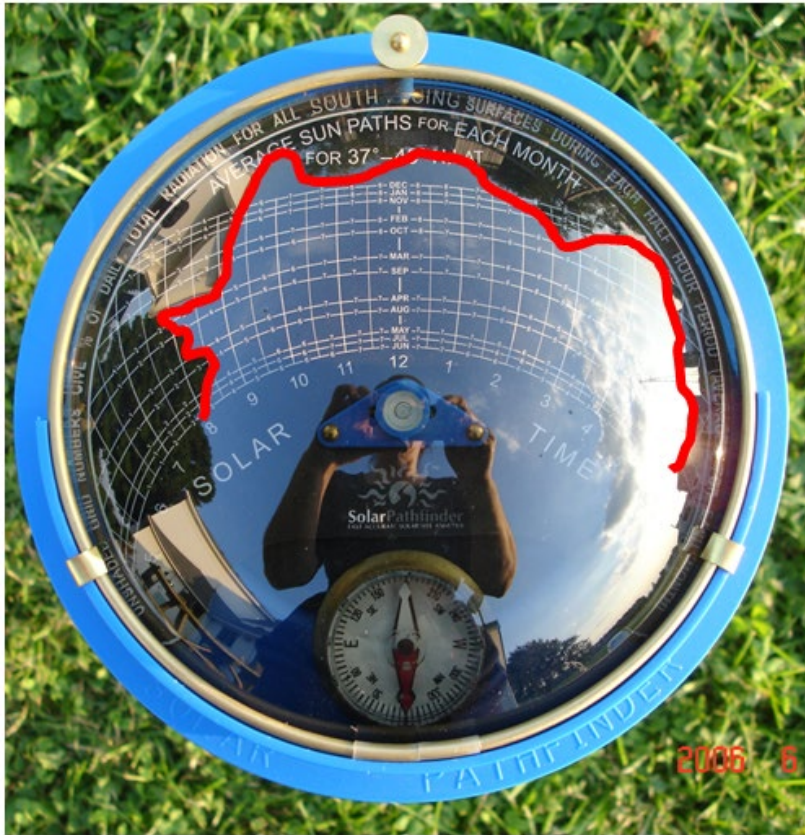
# Window Deflection Measurement





# Solar Pathfinder

## Azimuth and Altitude Seasonal Constraints

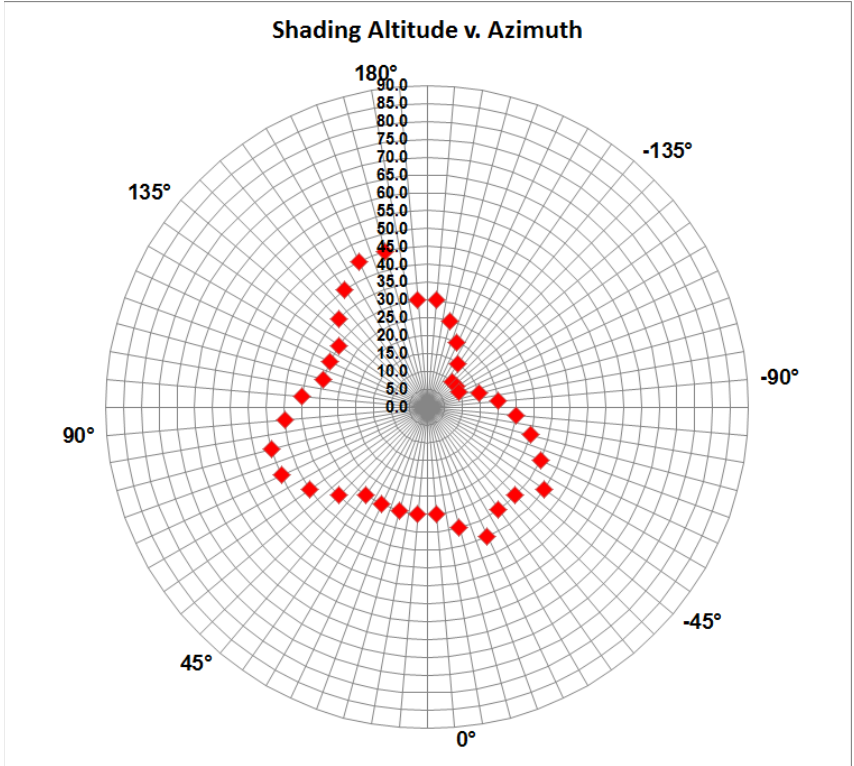
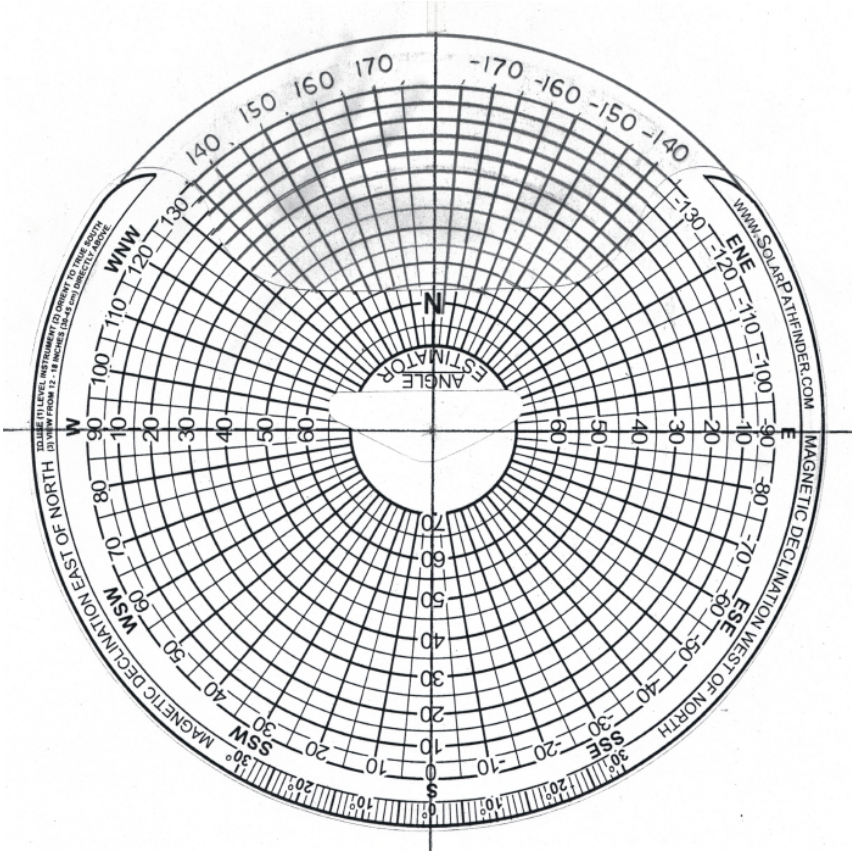




# SunEye 210



# Determination of Shade Factor





# Absorbed Blackbody Temperature: $\sim 700^{\circ}\text{F}$

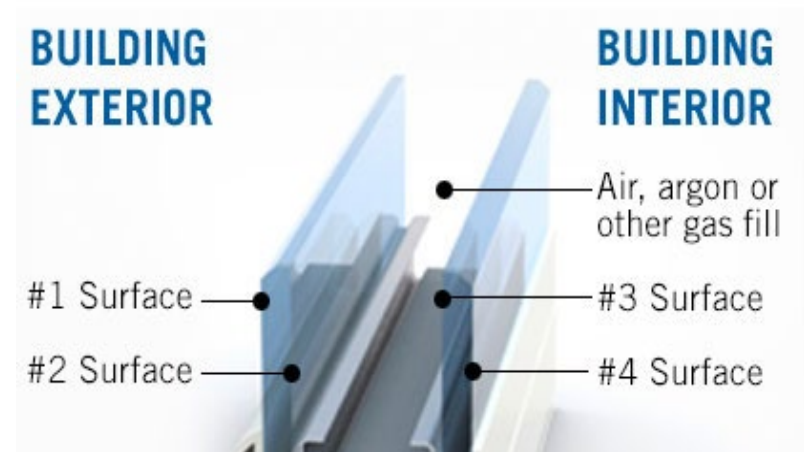


# Conclusions

- 1) Western Red cedar has an unpiloted ignition temperatures of only 385°F and can spontaneously ignite with concentrated reflected sunlight.
- 2) Low E Glass can become parabolic-like and reflects concentrated sunlight with irradiation that will damage buildings & ignite combustible surfaces. Absorbed blackbody temperatures documented at >530°F; solar concentrations can be > 12x direct sunlight.
- 3) Concentrated reflected sunlight from Low E Glass can be profoundly dangerous to human eye safety.

# Resolutions

- 1) Install Exterior screening or shading.
- 2) Use 1/4" thick glass to increase focal distance.
- 3) Install clear thermopane with interior tint.
- 4) Tint exterior pane; use Low E glass with reflective coating on #3 surface.



# Learning Question

The focal distance of concentrated reflected light is affected by:

- a) Ambient temperature
- b) Intensity of solar insolation
- c) Wind velocity
- d) Atmospheric conditions
- e) Day number
- f) Thickness of glass
- g) Interior temperature
- h) Building orientation
- i) Pitch of window
- j) a, c, f, g, & h
- k) All of the above



# Answer

k) All of the above

# Questions?

(Photos captured at an engineering college in the Northeast)

